EECS2101-XZ Winter 2025
Fundamentals of Data Structures
Example Exam Questions
Final Exam
April 20, 2025
Time Limit: 180 Minutes

Name (Last, First):

Student Number:	
PPY Login	
Signature	

• NO QUESTIONS DURING THE EXAM.

- This is a 180 minute test.
- This is a closed book test:
 - A one-sided data sheet is permitted.
 - **No** calculator is permitted.
- Spell <u>clearly</u> your name, student number, and other required information.
- For the written questions:
 - Write your answers with either a pen or a pencil.
 Writing in a colour <u>other than black and blue</u> (e.g., red, green, purple) will receive an <u>immediate zero</u>.
 - Writing in <u>cursive</u> will receive an Do not write in this table which <u>immediate zero</u>.
 - Write legibly: unrecognized answers will receive <u>no</u> credits.
 - Express your ideas concisely and precisely.
 - Organize your answers.
- Some tips for tackling the exam questions:
 - Spend a few minutes skimming over the entire question booklet to have an idea about what topics are covered.
 - Build the confidence and momentum by first answering questions that you feel more comfortable about.
 - Do not get stuck in a single question for too long: set yourself some time limit, document where you get stuck, and come back later.
 - It is natural to feel nervous and frustrated when you do not have the immediate clues about the more challenging questions. Just <u>expect</u> and <u>embrace</u> those feelings.
 - Stay calm and identify/highlight key terms in questions.

Problem	Points	Score
1	20	
2	30	
3	50	
Total:	100	

1. Consider the following fragment of Java code:

```
1
  boolean containsDuplicate (int[] a, int n) {
2
    for (int i = 0; i < n;) {
3
      for (int j = 0; j < n;) {
        if (i != j && a[i] == a[j]) {
4
5
         return true; }
6
        j ++; }
7
      i ++; }
8
    return false; }
```

Derive, in the worst case, the number of primitive operations executed to return the result.

Solution:

- The answer is: $9n^2 + 5n + 3$
- See the solution walkthrough here: https://www.youtube.com/watch?v=k-ijBQgmBtY& list=PL5dxAmCmjv_6EOKnlgJJ4OEKC7ZqJ0Hsv&index=4&t=796s
- Solution notes here: https://www.eecs.yorku.ca/~jackie/teaching/lectures/2022/ W/EECS2011/blackboards/Blackboard-EECS2011-W22-Q&A-20220120.pdf#page=3

of 20 marks]

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- 2. (a) Given a BST rooted at node n, describe how an entry (k, v) can be inserted.
 - **<u>Requirements</u>**. Do <u>not</u> write any Java code. Describe the steps precisely and concisely.

Solution:
- Let node \mathbf{p} be the return value from search(n, k).
- If p is an internal node
\Rightarrow Key k exists in the BST.
\Rightarrow Set p's value to v.
- If p is an external node
\Rightarrow Key k deos <u>not</u> exist in the BST.
\Rightarrow Set p's key and value to k and v.

of 20 marks]

(b) Explain why an *inorder* traversal of a binary search tree produces a sequence of entries whose keys are sorted in an *increasing* order.

Solution:

- A binary search tree must satisfy the search property: all nodes on the LST of the root have keys that are strictly less than that of the root; and all nodes on the RSH of the root have keys that are strictly less than that of the root.
- For each subtree, say rooted at r, in a binary search tree, an inorder traversal first visits r's LST, then r, and then r's RST.
- Consequently, the produced sequence of keys are sorted in an increasing order.

of 10 marks]

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- 3. (a) Consider the following classes of functions:
 - *O*(*n*)
 - O(log(n))
 - $O(n^2)$
 - O(1)
 - $O(2^n)$
 - $O(n^3)$
 - $O(n \cdot log(n))$

Say each of the above functions maps from input size n to the *approximated* algorithm running time. Sort, from left to right, the above classes of functions from the cheapest to the most expensive. **Caution:** You will lose **all** marks if the order is not completely correct.

Solution: $O(1) \quad O(log(n)) \quad O(n) \quad O(n \cdot log(n)) \quad O(n^2) \quad O(n^3) \quad O(2^n)$

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For Part (b) to Part (d), consider the following statements:

- (A) 3n + 7 is $O(n \cdot log(n))$
- (**B**) 3n + 7 is O(n)
- (C) 3n + 7 is O(1)
- (**D**) 3n + 7 is $O(2^n)$
- (E) 3n + 7 is O(log(n))
- (**F**) 3n + 7 is $O(n^2)$
- (b) Which of the above statement or statements are *correct*? Do not guess: you lose **all** marks if you make a mistake.

Solution: Statements A B D F

of 10 marks]

(c) Among the above statement or statements that are *correct*, which **one** is the most *accurate*?

Solution: Statement B

of 10 marks]

(d) Justify your answer to the previous question. That is, clearly explain why it is more *accurate* than all other *correct* statements.

Solution: The highest power of n in 3n + 7 is one. So Statement B is the most accurate by saying that 3n + 7 is O(n). The class O(n) is strictly contained by $O(n \cdot log(n))$, which is strictly contained by $O(n^2)$, which is strictly contained by $O(2^n)$.

of 10 marks]

(e) Prove that $f(n) = 4n^3 - 5n^2 + 59 + n^4 + 9n$ is $O(n^4)$.

Solution: Choose c = 78 and $n_0 = 1$.

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