

#### Learning Outcomes of this Lecture

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This module is designed to help you learn about:

- The notion of *Abstract Data Types (ADTs)*
- **ADTs**: Stack vs. Queue
- Implementing <u>Stack</u> and <u>Queue</u> in Java [interface, classes]
- · Applications of Stacks vs. Queues
- Circular Arrays
- <u>Optional</u> (but highly <u>encouraged</u>):
  - Criterion of *Modularity*, Modular Design
  - *Dynamic* Arrays, *Amortized* Analysis

# Java API Approximates ADTs (1)



#### It is useful to have:

- A *generic collection class* where the *homogeneous type* of elements are parameterized as E.
- A reasonably *intuitive overview* of the ADT.

Java 8 List API

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## Java API Approximates ADTs (2)

E	<pre>set(int index, E element) Replaces the element at the specified position in this list with the specified element (optional operation).</pre>
s <b>et</b> E set(int index, E element)	
Replaces the element at	the specified position in this list with the specified element (optional operation).
Parameters:	
index - index of the	element to replace
element - element to	be stored at the specified position
Returns:	
the element previous	y at the specified position
Throws:	
UnsupportedOperation	xception - if the set operation is not supported by this list
ClassCastException -	if the class of the specified element prevents it from being added to this list
NullPointerException	- if the specified element is null and this list does not permit null elements
IllegalArgumentExcept	ion - if some property of the specified element prevents it from being added to this list
	tion - if the index is out of range (index < $\theta$    index >= size())

Methods described in a *natural language* can be *ambiguous*.

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## What is a Stack?

- A *stack* is a collection of objects.
- Objects in a *stack* are inserted and removed according to the *last-in, first-out (LIFO)* principle.

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- *Cannot* access arbitrary elements of a stack
- *Can* only access or remove the *most-recently added* element



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## **Building ADTs for Reusability**

ADTs are reusable software components that are common for
solving many real-world problems.
e.g., Stacks, Queues, Lists, Tables, Trees, Graphs
An ADT, once thoroughly tested, can be reused by:
<ul> <li>Clients of Applications</li> </ul>
<ul> <li>Suppliers of other ADTs</li> </ul>
As a supplier, you are obliged to:
• <i>Implement</i> standard ADTs [≈ lego building bricks]
Note. Recall the basic data structures: arrays vs. SLLs vs. DLLs
• <b>Design</b> algorithms using standard ADTs [ $\approx$ lego houses, ships ]
For each <u>standard ADT</u> , you should know its interface:
• Stored <i>data</i>
<ul> <li>For each operation manipulating the stored data</li> </ul>
<ul> <li>How are <i>clients</i> supposed to use the method?</li> </ul>
What are the services provided by <i>suppliers</i> ?
<ul> <li>Time (and sometimes space) complexity</li> </ul>
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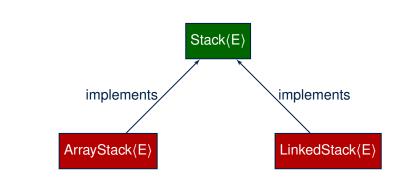
## **The Stack ADT**

• top	
	[ precondition: stack is not empty ]
	[ postcondition: return item last pushed to the stack ]
• size	
	[ precondition: none ]
	[ postcondition: return number of items pushed to the stack ]
• isEmpty	
	[precondition: none]
	[ <i>postcondition</i> : return whether there is <u>no</u> item in the stack ]
• push(item	n)
	[ precondition: stack is not full ]
	[ postcondition: push the input item onto the top of the stack ]
• <i>pop</i>	
pop	[ precondition: stack is not empty ]
	[ postcondition: remove and return the top of stack ]
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## Stack: Illustration

	RETURN VALUE	STACK CONTENTS
OPERATION	RETURN VALUE	STACK CONTENTS
-	-	Ø
isEmpty	true	Ø
push(5)	_	5
push(3)	_	3 5
,		5
push(1)	_	1 3 5
1 ()		
size	3	1 3 5
	-	5
top	1	1 3 5
top		5
рор	1	<u>3</u> 5
P0P		
рор	3	5
рор	5	Ø

### **Generic Stack: Architecture**



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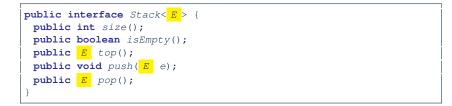
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**Generic Stack: Interface** 



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The *Stack* ADT, declared as an *interface*, allows *alternative implementations* to conform to its method headers.



<pre>public class ArrayStack<e> implements Stack<e> {     private final int MAX_CAPACITY = 1000;     private E[] data;</e></e></pre>
<pre>private int t; /* index of top */</pre>
<pre>public ArrayStack() {</pre>
• • • • • • • • • • • • • • • • • • •
<pre>data = (E[]) new Object[MAX_CAPACITY];</pre>
t = -1;
}
<pre>public int size() { return (t + 1); }</pre>
<pre>public boolean isEmpty() { return (t == -1); }</pre>
<pre>public E top() {</pre>
<pre>if (isEmpty()) { /* Precondition Violated */ }</pre>
else { return data[t]; }
1
<pre>public void push(E e) {</pre>
if (size() == MAX CAPACITY) { /* Precondition Violated */ }
<b>else</b> { t ++; data[t] = e; }
}
public E pop() {
E result;
<pre>if (isEmpty()) { /* Precondition Violated */ }</pre>
<pre>else { result = data[t]; data[t] = null; t; }</pre>
return result;
}
3
3

#### Implementing Stack: Array (2)



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• Running Times of Array-Based Stack Operations?

ArrayStack Method	Running Time
size	O(1)
isEmpty	O(1)
top	O(1)
push	O(1)
рор	O(1)

- <u>Exercise</u> This version of implementation treats the *end* of array as the *top* of stack. Would the RTs of operations <u>change</u> if we treated the *beginning* of array as the *top* of stack?
- Q. What if the preset capacity turns out to be insufficient?

A. IllegalArgumentException occurs and it takes O(1) time to respond.

• At the end, we will explore the alternative of a *dynamic array*.

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#### Implementing Stack: Singly-Linked List (2)



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- If the *front of list* is treated as the *top of stack*, then:
  - All stack operations remain O(1) [.: removeFirst takes O(1)]
- If the end of list is treated as the top of stack, then:
  - The *pop* operation takes *O(n)* [:: removeLast takes *O(n)*]
- But in both cases, given that a linked, *dynamic* structure is used, *no resizing* is necessary!

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Implementing Stack: Singly-Linked List (1)

public class LinkedStack<E> implements Stack<E> {
 private SinglyLinkedList<E> list;
 ...

#### Question:

Stack Method	Singly-Linked	d List Method
Slack Melliou	Strategy 1	Strategy 2
size	list.size	
isEmpty	list.isEmpty	
top	list.first	list.last
push	list.addFirst	list.addLast
рор	list.removeFirst	list.removeLast

Which implementation strategy should be chosen?

## **Generic Stack: Testing Implementations**

#### @Test

public void testPolymorphicStacks() {
 Stack<String> s = new ArrayStack<>();
 s.push("Alan"); /\* dynamic binding \*/
 s.push("Mark"); /\* dynamic binding \*/
 assertTrue(s.size() == 3 && !s.isEmpty());
 assertEquals("Tom", s.top());

 s = new LinkedStack<>();
 s.push("Alan"); /\* dynamic binding \*/
 s.push("Mark"); /\* dynamic binding \*/

s.push("Tom"); /\* dynamic binding \*/
assertTrue(s.size() == 3 && !s.isEmpty());
assertEquals("Tom", s.top());

## **Polymorphism & Dynamic Binding**



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#### Stack<String> myStack;

- myStack = new ArrayStack<String>();
- 3 myStack.push("Alan"); 4
  - myStack = new LinkedStack<String>();
  - myStack.push("Alan");

#### Polymorphism

An object may change its "shape" (i.e., dynamic type) at runtime.

Which lines? 2, 4

Dynamic Binding

Effect of a method call depends on the "current shape" of the target object.

Which lines? 3, 5

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1 2

5

## Stack Application: Matching Delimiters (1)



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#### Problem

Opening delimiters: (, [, { Closing delimiters: ), ], } e.g., **Correct**: () (()) { ([()]) } e.g., **Incorrect**: ({[])}

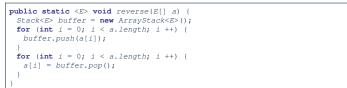
#### Sketch of Solution

- When a new opening delimiter is found, push it to the stack.
- Most-recently found delimiter should be matched first.
- When a new *closing* delimiter is found:
  - If it matches the top of the stack, then pop off the stack.
  - Otherwise, an error is found!
- Finishing reading the input, an empty stack means a success!

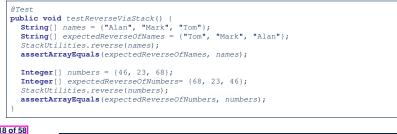
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## Stack Application: Reversing an Array

• *Implementing* a *generic* algorithm:



#### • Testing the generic algorithm:



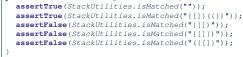
## Stack Application: Matching Delimiters (2)

#### Implementing the algorithm:

```
public static boolean isMatched(String expression) {
    final String opening = "([{";
    final String closing = ")]}";
    Stack<Character> openings = new LinkedStack<Character>();
    int i = 0;
    boolean foundError = false;
    while (!foundError && i < expression.length()) {</pre>
       char c = expression.charAt(i);
       if(opening.indexOf(c) != -1) { openings.push(c); }
       else if (closing.indexOf(c) != -1) {
         if(openings.isEmpty()) { foundError = true; }
         else {
           if (opening.indexOf(openings.top()) == closing.indexOf(c)) { openings.pop(); }
           else { foundError = true; } } }
       i ++: }
    return !foundError && openings.isEmpty(); }

    Testing the algorithm:

                   ATest
                  public void testMatchingDelimiters() {
```



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[e.g., 523+\*+]

[e.g., 53+6]

Problem: Given a postfix expression, calculate its value.

Infix Notation	Postfix Notation
Operator <i>in-between</i> Operands	Operator <i>follows</i> Operands
Parentheses force precedence	Order of evaluation embedded
3	3
3 + 4	3 4 +
3 + 4 + 5	3 4 + 5 +
3 + (4 + 5)	3 4 5 + +
3 - 4 * 5	345*-
(3 - 4) * 5	34-5*

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Stack Application: Postfix Notations (2)

#### **Sketch of Solution**

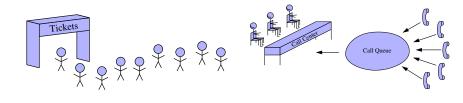
- When input is an *operand* (i.e., a number), *push* it to the <u>stack</u>.
- When input is an *operator*, obtain its two *operands* by *popping* off the <u>stack</u> <u>twice</u>, evaluate, then *push* the result back to <u>stack</u>.
- When finishing reading the input, there should be **only one** number left in the <u>stack</u>.
- Error if:
  - Not enough items left in the stack for the operator
  - When finished, two or more numbers left in stack

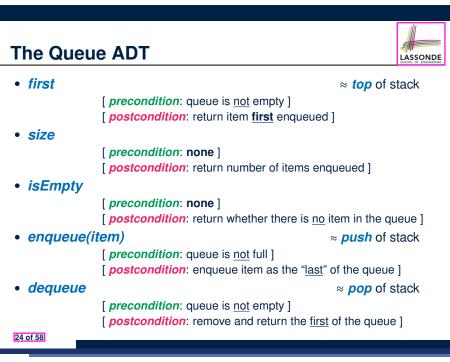


- A *queue* is a collection of objects.
- Objects in a *queue* are inserted and removed according to the *first-in, first-out (FIFO)* principle.

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- Each new element joins at the *back/end* of the queue.
- Cannot access arbitrary elements of a queue
- Can only access or remove the least-recently inserted (or longest-waiting) element



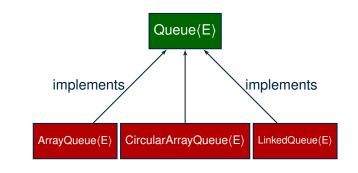


#### **Queue: Illustration**

Operation	Return Value	Queue Contents
_	—	Ø
isEmpty	true	Ø
enqueue(5)	_	(5)
enqueue(3)	_	(5, 3)
enqueue(1)	_	(5, 3, 1)
size	3	(5, 3, 1)
dequeue	5	(3, 1)
dequeue	3	1
dequeue	1	Ø

#### **Generic Queue: Architecture**





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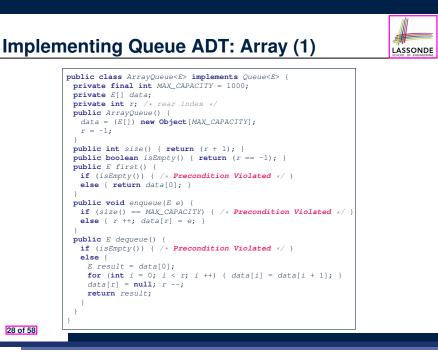
Generic Queue: Interface



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public interface Queue< E > {
 public int size();
 public boolean isEmpty();
 public E first();
 public void enqueue(E e);
 public E dequeue();
}

The *Queue* ADT, declared as an *interface*, allows *alternative implementations* to conform to its method headers.



#### Implementing Queue ADT: Array (2)



Running Times of Array-Based Queue Operations?

ArrayQueue Method	Running Time
size	O(1)
isEmpty	O(1)
first	O(1)
enqueue	O(1)
dequeue	<i>O</i> ( <i>n</i> )

- <u>Exercise</u> This version of implementation treats the *beginning* of array as the *first* of queue. Would the RTs of operations <u>change</u> if we treated the *end* of array as the *first* of queue?
- Q. What if the preset capacity turns out to be insufficient?
  - A. IllegalArgumentException occurs and it takes O(1) time to respond.
- At the end, we will explore the alternative of a *dynamic array*.

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- If the *front of list* is treated as the *first of queue*, then:
  - All queue operations remain *O*(1) [ :: removeFirst takes *O*(1) ]
- If the end of list is treated as the first of queue, then:
  - The *dequeue* operation takes *O(n)* [ ·: removeLast takes *O(n)* ]
- But in both cases, given that a linked, *dynamic* structure is used, *no resizing* is necessary!

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Implementing Queue: Singly-Linked List (1)

public class LinkedQueue<E> implements Queue<E> {
 private SinglyLinkedList<E> list;
 ...

#### **Question:**

Oursey Mathead	Singly-Linked	d List Method
Queue Method	Strategy 1	Strategy 2
size	list.size	
isEmpty	list.isEmpty	
first	list.first	list.last
enqueue	list.addLast	list.addFirst
dequeue	list.removeFirst	list.removeLast

Which *implementation strategy* should be chosen?

## **Generic Queue: Testing Implementations**

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#### @Test

public void testPolymorphicQueues() {
 Queue<String> q = new ArrayQueue<>)();
 q.enqueue("Alan"); /\* dynamic binding \*/
 q.enqueue("Mark"); /\* dynamic binding \*/
 q.enqueue("Tom"); /\* dynamic binding \*/
 assertTrue(q.size() == 3 && !q.isEmpty());
 assertEquals("Alan", q.first());

 q = new LinkedQueue<>();
 q.enqueue("Mark"); /\* dynamic binding \*/
 q.enqueue("Mark"); /\* dynamic binding \*/
 q.enqueue("Mark"); /\* dynamic binding \*/
 q.enqueue("Alan"); /\* dynamic binding \*/
 q.enqueue("Mark"); /\* dynamic binding \*/
 q.enqueue("Mark"); /\* dynamic binding \*/
 q.enqueue("Tom"); /\* dynamic b

## **Polymorphism & Dynamic Binding**



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#### Queue<**String**> myQueue;

- myQueue = new CircularArrayQueue<String>();
- 3 myQueue.enqueue("Alan");
  4 myQueue = new LinkedQueue<St;</pre>
- myQueue = new LinkedQueue<String>();
- myQueue.enqueue("Alan");
  - Polymorphism

An object may change its *"shape"* (i.e., *dynamic type*) at runtime.

Which lines? 2, 4

Dynamic Binding

Effect of a method call depends on the *"current shape"* of the target object.

Which lines? 3, 5

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2

5



. . .



#### • Maximum size: N-1 [N = data.length]

- Empty Queue: when *r* = *f*
- f, r
   Full Queue: when ((r + 1) % N) = f

• When *r* > *f*:

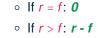
• When *r* < *f*:

f r f

. . .

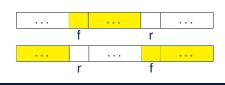
f, r

• Size of Queue:



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• If *r* < *f*: *r* + (*N* - *f*)



## Exercise:

## Implementing a Queue using Two Stacks

```
public class StackQueue<E> implements Queue<E> {
    private Stack<E> inStack;
    private Stack<E> outStack;
    ...
    ...
}
```

- For *size*, add up sizes of inStack and outStack.
- For *isEmpty*, are inStack and outStack both empty?
- For enqueue, push to inStack.
- For dequeue :
  - **pop from** outStack

If outStack is empty, we need to first *pop* <u>all</u> items from inStack and *push* them to outStack.

Exercise: Why does this work? [*implement* and *test*] Exercise: Running Time? [see analysis on *dynamic arrays*] 34 of 58 Implementing Queue ADT: Circular Array (2)

Running Times of *CircularArray*-Based *Queue* Operations?

CircularArrayQueue Method	Running Time
size	O(1)
isEmpty	O(1)
first	O(1)
enqueue	O(1)
dequeue	<i>O</i> (1)

**Exercise**: Create a Java class CircularArrayQueue that implements the Queue interface using a *circular array*.

## **Limitations of Queue**

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- Say we use a *queue* to implement a *waiting list*.
  - What if we dequeue the front customer, but find that we need to *put them back to the front* (e.g., seat is still not available, the table assigned is not satisfactory, *etc.*)?
  - What if the customer at the end of the queue decides not to wait and leave, how do we *remove them from the end of the queue*?
- Solution: A new ADT extending the Queue by supporting:
  - insertion to the front
  - *deletion* from the *end*

#### **Optional Materials**



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## These topics are useful for your knowledge about ADTs, stacks, and Queues.

You are **<u>encouraged</u>** to follow through these online lectures:

https://www.eecs.yorku.ca/~jackie/teaching/ lectures/index.html#EECS2011\_W22

- Design by Contract and Modularity
  - Week 5: Lecture 3, Parts A2 A3
- Dynamic Arrays and Amortized Analysis
  - Week 6: Lecture 3, Parts E1 E5

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The Double-Ended Queue ADT

•	<u>Double-Ended Queue</u>	(or	Deque	) is a <u>queue-like</u> data		
	structure that supports <i>insertion</i> and <i>deletion</i> at both the					
	front and the end of the queue.					

<pre>public interface Deque<e> {</e></pre>
/* Queue operations */
<pre>public int size();</pre>
<pre>public boolean isEmpty();</pre>
<pre>public E first();</pre>
<pre>public void addLast(E e); /* enqueue */</pre>
<pre>public E removeFirst(); /* dequeue */</pre>
<pre>/* Extended operations */</pre>
<pre>public void addFirst(E e);</pre>
<pre>public E removeLast();</pre>
}

- **<u>Exercise</u>**: Implement *Deque* using a *circular array*.
- **<u>Exercise</u>**: Implement *Deque* using a *SLL* and/or *DLL*.

#### Terminology: Contract, Client, Supplier

- A *supplier* implements/provides a service (e.g., microwave).
- A *client* uses a service provided by some supplier.
  - The client is required to follow certain instructions to obtain the service (e.g., supplier **assumes** that client powers on, closes door, and heats something that is not explosive).
  - If instructions are followed, the client would **expect** that the service does <u>what</u> is guaranteed (e.g., a lunch box is heated).
  - $\circ~$  The client does not care  $\underline{how}$  the supplier implements it.
- What are the *benefits* and *obligations* of the two parties?

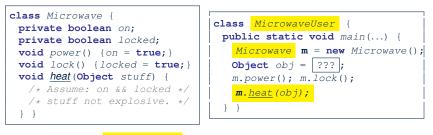
	benefits	obligations
CLIENT	obtain a service	follow instructions
SUPPLIER	assume instructions followed	provide a service

- There is a *contract* between two parties, <u>violated</u> if:
  - The instructions are not followed. [Client's fault]
- Instructions followed, but service not satisfactory. [Supplier's fault]

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## Client, Supplier, Contract in OOP (1)



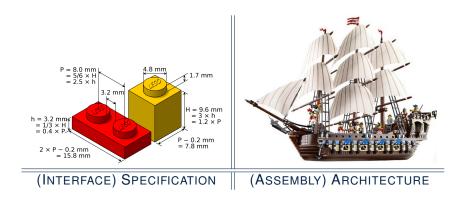


Method call *m.<u>heat(obj)</u> indicates a client-supplier relation.* 

- Client: resident class of the method call [MicrowaveUser]
- $\circ~$  Supplier: type of context object (or call target) m~ [ <code>Microwave</code> ]

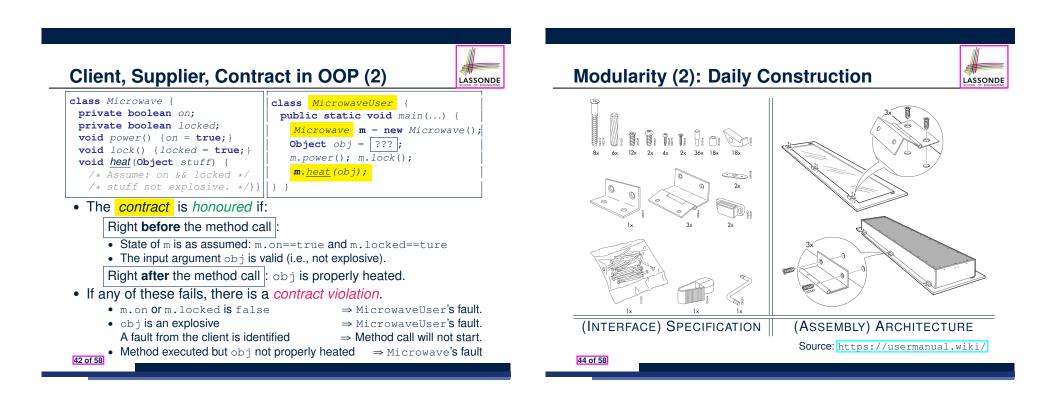
## Modularity (1): Childhood Activity





Sources: https://commons.wikimedia.org and https://www.wish.com

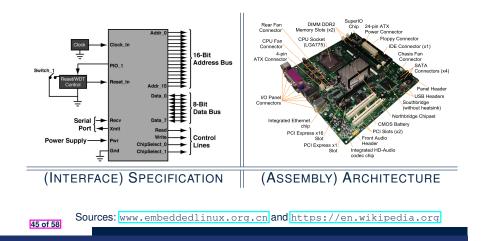
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## Modularity (3): Computer Architecture

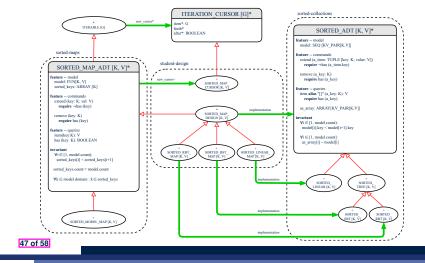


Motherboards are built from functioning units (e.g., CPUs).



#### Modularity (5): Software Design

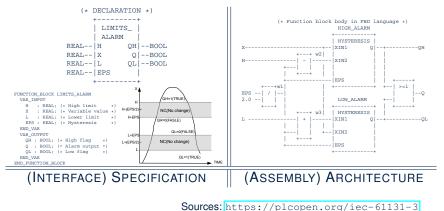
Software systems are composed of *well-specified classes*.



## Modularity (4): System Development



Safety-critical systems (e.g., *nuclear shutdown systems*) are built from *function blocks*.



#### **Design Principle: Modularity**



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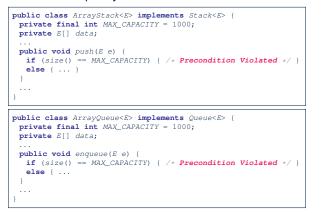
- *Modularity* refers to a sound quality of your design:
  - 1. <u>Divide</u> a given complex *problem* into inter-related *sub-problems* via a logical/justifiable <u>functional decomposition</u>.
    - e.g., In designing a game, solve sub-problems of: 1) rules of the game; 2) actor characterizations; and 3) presentation.
  - 2. <u>Specify</u> each *sub-solution* as a *module* with a clear <u>interface</u>: inputs, outputs, and <u>input-output relations</u>.
    - The UNIX principle: Each command does one thing and does it well.
    - In objected-oriented design (OOD), each <u>class</u> serves as a module.
  - 3. <u>Conquer</u> original *problem* by assembling *sub-solutions*.
    - In OOD, classes are assembled via <u>client-supplier</u> relations (aggregations or compositions) or <u>inheritance</u> relations.
- A *modular design* satisfies the criterion of modularity and is:
  - Maintainable: fix issues by changing the relevant modules only.
  - *Extensible*: introduce new functionalities by adding new modules.
  - *Reusable*: a module may be used in <u>different</u> compositions
- Opposite of modularity: A superman module doing everything.

## Array Implementations: Stack and Queue



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When implementing *stack* and *queue* via *arrays*, we imposed a maximum capacity:



• This made the *push* and *enqueue* operations both cost *O(1)*.

## **Dynamic Array: Doubling**

Implement *stack* using a *dynamic array* resizing itself by <u>doubling</u>:

1	<pre>public class ArrayStack<e> implements Stack<e> {</e></e></pre>			
2	private int I;			
3	private int capacity;			
4	<pre>private E[] data;</pre>			
5	<pre>public ArrayStack() {</pre>			
6	<pre>I = 1000; /* arbitrary initial size */</pre>			
7	capacity = I;			
8	<pre>data = (E[]) new Object[capacity];</pre>			
9	t = -1;			
10	}			
11	<pre>public void push(E e) {</pre>			
12	<pre>if (size() == capacity) {</pre>			
13	/* resizing by doubling */			
14	<pre>E[] temp = (E[]) new Object[capacity * 2];</pre>			
15	<pre>for(int i = 0; i &lt; capacity; i ++) {</pre>			
16	<pre>temp[i] = data[i];</pre>			
17	}			
18	data = temp;			
19	capacity = capacity * 2			
20	}			
21	t++;			
22	data[t] = e;			
23	}			
24	}			
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- This alternative strategy resizes the array, whenever needed, by *doubling* its current size.
- L15 L17 make *push* cost *O(n)*, in the *worst case*.
- However, given that *resizing* only happens <u>rarely</u>, how about the <u>average</u> running time?
- We will refer L12 L20 as the resizing part and L21 – L22 as the update part.

#### **Dynamic Array: Constant Increments**

Implement stack using a dynamic array resizing itself by a constant increment:



- This alternative strategy resizes the array, whenever needed, by a constant amount.
- L17 L19 make *push* cost *O(n)*, in the *worst case*.
- However, given that *resizing* only happens <u>rarely</u>, how about the <u>average</u> running time?
- We will refer L14 L22 as the resizing part and L23 – L24 as the update part.

## Avg. RT: Const. Increment vs. Doubling



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 <u>Without loss of generality</u>, assume: There are *n push* operations, and the <u>last push</u> triggers the <u>last</u> *resizing* routine.

	Constant Increments	Doubling
RT of exec. update part for <i>n</i> pushes	O(n)	
RT of executing 1st resizing		
RT of executing 2nd resizing	I + C	2 · 1
RT of executing 3rd resizing	$I + 2 \cdot C$	4 · /
RT of executing 4th resizing	$I + 3 \cdot C$	8 · /
RT of executing k <sup>th</sup> resizing	$I + (\mathbf{k} - 1) \cdot C$	2 <sup>k−1</sup> · I
RT of executing last resizing	n	
# of <u>resizing</u> needed (solve k for $RT = n$ )	<i>O</i> ( <i>n</i> )	$O(log_2n)$
Total RT for <i>n</i> pushes	$O(n^2)$	<i>O</i> ( <i>n</i> )
Amortized/Average RT over <i>n</i> pushes	<i>O</i> ( <i>n</i> )	O(1)

Over *n* push operations, the *amortized / average* running time of the *doubling* strategy is more efficient.

### Beyond this lecture ....



#### · Attempt the exercises throughout the lecture.

Implement the *Postfix Calculator* using a <u>stack</u>.

#### Index (2)

Implementing Stack: Array (2)

Implementing Stack: Singly-Linked List (1)

Implementing Stack: Singly-Linked List (2)

Generic Stack: Testing Implementations

- Polymorphism & Dynamic Binding
- Stack Application: Reversing an Array
- Stack Application: Matching Delimiters (1)

Stack Application: Matching Delimiters (2)

- Stack Application: Postfix Notations (1)
- Stack Application: Postfix Notations (2)

What is a Queue?

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## Index (1)

Learning Outcomes of this Lecture

Abstract Data Types (ADTs)

Java API Approximates ADTs (1)

Java API Approximates ADTs (2)

Building ADTs for Reusability

What is a Stack?

The Stack ADT

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Stack: Illustration

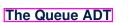
Generic Stack: Interface

Generic Stack: Architecture

Implementing Stack: Array (1)

Index (3)

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Queue: Illustration

- Generic Queue: Interface
- Generic Queue: Architecture
- Implementing Queue ADT: Array (1)
- Implementing Queue ADT: Array (2)
- Implementing Queue: Singly-Linked List (1)
- Implementing Queue: Singly-Linked List (2)

Generic Queue: Testing Implementations

Polymorphism & Dynamic Binding

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## Index (4)

#### Exercise:

Implementing a Queue using Two Stacks

Implementing Queue ADT: Circular Array (1)

Implementing Queue ADT: Circular Array (2)

Limitations of Queue

The Double-Ended Queue ADT

**Optional Materials** 

Terminology: Contract, Client, Supplier

Client, Supplier, Contract in OOP (1)

Client, Supplier, Contract in OOP (2)

Modularity (1): Childhood Activity

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Index (5)

Modularity (2): Daily Construction

Modularity (3): Computer Architecture

Modularity (4): System Development

Modularity (5): Software Design

Design Principle: Modularity

Array Implementations: Stack and Queue

Dynamic Array: Constant Increments

Dynamic Array: Doubling

Avg. RT: Const. Increment vs. Doubling

Beyond this lecture ...