Recursion



EECS2030 B & G: Advanced Object Oriented Programming Fall 2025

CHEN-WEI WANG

Learning Outcomes



This module is designed to help you learn about:

- 1. How to solve problems recursively
- 2. Example *recursions* on string and arrays
- 3. Some more advanced example (if time permitted)

Beyond this lecture ...



 Fantastic resources for sharpening your recursive skills for the exam:

```
http://codingbat.com/java/Recursion-1
http://codingbat.com/java/Recursion-2
```

• The *best* approach to learning about recursion is via a functional programming language:

Haskell Tutorial: https://www.haskell.org/tutorial/

3 of 37

Recursion: Principle



- *Recursion* is useful in expressing solutions to problems that can be *recursively* defined:
 - **Base Cases:** Small problem instances immediately solvable.
 - Recursive Cases:
 - Large problem instances not immediately solvable.
 - Solve by reusing *solution(s)* to *strictly smaller problem instances*.
- Similar idea learnt in high school: [mathematical induction]
- Recursion can be easily expressed programmatically in Java:

```
m(i) {
  if(i == ...) { /* base case: do something directly */ }
  else {
    m(j);/* recursive call with strictly smaller value */
  }
}
```

- In the body of a method *m*, there might be *a call or calls to m itself*.
- Each such self-call is said to be a recursive call.
- o Inside the execution of m(i), a recursive call m(j) must be that j < i.

LASSONDE SCHOOL OF ENGINEERING

Tracing Method Calls via a Stack

- When a method is called, it is activated (and becomes active) and pushed onto the stack.
- When the body of a method makes a (helper) method call, that (helper) method is activated (and becomes active) and pushed onto the stack.
 - ⇒ The stack contains activation records of all *active* methods.
 - of stack denotes the current point of execution.
 - Remaining parts of stack are (temporarily) suspended.
- When entire body of a method is executed, stack is *popped*.
 - ⇒ The current point of execution is returned to the new top of stack (which was suspended and just became active).
- Execution terminates when the stack becomes empty.

5 of 37

6 of 37



Recursion: Factorial (1)

• Recall the formal definition of calculating the *n* factorial:

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ n \cdot (n-1) \cdot (n-2) \cdot \dots \cdot 3 \cdot 2 \cdot 1 & \text{if } n \ge 1 \end{cases}$$

• How do you define the same problem *recursively*?

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ n \cdot (n-1)! & \text{if } n \ge 1 \end{cases}$$

• To solve n!, we combine n and the solution to (n - 1)!.

```
int factorial (int n) {
  int result;
  if(n == 0) { /* base case */ result = 1; }
  else { /* recursive case */
    result = n * factorial (n - 1);
  }
  return result;
}
```

Common Errors of Recursive Methods



Missing Base Case(s).

```
int factorial (int n) {
  return n * factorial (n - 1);
}
```

Base case(s) are meant as points of stopping growing the runtime stack.

• Recursive Calls on Non-Smaller Problem Instances.

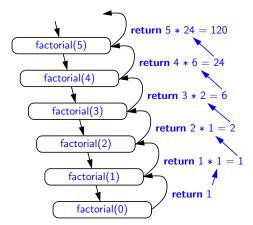
```
int factorial (int n) {
  if(n == 0) { /* base case */ return 1; }
  else { /* recursive case */ return n * factorial (n); }
}
```

Recursive calls on *strictly smaller* problem instances are meant for moving gradually towards the base case(s).

• In both cases, a StackOverflowException will be thrown.

Recursion: Factorial (2)





LASSONDE SCHOOL OF ENGINEERING

Recursion: Factorial (3)

- When running factorial(5), a recursive call factorial(4) is made.
 Call to factorial(5) suspended until factorial(4) returns a value.
- When running factorial(4), a recursive call factorial(3) is made.
 Call to factorial(4) suspended until factorial(3) returns a value.
- factorial(0) returns 1 back to suspended call factorial(1).
- factorial(1) receives 1 from factorial(0), multiplies 1 to it, and returns 1 back to the suspended call factorial(2).
- factorial(2) receives 1 from factorial(1), multiplies 2 to it, and returns 2 back to the suspended call factorial(3).
- factorial(3) receives 2 from factorial(1), multiplies 3 to it, and returns 6 back to the suspended call factorial(4).
- factorial(4) receives 6 from factorial(3), multiplies 4 to it, and returns 24 back to the suspended call factorial(5).
- factorial(5) receives 24 from factorial(4), multiplies 5 to it, and returns 120 as the result.

9 of 37



Recursion: Factorial (4)

- When the execution of a method (e.g., *factorial(5)*) leads to a nested method call (e.g., *factorial(4)*):
 - The execution of the current method (i.e., factorial(5)) is suspended, and a structure known as an activation record or activation frame is created to store information about the progress of that method (e.g., values of parameters and local variables).
 - The nested methods (e.g., factorial(4)) may call other nested methods (factorial(3)).
 - When all nested methods complete, the activation frame of the <u>latest</u> <u>suspended</u> method is re-activated, then continue its execution.
- What kind of data structure does this activation-suspension process correspond to? [LIFO Stack]

10 of 37

Recursion: Fibonacci Sequence (1)



• Can you identify the pattern of a Fibonacci sequence?

$$F = 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, \dots$$

• Here is the formal, *recursive* definition of calculating the n_{th} number in a Fibonacci sequence (denoted as F_n):

$$F_n = \begin{cases} 1 & \text{if } n = 1 \\ 1 & \text{if } n = 2 \\ F_{n-1} + F_{n-2} & \text{if } n > 2 \end{cases}$$

```
int fib (int n) {
   int result;
   if(n == 1) { /* base case */ result = 1; }
   else if(n == 2) { /* base case */ result = 1; }
   else { /* recursive case */
      result = fib (n - 1) + fib (n - 2);
   }
   return result;
}
```

Recursion: Fibonacci Sequence (2)



```
{ fib(5) = fib(4) + fib(3); push(fib(5)); suspended: (fib(5)); active: fib(4) }
      fib(4) + fib(3)
     \{ fib(4) = \underline{fib(3)} + fib(2); suspended: (fib(4), fib(5)); active: fib(3) \}
     (fib(3) + fib(2)) + fib(3)
     \{fib(3) = \underline{fib(2)} + fib(1); suspended: \{fib(3), fib(4), fib(5)\}; active: fib(2)\}
     ((fib(2) + fib(1)) + fib(2)) + fib(3)
     { fib(2) returns 1; suspended: (fib(3), fib(4), fib(5)); active: fib(1) }
     ((1 + fib(1)) + fib(2)) + fib(3)
     { fib(1) returns 1; suspended: (fib(3), fib(4), fib(5)); active: fib(3) }
     ((1+1)+fib(2))+fib(3)
     { fib(3) returns 1 + 1; pop(); suspended: \{fib(4), fib(5)\}; active: fib(2) }
     (2 + fib(2)) + fib(3)
     { fib(2) returns 1; suspended: (fib(4), fib(5)); active: fib(4) }
     (2+1) + fib(3)
     { fib(4) returns 2 + 1; pop(); suspended: (fib(5)); active: fib(3) }
     3 + fib(3)
     \{ fib(3) = fib(2) + fib(1); suspended: (fib(3), fib(5)); active: fib(2) \}
     3 + (fib(2) + fib(1))
     { fib(2) returns 1; suspended: (fib(3), fib(5)); active: fib(1) }
     3 + (1 + fib(1))
     { fib(1) returns 1; suspended: (fib(3), fib(5)); active: fib(3) }
     3 + (1 + 1)
     { fib(3) returns 1 + 1; pop() ; suspended: fib(5); active: fib(5) }
     3 + 2
12 of 37 fib(5) returns 3 + 2; suspended: () }
```

Java Library: String



```
public class StringTester {
 public static void main(String[] args) {
  String s = "abcd";
  System.out.println(s.isEmpty()); /* false */
  /* Characters in index range [0, 0) */
  String t0 = s.substring(0, 0);
  System.out.println(t0); /* "" */
   /* Characters in index range [0, 4) */
  String t1 = s.substring(0, 4);
  System.out.println(t1); /* "abcd" */
  /* Characters in index range [1, 3) */
  String t2 = s.substring(1, 3);
  System.out.println(t2); /* "bc" */
  String t3 = s.substring(0, 2) + s.substring(2, 4);
   System.out.println(s.equals(t3)); /* true */
  for(int i = 0; i < s.length(); i ++) {</pre>
    System.out.print(s.charAt(i));
   System.out.println();
13 of 37
```

Recursion: Palindrome (1)



Problem: A palindrome is a word that reads the same forwards and backwards. Write a method that takes a string and determines whether or not it is a palindrome.

```
System.out.println(isPalindrome("")); true
System.out.println(isPalindrome("a")); true
System.out.println(isPalindrome("madam")); true
System.out.println(isPalindrome("racecar")); true
System.out.println(isPalindrome("man")); false
```

Base Case 1: Empty string → Return *true* immediately.

Base Case 2: String of length 1 → Return *true* immediately.

Recursive Case: String of length $\geq 2 \longrightarrow$

- o 1st and last characters match, and
- the rest (i.e., middle) of the string is a palindrome.

14 of 37

Recursion: Palindrome (2)



```
boolean isPalindrome (String word) {
  if(word.length() == 0 || word.length() == 1) {
    /* base case */
    return true;
  }
  else {
    /* recursive case */
    char firstChar = word.charAt(0);
    char lastChar = word.charAt(word.length() - 1);
    String middle = word.substring(1, word.length() - 1);
    return
        firstChar == lastChar
        /* See the API of java.lang.String.substring. */
        && isPalindrome (middle);
    }
}
```

15 of 37

Recursion: Reverse of String (1)



Problem: The reverse of a string is written backwards. Write a method that takes a string and returns its reverse.

```
System.out.println(reverseOf("")); /* "" */
System.out.println(reverseOf("a")); "a"
System.out.println(reverseOf("ab")); "ba"
System.out.println(reverseOf("abc")); "cba"
System.out.println(reverseOf("abcd")); "dcba"
```

Base Case 1: Empty string → Return *empty string*.

Base Case 2: String of length $1 \longrightarrow \text{Return } \text{that string.}$

Recursive Case: String of length $\geq 2 \longrightarrow$

- 1) Head of string (i.e., first character)
- 2) Reverse of the tail of string (i.e., all but the first character)

Return the concatenation of 2) and 1).

Recursion: Reverse of a String (2)



```
String reverseOf (String s) {
  if(s.isEmpty()) { /* base case 1 */
    return "";
  }
  else if(s.length() == 1) { /* base case 2 */
    return s;
  }
  else { /* recursive case */
    String tail = s.substring(1, s.length());
    String reverseOfTail = reverseOf (tail);
    char head = s.charAt(0);
    return reverseOfTail + head;
  }
}
```

17 of 37

Recursion: Number of Occurrences (1)



Problem: Write a method that takes a string s and a character c, then count the number of occurrences of c in s.

```
System.out.println(occurrencesOf("", 'a')); /* 0 */
System.out.println(occurrencesOf("a", 'a')); /* 1 */
System.out.println(occurrencesOf("b", 'a')); /* 0 */
System.out.println(occurrencesOf("baaba", 'a')); /* 3 */
System.out.println(occurrencesOf("baaba", 'b')); /* 2 */
System.out.println(occurrencesOf("baaba", 'c')); /* 0 */
```

Base Case: Empty string \longrightarrow Return 0.

Recursive Case: String of length $\geq 1 \longrightarrow$

- 1) Head of s (i.e., first character)
- 2) Number of occurrences of ${\tt c}$ in the \underline{tail} of $\underline{\tt s}$ (i.e., all but the first character)

If head is equal to c, return 1 + 2).

If head is not equal to c, return 0 + 2).

18 of 37

Recursion: Number of Occurrences (2)



```
int occurrencesOf (String s, char c) {
   if(s.isEmpty()) {
      /* Base Case */
      return 0;
   }
   else {
      /* Recursive Case */
      char head = s.charAt(0);
      String tail = s.substring(1, s.length());
      if(head == c) {
        return 1 + occurrencesOf (tail, c);
    }
    else {
        return 0 + occurrencesOf (tail, c);
    }
}
```

19 of 37

Making Recursive Calls on an Array



- Recursive calls denote solutions to *smaller* sub-problems.
- Naively, explicitly create a new, smaller array:

• For *efficiency*, we pass the *reference* of the same array and specify the *range of indices* to be considered:

20 of 37 • m(a, a.length-1, a.length-1) [Last r.c. on array of size 1]



Recursion: All Positive (1)

Problem: Determine if an array of integers are all positive.

```
System.out.println(allPositive({})); /* true */
System.out.println(allPositive({1, 2, 3, 4, 5})); /* true */
System.out.println(allPositive({1, 2, -3, 4, 5})); /* false */
```

Base Case: Empty array → Return *true* immediately.

The base case is true: we can not find a counter-example

(i.e., a number *not* positive) from an empty array.

Recursive Case: Non-Empty array →

- o 1st element positive, and
- the rest of the array is all positive.

Exercise: Write a method boolean somePostive(int[]

a) which *recursively* returns *true* if there is some positive number in a, and *false* if there are no positive numbers in a.

Hint: What to return in the base case of an empty array? [false]

... No witness (i.e., a positive number) from an empty array

21 of 37



Recursion: All Positive (2)

```
boolean allPositive(int[] a) {
  return allPositiveHelper (a, 0, a.length - 1);
}

boolean allPositiveHelper (int[] a, int from, int to) {
  if (from > to) { /* base case 1: empty range */
    return true;
  }
  else if(from == to) { /* base case 2: range of one element */
    return a[from] > 0;
  }
  else { /* recursive case */
    return a[from] > 0 && allPositiveHelper (a, from + 1, to);
  }
}
```



Recursion: Is an Array Sorted? (1)



Problem: Determine if an array of integers are sorted in a non-descending order.

```
System.out.println(isSorted({})); true
System.out.println(isSorted({1, 2, 2, 3, 4})); true
System.out.println(isSorted({1, 2, 2, 1, 3})); false
```

Base Case: Empty array \longrightarrow Return *true* immediately.

The base case is *true* : we can *not* find a counter-example (i.e., a pair of adjacent numbers that are *not* sorted in a non-descending order) from an empty array.

Recursive Case: Non-Empty array →

- 1st and 2nd elements are sorted in a non-descending order, and
- the rest of the array, starting from the 2nd element,

are sorted in a non-descending order.

23 of 37

Recursion: Is an Array Sorted? (2)

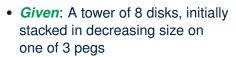


```
boolean isSorted(int[] a) {
  return isSortedHelper (a, 0, a.length - 1);
}

boolean isSortedHelper (int[] a, int from, int to) {
  if (from > to) { /* base case 1: empty range */
    return true;
  }
  else if(from == to) { /* base case 2: range of one element */
    return true;
  }
  else {
    return a[from] <= a[from + 1]
    && isSortedHelper (a, from + 1, to);
  }
}</pre>
```

Tower of Hanoi: Specification





• Rules:

- Move only one disk at a time.
- <u>Never</u> move a larger disk onto a smaller one.
- Problem: Transfer the entire tower to one of the other pegs.





The general, a recursive solution requires 3 steps:

- 1. Transfer the **n** 1 smallest disks to a **second** peg.
- 2. Move the largest peg to the third peg (free of disks).
- 3. Transfer the n 1 smallest disks back onto the largest disk.

25 of 37

Tower of Hanoi: Lengend





Brahmins at a temple in Benares, India have been carrying out movement of "Sacred Tower of Brahma", consisting of **sixty-four** golden disks, according to the same rules as in the Tower of Hanoi game, and that the completion of the tower would lead to the end of the world.

27 of 37

Tower of Hanoi in Java (1)



```
void towerOfHanoi(String[] disks) {
   tohHelper (disks, 0, disks.length - 1, 1, 3);
}
void tohHelper(String[] disks, int from, int to, int ori, int des) {
   if(from > to) {
      else if(from == to) {
        print("move " + disks[to] + " from " + ori + " to " + des);
   }
   else {
      int intermediate = 6 - ori - des;
      tohHelper (disks, from, to - 1, ori, intermediate);
      print("move " + disks[to] + " from " + ori + " to " + des);
      tohHelper (disks, from, to - 1, intermediate, des);
   }
}
```

- tohHelper(disks, from, to, ori, des) moves disks {disks[from], disks[from+1],..., disks[to]} from peg ori to peg des.
- Peg id's are 1, 2, and $3 \Rightarrow$ The intermediate one is 6 ori des.

Tower of Hanoi in Java (2)



Say ds (disks) is $\{A, B, C\}$, where A < B < C.

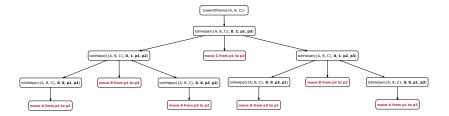
$$tohH(ds, \ 0, 2 \ , p1, p3) = \begin{cases} tohH(ds, 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 1 \ , p1, p2) = \begin{cases} AB \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p2) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p2) = \begin{cases} Move \ A: \ p3 \ to \ p2 \end{cases} \\ \hline tohH(ds, \ 0, 0, p2, p1) = \begin{cases} Move \ A: \ p3 \ to \ p2 \end{cases} \\ \hline tohH(ds, \ 0, 1 \ , p2, p3) = \begin{cases} Move \ B: \ p2 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p1 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p2 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p2 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p2 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p1, p3) = \begin{cases} Move \ A: \ p2 \ to \ p3 \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) = \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) = \begin{cases} Move \ A: \ p3 \ tohH(ds, \ 0, 0, p3, p3) = \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) = \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) = \begin{cases} Move \ A: \ p3 \ tohH(ds, \ 0, 0, p3, p3) = \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) = \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) = \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) = \end{cases} \\ \hline tohH(ds, \ 0, 0, p3, p3) =$$

29 of 37

30 of 37

Tower of Hanoi in Java (3)





Running Time: Tower of Hanoi (1)



- Generalize the problem by considering n disks.
- Let *T(n)* denote the number of moves required to to transfer n
 disks from one to another under the rules.
- Recall the general solution pattern:
 - 1. Transfer the **n** 1 smallest disks to a second peg.
 - 2. Move the largest peg to the *third* peg (free of disks).
 - **3.** Transfer the **n 1 smallest** disks back onto the **largest** disk.
- We end up with the following recurrence relation that allows us to compute *T(n)* for any **n** we like:

$$\begin{cases} T(1) = 1 \\ T(n) = 2 \cdot T(n-1) + 1 \text{ where } n > 0 \end{cases}$$

• To solve this recurrence relation, we study the pattern of *T(n)* and observe how it reaches the *base case(s)*.

31 of 37

Running Time: Tower of Hanoi (2)



$$T(n) = \underbrace{2 \times T(n-1) + 1}_{1 \text{ term}}$$

$$= \underbrace{2 \times (2 \times T(n-2) + 1) + 1}_{2 \text{ terms}}$$

$$= \underbrace{2 \times (2 \times (2 \times T(n-3) + 1) + 1) + 1}_{3 \text{ terms}}$$

$$= \dots$$

$$= \underbrace{2 \times (2 \times (2 \times T(n-3) + 1) + 1) + 1}_{n-1 \text{ terms}}$$

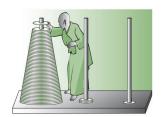
$$= \underbrace{2 \times (2 \times (2 \times (\dots \times (2 \times T(n-1))) + 1) + 1) + 1}_{n-1 \text{ terms}}$$

$$= \underbrace{2^{n-1} + (n-1)}_{1 \text{ terms}}$$

T(n) is $O(2^n)$

Tower of Hanoi: Lengend





Brahmins at a temple in Benares, India have been carrying out movement of "Sacred Tower of Brahma", consisting of **sixty-four** golden disks, according to the same rules as in the Tower of Hanoi game, and that the completion of the tower would lead to the end of the world.

Say one disk can be moved in one second.

Q. How long does it take to finish moving 64 disks (n = 64)?

A. 2^{64} seconds ≈ 585 billion years (>> 5 billion centries)!

33 of 37

Beyond this lecture ...



- Recursions on Arrays: Lab Exercise from EECS2030-F19
- · Notes on Recursion:

http://www.eecs.yorku.ca/~jackie/teaching/ lectures/2025/F/EECS2030/notes/EECS2030_F25_ Notes Recursion.pdf

• API for String:

https://docs.oracle.com/javase/8/docs/api/
java/lang/String.html

 Fantastic resources for sharpening your recursive skills for the exam:

http://codingbat.com/java/Recursion-1
http://codingbat.com/java/Recursion-2

 The <u>best</u> approach to learning about recursion is via a functional programming language:

Haskell Tutorial: https://www.haskell.org/tutorial/

Index (1)



Learning Outcomes

Beyond this lecture ...

Recursion: Principle

Tracing Method Calls via a Stack

Recursion: Factorial (1)

Common Errors of Recursive Methods

Recursion: Factorial (2)
Recursion: Factorial (3)
Recursion: Factorial (4)

Recursion: Fibonacci Sequence (1)
Recursion: Fibonacci Sequence (2)

35 of 37

Index (2)



Java Library: String

Recursion: Palindrome (1)

Recursion: Palindrome (2)

Recursion: Reverse of a String (1)

Recursion: Reverse of a String (2)

Recursion: Number of Occurrences (1)

Recursion: Number of Occurrences (2)

Making Recursive Calls on an Array

Recursion: All Positive (1)

Recursion: All Positive (2)

Recursion: Is an Array Sorted? (1)

Index (3)



Recursion: Is an Array Sorted? (2)

Tower of Hanoi: Specification

Tower of Hanoi: Legend

Tower of Hanoi: A Recursive Solution

Tower of Hanoi in Java (1)

Tower of Hanoi in Java (2)

Tower of Hanoi in Java (3)

Running Time: Tower of Hanoi (1)

Running Time: Tower of Hanoi (2)

Tower of Hanoi: Legend

Beyond this lecture ...