

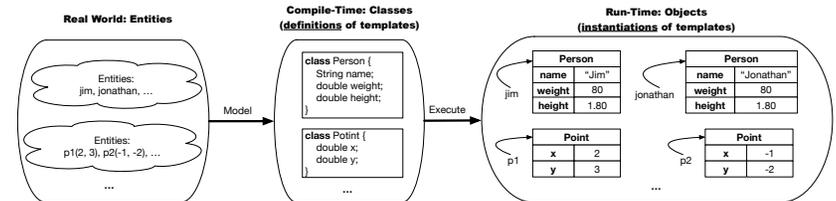
Classes and Objects



EECS2030 B: Advanced
Object Oriented Programming
Fall 2018

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Object Orientation: Observe, Model, and Execute



- o Study this tutorial video that walks you through the idea of **object orientation**.
- o We **observe** how real-world *entities* behave.
- o We **model** the common *attributes* and *behaviour* of a set of entities in a single *class*.
- o We **execute** the program by creating *instances* of classes, which interact in a way analogous to that of real-world *entities*.

3 of 68

Separation of Concerns: App/Tester vs. Model



- o In EECS1022:
 - o **Model Component**: One or More Java Classes
e.g., `Person` vs. `SMS`, `Student`, `CourseRecord`
 - o Another Java class that "manipulates" the model class (by creating instances and calling methods):
 - o **Controller** (e.g., `BMIActivity`, `BankActivity`). Effects? Visualized (via a GUI) at connected tablet
 - o **Tester** with `main` (e.g., `PersonTester`, `BankTester`). Effects? Seen (as textual outputs) at console
- o In Java:
 - o We may define more than one *classes*.
 - o Each class may contain more than one *methods*.
 - o **object-oriented programming** in Java:
 - o Use **classes** to define templates
 - o Use **objects** to instantiate classes
 - o At *runtime*, *create* objects and *call* methods on objects, to *simulate interactions* between real-life entities.

2 of 68

Object-Oriented Programming (OOP)



- o In real life, lots of **entities** exist and interact with each other.
e.g., *People* gain/lose weight, marry/divorce, or get older.
e.g., *Cars* move from one point to another.
e.g., *Clients* initiate transactions with banks.
- o Entities:
 - o Possess *attributes*;
 - o Exhibit *behaviour*; and
 - o Interact with each other.
- o Goals: Solve problems *programmatically* by
 - o *Classifying* entities of interest
Entities in the same class share *common* attributes and behaviour.
 - o *Manipulating* data that represent these entities
Each entity is represented by *specific* values.

4 of 68

OO Thinking: Templates vs. Instances (1.1)



A person is a being, such as a human, that has certain attributes and behaviour constituting personhood: a person ages and grows on their heights and weights.

- A template called `Person` defines the common
 - **attributes** (e.g., age, weight, height) [≈ nouns]
 - **behaviour** (e.g., get older, gain weight) [≈ verbs]

5 of 68

OO Thinking: Templates vs. Instances (2.1)



Points on a two-dimensional plane are identified by their signed distances from the X- and Y-axes. A point may move arbitrarily towards any direction on the plane. Given two points, we are often interested in knowing the distance between them.

- A template called `Point` defines the common
 - **attributes** (e.g., x, y) [≈ nouns]
 - **behaviour** (e.g., move up, get distance from) [≈ verbs]

7 of 68

OO Thinking: Templates vs. Instances (1.2)



- Persons share these common *attributes* and *behaviour*.
 - Each person possesses an age, a weight, and a height.
 - Each person's age, weight, and height might be *distinct*
e.g., jim is 50-years old, 1.8-meters tall and 80-kg heavy
e.g., jonathan is 65-years old, 1.73-meters tall and 90-kg heavy
- Each person, depending on the **specific values** of their attributes, might exhibit *distinct* behaviour:
 - When jim gets older, he becomes 51
 - When jonathan gets older, he becomes 66.
 - jim's BMI is based on his own height and weight $\left[\frac{80}{1.8^2}\right]$
 - jonathan's BMI is based on his own height and weight $\left[\frac{90}{1.73^2}\right]$

6 of 68

OO Thinking: Templates vs. Instances (2.2)



- Points share these common *attributes* and *behaviour*.
 - Each point possesses an x-coordinate and a y-coordinate.
 - Each point's location might be *distinct*
e.g., p1 is located at (3, 4)
e.g., p2 is located at (-4, -3)
- Each point, depending on the **specific values** of their attributes (i.e., locations), might exhibit *distinct* behaviour:
 - When p1 moves up for 1 unit, it will end up being at (3, 5)
 - When p2 moves up for 1 unit, it will end up being at (-4, -2)
 - Then, p1's distance from origin: $\left[\sqrt{3^2 + 5^2}\right]$
 - Then, p2's distance from origin: $\left[\sqrt{(-4)^2 + (-2)^2}\right]$

8 of 68

OO Thinking: Templates vs. Instances (3)



- A **template** defines what's **shared** by a set of related entities.
 - Common **attributes** (age in Person, x in Point)
 - Common **behaviour** (get older for Person, move up for Point)
- Each template may be **instantiated** into multiple instances.
 - Person instances: jim and jonathan
 - Point instances: p1 and p2
- Each **instance** may have **specific values** for the attributes.
 - Each Person instance has an age:
jim is 50-years old, jonathan is 65-years old
 - Each Point instance has a location:
p1 is at (3,4), p2 is at (-3,-4)
- Therefore, instances of the same template may exhibit **distinct behaviour**.
 - Each Person instance can get older: jim getting older from 50 to 51; jonathan getting older from 65 to 66.
 - Each Point instance can move up: p1 moving up from (3,3) results in (3,4); p1 moving up from (-3,-4) results in (-3,-3).

9 of 68

OOP: Classes \approx Templates



In Java, you use a **class** to define a **template** that enumerates **attributes** that are common to a set of **entities** of interest.

```
public class Person {
    int age;
    String nationality;
    double weight;
    double height;
}
```

```
public class Point {
    double x;
    double y;
}
```

10 of 68

OOP: Define Constructors for Creating Objects (1.1)



- Within class Point, you define **constructors**, specifying how instances of the Point template may be created.

```
public class Point {
    ... /* attributes: x, y */
    Point(double newX, double newY) {
        x = newX;
        y = newY; } }
```

- In the corresponding tester class, each **call** to the Point constructor creates an instance of the Point template.

```
public class PointTester {
    public static void main(String[] args) {
        Point p1 = new Point(2, 4);
        println(p1.x + " " + p1.y);
        Point p2 = new Point(-4, -3);
        println(p2.x + " " + p2.y); } }
```

11 of 68

OOP: Define Constructors for Creating Objects (1.2)



```
Point p1 = new Point(2, 4);
```

1. **RHS (Source) of Assignment:** `new Point(2, 4)` creates a new **Point object** in memory.

Point	
x	2.0
y	4.0

2. **LHS (Target) of Assignment:** `Point p1` declares a **variable** that is meant to store the **address** of **some Point object**.
3. **Assignment:** Executing `=` stores new object's address in p1.



12 of 68

OOP: Define Constructors for Creating Objects (2.1)

- Within class `Person`, you define **constructors**, specifying how instances of the `Person` template may be created.

```
public class Person {
    ... /* attributes: age, nationality, weight, height */
    Person(int newAge, String newNationality) {
        age = newAge;
        nationality = newNationality; } }
```

- In the corresponding tester class, each **call** to the `Person` constructor creates an instance of the `Person` template.

```
public class PersonTester {
    public static void main(String[] args) {
        Person jim = new Person(50, "British");
        println(jim.nationality + " " + jim.age);
        Person jonathan = new Person(60, "Canadian");
        println(jonathan.nationality + " " + jonathan.age); } }
```

13 of 68

Visualizing Objects at Runtime (1)

- To trace a program with sophisticated manipulations of objects, it's critical for you to visualize how objects are:
 - Created using **constructors**

```
Person jim = new Person(50, "British", 80, 1.8);
```
 - Inquired using **accessor methods**

```
double bmi = jim.getBMI();
```
 - Modified using **mutator methods**

```
jim.gainWeightBy(10);
```
- To visualize an object:
 - Draw a **rectangle box** to represent **contents** of that object:
 - Title** indicates the *name of class* from which the object is instantiated.
 - Left column** enumerates *names of attributes* of the instantiated class.
 - Right column** fills in *values* of the corresponding attributes.
 - Draw **arrow(s)** for *variable(s)* that store the object's **address**.

15 of 68

OOP: Define Constructors for Creating Objects (2.2)

```
Person jim = new Person(50, "British");
```

- RHS (Source) of Assignment:** `new Person(50, "British")` creates a new *Person object* in memory.
- LHS (Target) of Assignment:** `Person jim` declares a *variable* that is meant to store the *address of some Person object*.
- Assignment:** Executing `=` stores new object's address in `jim`.

Person	
age	50
nationality	"British"
weight	0.0
height	0.0

Person	
age	50
nationality	"British"
weight	0.0
height	0.0

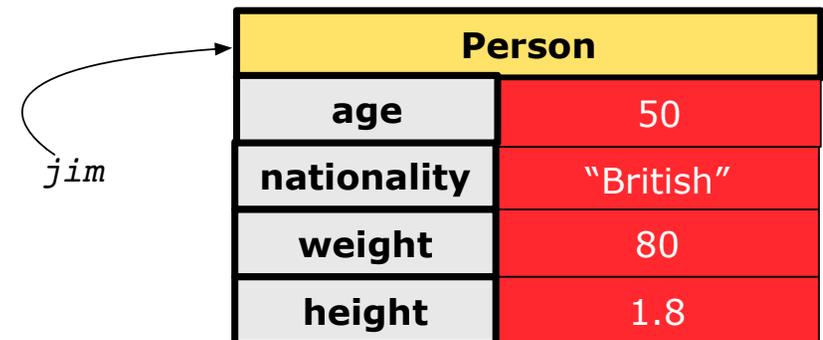
jim →

14 of 68

Visualizing Objects at Runtime (2.1)

After calling a **constructor** to create an object:

```
Person jim = new Person(50, "British", 80, 1.8);
```



16 of 68

Visualizing Objects at Runtime (2.2)



After calling an *accessor* to inquire about context object *jim*:

```
double bmi = jim.getBMI();
```

- Contents of the object pointed to by *jim* remain intact.
- Returned value $\frac{80}{(1.8)^2}$ of *jim.getBMI()* stored in variable *bmi*.

Person	
age	50
nationality	"British"
weight	80
height	1.8

17 of 68

Visualizing Objects at Runtime (2.4)



After calling the same *accessor* to inquire the *modified* state of context object *jim*:

```
bmi = p.getBMI();
```

- Contents of the object pointed to by *jim* remain intact.
- Returned value $\frac{90}{(1.8)^2}$ of *jim.getBMI()* stored in variable *bmi*.

Person	
age	50
nationality	"British"
weight	80 90
height	1.8

19 of 68

Visualizing Objects at Runtime (2.3)



After calling a *mutator* to modify the state of context object *jim*:

```
jim.gainWeightBy(10);
```

- **Contents** of the object pointed to by *jim* change.
- **Address** of the object remains unchanged.
⇒ *jim* points to the same object!

Person	
age	50
nationality	"British"
weight	80 90
height	1.8

18 of 68

The *this* Reference (1)



- Each *class* may be instantiated to multiple *objects* at runtime.

```
class Point {  
    double x; double y;  
    void moveUp(double units) { y += units; }  
}
```

- Each time when we call a method of some class, using the dot notation, there is a specific *target/context* object.

```
1 Point p1 = new Point(2, 3);  
2 Point p2 = new Point(4, 6);  
3 p1.moveUp(3.5);  
4 p2.moveUp(4.7);
```

- *p1* and *p2* are called the **call targets** or **context objects**.
- **Lines 3 and 4** apply the same definition of the `moveUp` method.
- But how does Java distinguish the change to *p1.y* versus the change to *p2.y*?

20 of 68

The this Reference (2)

- In the *method* definition, each *attribute* has an *implicit* `this` which refers to the **context object** in a call to that method.

```
class Point {
    double x;
    double y;
    Point(double newX, double newY) {
        this.x = newX;
        this.y = newY;
    }
    void moveUp(double units) {
        this.y = this.y + units;
    }
}
```

- Each time when the *class* definition is used to create a new *Point object*, the `this` reference is substituted by the name of the new object.

21 of 68

The this Reference (4)

- After we create `p2` as an instance of `Point`

```
Point p2 = new Point(4, 6);
```

- When invoking `p2.moveUp(4.7)`, a version of `moveUp` that is specific to `p2` will be used:

```
class Point {
    double x;
    double y;
    Point(double newX, double newY) {
        p2.x = newX;
        p2.y = newY;
    }
    void moveUp(double units) {
        p2.y = p2.y + units;
    }
}
```

23 of 68

The this Reference (3)

- After we create `p1` as an instance of `Point`

```
Point p1 = new Point(2, 3);
```

- When invoking `p1.moveUp(3.5)`, a version of `moveUp` that is specific to `p1` will be used:

```
class Point {
    double x;
    double y;
    Point(double newX, double newY) {
        p1.x = newX;
        p1.y = newY;
    }
    void moveUp(double units) {
        p1.y = p1.y + units;
    }
}
```

22 of 68

The this Reference (5)

The `this` reference can be used to **disambiguate** when the names of *input parameters* clash with the names of *class attributes*.

```
class Point {
    double x;
    double y;
    Point(double x, double y) {
        this.x = x;
        this.y = y;
    }
    void setX(double x) {
        this.x = x;
    }
    void setY(double y) {
        this.y = y;
    }
}
```

24 of 68

The this Reference (6.1): Common Error



The following code fragment compiles but is problematic:

```
class Person {
    String name;
    int age;
    Person(String name, int age) {
        name = name;
        age = age;
    }
    void setAge(int age) {
        age = age;
    }
}
```

Why? Fix?

25 of 68

The this Reference (6.2): Common Error



Always remember to use `this` when *input parameter* names clash with *class attribute* names.

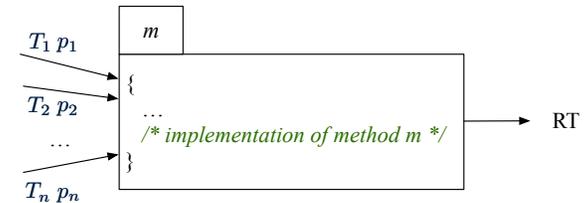
```
class Person {
    String name;
    int age;
    Person(String name, int age) {
        this.name = name;
        this.age = age;
    }
    void setAge(int age) {
        this.age = age;
    }
}
```

26 of 68

OOP: Methods (1.1)



- A **method** is a named block of code, *reusable* via its name.



- The **header** of a method consists of:
 - Return type [*RT* (which can be void)]
 - Name of method [*m*]
 - Zero or more *parameter names* [*p1, p2, ..., pn*]
 - The corresponding *parameter types* [*T1, T2, ..., Tn*]
- A call to method *m* has the form: $m(a_1, a_2, \dots, a_n)$
Types of *argument values* a_1, a_2, \dots, a_n must match the the corresponding parameter types T_1, T_2, \dots, T_n .

27 of 68

OOP: Methods (1.2)



- In the body of the method, you may
 - Declare and use new *local variables*.
Scope of local variables is only within that method.
 - Use or change values of *attributes*.
 - Use values of *parameters*, if any.

```
class Person {
    String nationality;
    void changeNationality(String newNationality) {
        nationality = newNationality; } }
```

- Call a method**, with a **context object**, by passing *arguments*.

```
class PersonTester {
    public static void main(String[] args) {
        Person jim = new Person(50, "British");
        Person jonathan = new Person(60, "Canadian");
        jim.changeNationality("Korean");
        jonathan.changeNationality("Korean"); } }
```

28 of 68

OOP: Methods (2)



- Each **class** `C` defines a list of methods.
 - A **method** `m` is a named block of code.
- We **reuse** the code of method `m` by calling it on an **object** `obj` of class `C`.
 - For each **method call** `obj.m(...)`:
 - `obj` is the **context object** of type `C`
 - `m` is a method defined in class `C`
 - We intend to apply the **code effect of method** `m` to object `obj`.
e.g., `jim.getOlder()` vs. `jonathan.getOlder()`
e.g., `p1.moveUp(3)` vs. `p2.moveUp(3)`
- All objects of class `C` share **the same definition** of method `m`.
- However:
 - ∴ Each object may have **distinct attribute values**.
 - ∴ Applying **the same definition** of method `m` has **distinct effects**.

29 of 68

OOP: The Dot Notation (1.1)



A binary operator:

- LHS stores an address (which denotes an object)
- RHS the name of an attribute or a method
- LHS . RHS means:
 - Locate** the context object whose address is stored in **LHS**, then apply **RHS**.
 - What if LHS stores `null`? [NullPointerException]

31 of 68

OOP: Methods (3)



1. **Constructor**
 - Same name as the class. No return type. **Initializes** attributes.
 - Called with the **new** keyword.
 - e.g., `Person jim = new Person(50, "British");`
2. **Mutator**
 - **Changes** (re-assigns) attributes
 - `void` return type
 - Cannot be used when a value is expected
 - e.g., `double h = jim.setHeight(78.5)` is illegal!
3. **Accessor**
 - **Uses** attributes for computations (without changing their values)
 - Any return type other than `void`
 - An explicit **return statement** (typically at the end of the method) returns the computation result to where the method is being used.
e.g., `double bmi = jim.getBMI();`
e.g., `println(p1.getDistanceFromOrigin());`

30 of 68

OOP: The Dot Notation (1.2)



- Given a **variable** of some **reference type** that is **not null**:
 - We use a dot to retrieve any of its **attributes**.
Analogous to 's in English
e.g., `jim.nationality` means jim's nationality
 - We use a dot to invoke any of its **mutator methods**, in order to **change** values of its attributes.
e.g., `jim.changeNationality("CAN")` changes the **nationality attribute** of `jim`
 - We use a dot to invoke any of its **accessor methods**, in order to **use** the result of some computation on its attribute values.
e.g., `jim.getBMI()` computes and returns the BMI calculated based on `jim`'s weight and height
 - Return value of an **accessor method** must be stored in a variable.
e.g., `double jimBMI = jim.getBMI();`

32 of 68

OOP: Method Calls



```
1 Point p1 = new Point (3, 4);
2 Point p2 = new Point (-6, -8);
3 System.out.println(p1. getDistanceFromOrigin() );
4 System.out.println(p2. getDistanceFromOrigin() );
5 p1. moveUp (2) ;
6 p2. moveUp (2) ;
7 System.out.println(p1. getDistanceFromOrigin() );
8 System.out.println(p2. getDistanceFromOrigin() );
```

- **Lines 1 and 2** create two different instances of `Point`
- **Lines 3 and 4:** invoking the same accessor method on two different instances returns *distinct* values
- **Lines 5 and 6:** invoking the same mutator method on two different instances results in *independent* changes
- **Lines 3 and 7:** invoking the same accessor method on the same instance *may* return *distinct* values, why? **Line 5**

33 of 68

OOP: Class Constructors (2)



```
public class Person {
    int age;
    String nationality;
    double weight;
    double height;
    Person(int initAge, String initNat) {
        age = initAge;
        nationality = initNat;
    }
    Person (double initW, double initH) {
        weight = initW;
        height = initH;
    }
    Person(int initAge, String initNat,
           double initW, double initH) {
        ... /* initialize all attributes using the parameters */
    }
}
```

35 of 68

OOP: Class Constructors (1)



- The purpose of defining a *class* is to be able to create *instances* out of it.
- To *instantiate* a class, we use one of its **constructors**.
- A constructor
 - declares input *parameters*
 - uses input parameters to *initialize* **some or all** of its *attributes*

34 of 68

OOP: Class Constructors (3)



```
public class Point {
    double x;
    double y;

    Point(double initX, double initY) {
        x = initX;
        y = initY;
    }

    Point(char axis, double distance) {
        if (axis == 'x') { x = distance; }
        else if (axis == 'y') { y = distance; }
        else { System.out.println("Error: invalid axis.") }
    }
}
```

36 of 68

OOP: Class Constructors (4)



- For each *class*, you may define **one or more constructors**:
 - *Names* of all constructors must match the class name.
 - **No return types** need to be specified for constructors.
 - Each constructor must have a **distinct** list of *input parameter types*.
 - Each *parameter* that is used to initialize an attribute must have a **matching type**.
 - The *body* of each constructor specifies how **some or all attributes** may be **initialized**.

37 of 68

OOP: Object Creation (1)



```
Point p1 = new Point(2, 4);  
System.out.println(p1);
```

```
Point@677327b6
```

By default, the address stored in `p1` gets printed.
Instead, print out attributes separately:

```
System.out.println("(" + p1.x + ", " + p1.y + ")");
```

```
(2.0, 4.0)
```

38 of 68

OOP: Object Creation (2)

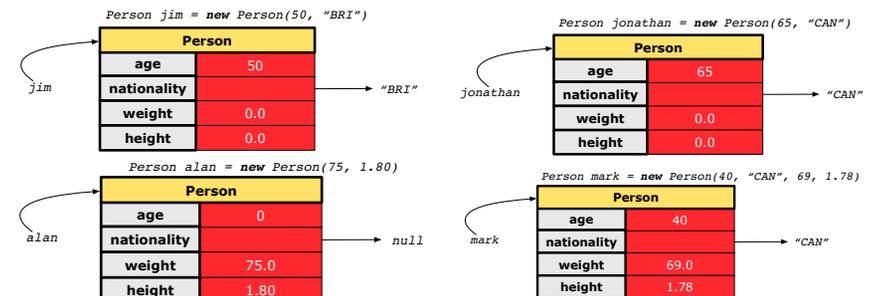


A constructor may only *initialize* some attributes and leave others *uninitialized*.

```
public class PersonTester {  
    public static void main(String[] args) {  
        /* initialize age and nationality only */  
        Person jim = new Person(50, "BRI");  
        /* initialize age and nationality only */  
        Person jonathan = new Person(65, "CAN");  
        /* initialize weight and height only */  
        Person alan = new Person(75, 1.80);  
        /* initialize all attributes of a person */  
        Person mark = new Person(40, "CAN", 69, 1.78);  
    }  
}
```

39 of 68

OOP: Object Creation (3)



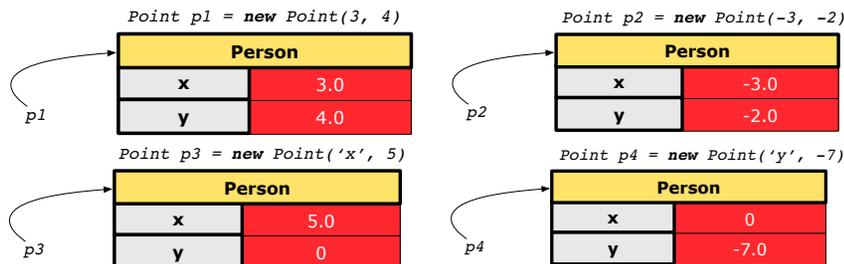
40 of 68

OOP: Object Creation (4)

A constructor may only *initialize* some attributes and leave others *uninitialized*.

```
public class PointTester {
    public static void main(String[] args) {
        Point p1 = new Point(3, 4);
        Point p2 = new Point(-3, -2);
        Point p3 = new Point('x', 5);
        Point p4 = new Point('y', -7);
    }
}
```

OOP: Object Creation (5)



OOP: Object Creation (6)

- When using the constructor, pass **valid argument values**:
 - The type of each argument value must match the corresponding parameter type.
 - e.g., Person(50, "BRI") matches Person(int initAge, String initNationality)
 - e.g., Point(3, 4) matches Point(double initX, double initY)
- When creating an instance, *uninitialized* attributes implicitly get assigned the **default values**.
 - Set *uninitialized* attributes properly later using **mutator** methods

```
Person jim = new Person(50, "British");
jim.setWeight(85);
jim.setHeight(1.81);
```

OOP: Mutator Methods

- These methods *change* values of attributes.
- We call such methods **mutators** (with void return type).

```
public class Person {
    ...
    void gainWeight(double units) {
        weight = weight + units;
    }
}
```

```
public class Point {
    ...
    void moveUp() {
        y = y + 1;
    }
}
```

OOP: Accessor Methods

- These methods *return* the result of computation based on attribute values.
- We call such methods **accessors** (with non-void return type).

```
public class Person {
    ...
    double getBMI() {
        double bmi = height / (weight * weight);
        return bmi;
    }
}
```

```
public class Point {
    ...
    double getDistanceFromOrigin() {
        double dist = Math.sqrt(x*x + y*y);
        return dist;
    }
}
```

45 of 68

OOP: Method Parameters

- **Principle 1:** A **constructor** needs an *input parameter* for every attribute that you wish to initialize.
e.g., Person(double w, double h) vs.
Person(String fName, String lName)
- **Principle 2:** A **mutator** method needs an *input parameter* for every attribute that you wish to modify.
e.g., In Point, void moveToXAxis() vs.
void moveUpBy(double unit)
- **Principle 3:** An **accessor method** needs *input parameters* if the attributes alone are not sufficient for the intended computation to complete.
e.g., In Point, double getDistFromOrigin() vs.
double getDistFrom(Point other)

47 of 68

OOP: Use of Mutator vs. Accessor Methods

- Calls to **mutator methods** *cannot* be used as values.
 - e.g., System.out.println(jim.setWeight(78.5)); ×
 - e.g., double w = jim.setWeight(78.5); ×
 - e.g., jim.setWeight(78.5); ✓
- Calls to **accessor methods** *should* be used as values.
 - e.g., jim.getBMI(); ×
 - e.g., System.out.println(jim.getBMI()); ✓
 - e.g., double w = jim.getBMI(); ✓

46 of 68

OOP: Object Alias (1)

```
1 int i = 3;
2 int j = i; System.out.println(i == j); /* true */
3 int k = 3; System.out.println(k == i && k == j); /* true */
```

- **Line 2** copies the number stored in *i* to *j*.
- **After Line 4**, *i*, *j*, *k* refer to three separate integer placeholder, which happen to store the same value 3.

```
1 Point p1 = new Point(2, 3);
2 Point p2 = p1; System.out.println(p1 == p2); /* true */
3 Point p3 = new Point(2, 3);
4 System.out.println(p3 == p1 || p3 == p2); /* false */
5 System.out.println(p3.x == p1.x && p3.y == p1.y); /* true */
6 System.out.println(p3.x == p2.x && p3.y == p2.y); /* true */
```

- **Line 2** copies the *address* stored in *p1* to *p2*.
- Both *p1* and *p2* refer to the same object in memory!
- *p3*, whose *contents* are same as *p1* and *p2*, refer to a different object in memory.

48 of 68

OO Program Programming: Object Alias (2.1)



Problem: Consider assignments to **primitive** variables:

```
1 int i1 = 1;
2 int i2 = 2;
3 int i3 = 3;
4 int[] numbers1 = {i1, i2, i3};
5 int[] numbers2 = new int[numbers1.length];
6 for(int i = 0; i < numbers1.length; i++) {
7     numbers2[i] = numbers1[i];
8 }
9 numbers1[0] = 4;
10 System.out.println(numbers1[0]);
11 System.out.println(numbers2[0]);
```

49 of 68

OO Program Programming: Object Alias (3)



```
Person tom = new Person("TomCruise");
Person ethanHunt = tom;
Person spy = ethanHunt;
tom.setWeight(77); print(tom.weight); /* 77 */
ethanHunt.gainWeight(10); print(tom.weight); /* 87 */
spy.loseWeight(10); print(tom.weight); /* 77 */
Person prof = new Person("Jackie"); prof.setWeight(80);
spy = prof; prof = tom; tom = spy;
print(prof.name+" teaches 2030");/*TomCruise teaches 2030*/
print("EthanHunt is "+ethanHunt.name);/*EthanHunt is TomCruise*/
print("EthanHunt is "+spy.name);/*EthanHunt is Jackie*/
print("TomCruise is "+tom.name);/*TomCruise is Jackie*/
print("Jackie is "+prof.name);/*Jackie is TomCruise*/
```

- An **object** at runtime may have **more than one identities**. Its **address** may be stored in multiple **reference variables**.
- Calling a **method** on one of an object's identities has the **same effect** as calling the same method on any of its other identities.

51 of 68

OO Program Programming: Object Alias (2.2)



Problem: Consider assignments to **reference** variables:

```
1 Person alan = new Person("Alan");
2 Person mark = new Person("Mark");
3 Person tom = new Person("Tom");
4 Person jim = new Person("Jim");
5 Person[] persons1 = {alan, mark, tom};
6 Person[] persons2 = new Person[persons1.length];
7 for(int i = 0; i < persons1.length; i++) {
8     persons2[i] = persons1[(i + 1) % persons1.length]; }
9 persons1[0].setAge(70);
10 System.out.println(jim.age); /* 0 */
11 System.out.println(alan.age); /* 70 */
12 System.out.println(persons2[0].age); /* 0 */
13 persons1[0] = jim;
14 persons1[0].setAge(75);
15 System.out.println(jim.age); /* 75 */
16 System.out.println(alan.age); /* 70 */
17 System.out.println(persons2[0].age); /* 0 */
```

50 of 68

Anonymous Objects (1)



- What's the difference between these two fragments of code?

```
1 double square(double x) {
2     double sqr = x * x;
3     return sqr; }
1 double square(double x) {
2     return x * x; }
```

After L2, the result of $x * x$:

- LHS: it can be **reused** (without recalculating) via the name `sqr`.
- RHS: it is **not stored** anywhere and returned right away.

- Same principles applies to objects:

```
1 Person getP(String n) {
2     Person p = new Person(n);
3     return p; }
1 Person getP(String n) {
2     return new Person(n); }
```

new Person(n) denotes an object without a name reference.

- LHS: L2 stores the address of this anonymous object in `p`.
- RHS: L2 returns the address of this anonymous object directly.

52 of 68

Anonymous Objects (2.1)

Anonymous objects can also be used as *assignment sources* or *argument values*:

```
class Member {
    Order[] orders;
    int noo;
    /* constructor omitted */
    void addOrder(Order o) {
        orders[noo] = o;
        noo++;
    }
    void addOrder(String n, double p, double q) {
        addOrder(new Order(n, p, q));
        /* Equivalent implementation:
        * orders[noo] = new Order(n, p, q);
        * noo++; */
    }
}
```

53 of 68

Java Data Types (1)

A (data) type denotes a set of related *runtime values*.

1. Primitive Types

- o **Integer** Type
 - int [set of 32-bit integers]
 - long [set of 64-bit integers]
- o **Floating-Point Number** Type
 - double [set of 64-bit FP numbers]
- o **Character** Type
 - char [set of single characters]
- o **Boolean** Type
 - boolean [set of true and false]

2. Reference Type: *Complex Type with Attributes and Methods*

- o **String** [set of references to character sequences]
- o **Person** [set of references to Person objects]
- o **Point** [set of references to Point objects]
- o **Scanner** [set of references to Scanner objects]

55 of 68

Anonymous Objects (2.2)

One more example on using anonymous objects:

```
class MemberTester {
    public static void main(String[] args) {
        Member m = new Member("Alan");
        Order o = new Order("Americano", 4.7, 3);
        m.addOrder(o);
        m.addOrder(new Order("Cafe Latte", 5.1, 4));
    }
}
```

54 of 68

Java Data Types (2)

• A variable that is declared with a *type* but *uninitialized* is implicitly assigned with its **default value**.

- o **Primitive Type**
 - int i; [0 is implicitly assigned to i]
 - double d; [0.0 is implicitly assigned to d]
 - boolean b; [false is implicitly assigned to b]
- o **Reference Type**
 - String s; [null is implicitly assigned to s]
 - Person jim; [null is implicitly assigned to jim]
 - Point p1; [null is implicitly assigned to p1]
 - Scanner input; [null is implicitly assigned to input]

• You *can* use a primitive variable that is *uninitialized*.

Make sure the **default value** is what you want!

• Calling a method on a *uninitialized* reference variable crashes your program. [*NullPointerException*]

Always initialize reference variables!

56 of 68

Java Data Types (3.1)



- An attribute may store the reference to some object.

```
class Person { Person spouse; }
```

- Methods may take as **parameters** references to other objects.

```
class Person {  
    void marry(Person other) { ... } }
```

- **Return values** from methods may be references to other objects.

```
class Point {  
    void moveUpBy(int i) { y = y + i; }  
    Point movedUpBy(int i) {  
        Point np = new Point(x, y);  
        np.moveUp(i);  
        return np;  
    }  
}
```

57 of 68

Java Data Types (3.2.2)



```
1 class PointCollectorTester {  
2     public static void main(String[] args) {  
3         PointCollector pc = new PointCollector();  
4         System.out.println(pc.nop); /* 0 */  
5         pc.addPoint(3, 4);  
6         System.out.println(pc.nop); /* 1 */  
7         pc.addPoint(-3, 4);  
8         System.out.println(pc.nop); /* 2 */  
9         pc.addPoint(-3, -4);  
10        System.out.println(pc.nop); /* 3 */  
11        pc.addPoint(3, -4);  
12        System.out.println(pc.nop); /* 4 */  
13        Point[] ps = pc.getPointsInQuadrantI();  
14        System.out.println(ps.length); /* 1 */  
15        System.out.println("(" + ps[0].x + ", " + ps[0].y + ")");  
16        /* (3, 4) */  
17    }  
18 }
```

59 of 68

Java Data Types (3.2.1)



An attribute may be of type **Point[]**, storing references to Point objects.

```
1 class PointCollector {  
2     Point[] points; int nop; /* number of points */  
3     PointCollector() { points = new Point[100]; }  
4     void addPoint(double x, double y) {  
5         points[nop] = new Point(x, y); nop++; }  
6     Point[] getPointsInQuadrantI() {  
7         Point[] ps = new Point[nop];  
8         int count = 0; /* number of points in Quadrant I */  
9         for(int i = 0; i < nop; i++) {  
10            Point p = points[i];  
11            if(p.x > 0 && p.y > 0) { ps[count] = p; count++; } }  
12        Point[] q1Points = new Point[count];  
13        /* ps contains null if count < nop */  
14        for(int i = 0; i < count; i++) { q1Points[i] = ps[i] }  
15        return q1Points;  
16    } }
```

58 of 68

Required Reading: Point and PointCollector

Static Variables (1)



```
class Account {  
    int id;  
    String owner;  
    Account(int id, String owner) {  
        this.id = id;  
        this.owner = owner;  
    }  
}
```

```
class AccountTester {  
    Account acc1 = new Account(1, "Jim");  
    Account acc2 = new Account(2, "Jeremy");  
    System.out.println(acc1.id != acc2.id);  
}
```

But, managing the unique id's **manually** is **error-prone** !

58 of 68

Static Variables (2)



```
class Account {
    static int globalCounter = 1;
    int id; String owner;
    Account(String owner) {
        this.id = globalCounter; globalCounter++;
        this.owner = owner; } }

```

```
class AccountTester {
    Account acc1 = new Account("Jim");
    Account acc2 = new Account("Jeremy");
    System.out.println(acc1.id != acc2.id); }

```

- Each instance of a class (e.g., acc1, acc2) has a *local* copy of each attribute or instance variable (e.g., id).
 - Changing acc1.id does not affect acc2.id.
- A **static** variable (e.g., globalCounter) belongs to the class.
 - All instances of the class share a *single* copy of the **static** variable.
 - Change to globalCounter via c1 is also visible to c2.

61 of 68

Static Variables (4.1): Common Error



```
class Client {
    Account[] accounts;
    static int numberOfAccounts = 0;
    void addAccount(Account acc) {
        accounts[numberOfAccounts] = acc;
        numberOfAccounts++;
    } }

```

```
class ClientTester {
    Client bill = new Client("Bill");
    Client steve = new Client("Steve");
    Account acc1 = new Account();
    Account acc2 = new Account();
    bill.addAccount(acc1);
    /* correctly added to bill.accounts[0] */
    steve.addAccount(acc2);
    /* mistakenly added to steve.accounts[1]! */
}

```

63 of 68

Static Variables (3)



```
class Account {
    static int globalCounter = 1;
    int id; String owner;
    Account(String owner) {
        this.id = globalCounter;
        globalCounter++;
        this.owner = owner;
    } }

```

- **Static** variable globalCounter is not instance-specific like *instance* variable (i.e., attribute) id is.
- To access a **static** variable:
 - **No** context object is needed.
 - Use of the class name suffices, e.g., Account.globalCounter.
- Each time Account's constructor is called to create a new instance, the increment effect is *visible to all existing objects* of Account.

62 of 68

Static Variables (4.2): Common Error



- Attribute numberOfAccounts should **not** be declared as static as its value should be specific to the client object.
- If it were declared as static, then every time the addAccount method is called, although on different objects, the increment effect of numberOfAccounts will be visible to all Client objects.
- Here is the correct version:

```
class Client {
    Account[] accounts;
    int numberOfAccounts = 0;
    void addAccount(Account acc) {
        accounts[numberOfAccounts] = acc;
        numberOfAccounts++;
    } }

```

64 of 68

Static Variables (5.1): Common Error



```
1 public class Bank {
2     public string branchName;
3     public static int nextAccountNumber = 1;
4     public static void useAccountNumber() {
5         System.out.println (branchName + ...);
6         nextAccountNumber ++;
7     }
8 }
```

- *Non-static method cannot be referenced from a static context*
- **Line 4** declares that we **can** call the method `useAccountNumber` without instantiating an object of the class `Bank`.
- However, in **Lined 5**, the *static* method references a *non-static* attribute, for which we **must** instantiate a `Bank` object.

65 of 68

Static Variables (5.3): Common Error



There are two possible ways to fix:

1. Remove all uses of *non-static* variables (i.e., `branchName`) in the *static* method (i.e., `useAccountNumber`).
2. Declare `branchName` as a *static* variable.
 - This does not make sense.
∴ `branchName` should be a value specific to each `Bank` instance.

67 of 68

Static Variables (5.2): Common Error



```
1 public class Bank {
2     public string branchName;
3     public static int nextAccountNumber = 1;
4     public static void useAccountNumber() {
5         System.out.println (branchName + ...);
6         nextAccountNumber ++;
7     }
8 }
```

- To call `useAccountNumber()`, no instances of `Bank` are required:

```
Bank.useAccountNumber();
```

- *Contradictorily*, to access `branchName`, a *context object* is required:

```
Bank b1 = new Bank(); b1.setBranch("Songdo IBK");
System.out.println(b1.branchName);
```

66 of 68

Index (1)



Separation of Concerns: App/Tester vs. Model

Object Orientation:

Observe, Model, and Execute

Object-Oriented Programming (OOP)

OO Thinking: Templates vs. Instances (1.1)

OO Thinking: Templates vs. Instances (1.2)

OO Thinking: Templates vs. Instances (2.1)

OO Thinking: Templates vs. Instances (2.2)

OO Thinking: Templates vs. Instances (3)

OOP: Classes \approx Templates

OOP:

Define Constructors for Creating Objects (1.1)

OOP:

Define Constructors for Creating Objects (1.2)

68 of 68

Index (2)

OOP:
Define Constructors for Creating Objects (2.1)
OOP:
Define Constructors for Creating Objects (2.2)
Visualizing Objects at Runtime (1)
Visualizing Objects at Runtime (2.1)
Visualizing Objects at Runtime (2.2)
Visualizing Objects at Runtime (2.3)
Visualizing Objects at Runtime (2.4)
The `this` Reference (1)
The `this` Reference (2)
The `this` Reference (3)
The `this` Reference (4)
The `this` Reference (5)

69 of 68

Index (4)

OOP: Object Creation (2)
OOP: Object Creation (3)
OOP: Object Creation (4)
OOP: Object Creation (5)
OOP: Object Creation (6)
OOP: Mutator Methods
OOP: Accessor Methods
OOP: Use of Mutator vs. Accessor Methods
OOP: Method Parameters
OOP: Object Alias (1)
OOP: Object Alias (2.1)
OOP: Object Alias (2.2)
OOP: Object Alias (3)
Anonymous Objects (1)

71 of 68

Index (3)

The `this` Reference (6.1): Common Error
The `this` Reference (6.2): Common Error
OOP: Methods (1.1)
OOP: Methods (1.2)
OOP: Methods (2)
OOP: Methods (3)
OOP: The Dot Notation (1.1)
OOP: The Dot Notation (1.2)
OOP: Method Calls
OOP: Class Constructors (1)
OOP: Class Constructors (2)
OOP: Class Constructors (3)
OOP: Class Constructors (4)
OOP: Object Creation (1)

70 of 68

Index (5)

Anonymous Objects (2.1)
Anonymous Objects (2.2)
Java Data Types (1)
Java Data Types (2)
Java Data Types (3.1)
Java Data Types (3.2.1)
Java Data Types (3.2.2)
Static Variables (1)
Static Variables (2)
Static Variables (3)
Static Variables (4.1): Common Error
Static Variables (4.2): Common Error
Static Variables (5.1): Common Error
Static Variables (5.2): Common Error

72 of 68

Index (6)

Static Variables (5.3): Common Error



73 of 68

Exceptions



EECS2030 B: Advanced
Object Oriented Programming
Fall 2018

CHEN-WEI WANG

Caller vs. Callee



- Within the body implementation of a method, we may call other methods.

```
1 class C1 {
2     void m1() {
3         C2 o = new C2();
4         o.m2(); /* static type of o is C2 */
5     }
6 }
```

- From **Line 4**, we say:
 - Method **C1.m1** (i.e., method `m1` from class `C1`) is the **caller** of method **C2.m2**.
 - Method **C2.m2** is the **callee** of method **C1.m1**.

2 of 41

Why Exceptions? (1.1)



```
1 class Circle {
2     double radius;
3     Circle() { /* radius defaults to 0 */ }
4     void setRadius(double r) {
5         if (r < 0) { System.out.println("Invalid radius."); }
6         else { radius = r; }
7     }
8     double getArea() { return radius * radius * 3.14; }
9 }
```

- A negative radius is considered as an **invalid input value** to method `setRadius`.
- What if the **caller** of `Circle.setRadius` passes a negative value for `r`?
 - An error message is **printed to the console** (**Line 5**) to warn the **caller** of `setRadius`.
 - However, printing an error message to the console **does not force** the **caller** `setRadius` to stop and handle invalid values of `r`.

3 of 41

Why Exceptions? (1.2)

```
1 class CircleCalculator {
2     public static void main(String[] args) {
3         Circle c = new Circle();
4         c.setRadius(-10);
5         double area = c.getArea();
6         System.out.println("Area: " + area);
7     }
8 }
```

- L4: `CircleCalculator.main` is **caller** of `Circle.setRadius`
- A negative radius is passed to `setRadius` in **Line 4**.
- The execution *always flows smoothly* from **Lines 4 to Line 5, even when there was an error message printed from **Line 4**.**
- It is not feasible to check if there is any kind of error message printed to the console right after the execution of **Line 4**.
- **Solution:** A way to force `CircleCalculator.main`, **caller** of `Circle.setRadius`, to realize that things might go wrong.
⇒ When things do go wrong, immediate actions are needed.

4 of 41

Why Exceptions? (2.2)

```
1 class Bank {
2     Account[] accounts; int numberOfAccounts;
3     Account(int id) { ... }
4     void withdrawFrom(int id, double a) {
5         for(int i = 0; i < numberOfAccounts; i++) {
6             if(accounts[i].id == id) {
7                 accounts[i].withdraw(a);
8             }
9         } /* end for */
10    } /* end withdraw */
11 }
```

- L7: `Bank.withdrawFrom` is **caller** of `Account.withdraw`
- What if in **Line 7** the value of `a` is negative?
Error message `Invalid withdraw` printed from method `Account.withdraw` to console.
- Impossible to force `Bank.withdrawFrom`, the **caller** of `Account.withdraw`, to stop and handle invalid values of `a`.

6 of 41

Why Exceptions? (2.1)

```
class Account {
    int id; double balance;
    Account(int id) { this.id = id; /* balance defaults to 0 */ }
    void deposit(double a) {
        if (a < 0) { System.out.println("Invalid deposit."); }
        else { balance += a; }
    }
    void withdraw(double a) {
        if (a < 0 || balance - a < 0) {
            System.out.println("Invalid withdraw."); }
        else { balance -= a; }
    }
}
```

- A negative deposit or withdraw amount is *invalid*.
- When an *error* occurs, a message is *printed to the console*.
- However, printing error messages does not force the **caller** of `Account.deposit` or `Account.withdraw` to stop and handle invalid values of `a`.

5 of 41

Why Exceptions? (2.3)

```
1 class BankApplication {
2     public static void main(String[] args) {
3         Scanner input = new Scanner(System.in);
4         Bank b = new Bank(); Account acc1 = new Account(23);
5         b.addAccount(acc1);
6         double a = input.nextDouble();
7         b.withdrawFrom(23, a);
8     }
}
```

- There is a chain of method calls:
 - `BankApplication.main` calls `Bank.withdrawFrom`
 - `Bank.withdrawFrom` calls `Account.withdraw`.
- The actual update of balance occurs at the `Account` class.
 - What if in **Line 7** the value of `a` is negative?
`Invalid withdraw` printed from `Bank.withdrawFrom`, printed from `Account.withdraw` to console.
 - Impossible to force `BankApplication.main`, the **caller** of `Bank.withdrawFrom`, to stop and handle invalid values of `a`.
- **Solution:** Define error checking only once and let it *propagate*.

7 of 41

What is an Exception?



- An **exception** is an *event*, which
 - occurs during the *execution of a program*
 - *disrupts the normal flow* of the program's instructions
- When an error occurs within a method:
 - the method throws an exception:
 - first creates an *exception object*
 - then hands it over to the *runtime system*
 - the exception object contains information about the error:
 - type [e.g., NegativeRadiusException]
 - the state of the program when the error occurred

8 of 41

Exceptions in Java (1.1)



```
public class InvalidRadiusException extends Exception {
    public InvalidRadiusException(String s) {
        super(s);
    }
}
```

- A new kind of Exception: InvalidRadiusException
- For any method that can have this kind of error, we declare at that method's *signature* that it may *throw* an InvalidRadiusException object.

9 of 41

Exceptions in Java (1.2)



```
class Circle {
    double radius;
    Circle() { /* radius defaults to 0 */ }
    void setRadius(double r) throws InvalidRadiusException {
        if (r < 0) {
            throw new InvalidRadiusException("Negative radius.");
        }
        else { radius = r; }
    }
    double getArea() { return radius * radius * 3.14; }
}
```

- As part of the *signature* of setRadius, we declare that it may *throw* an InvalidRadiusException object at runtime.
- Any method that calls setRadius will be forced to *deal with this potential error*.

10 of 41

Exceptions in Java (1.3)



```
1 class CircleCalculator1 {
2     public static void main(String[] args) {
3         Circle c = new Circle();
4         try {
5             c.setRadius(-10);
6             double area = c.getArea();
7             System.out.println("Area: " + area);
8         }
9         catch(InvalidRadiusException e) {
10            System.out.println(e);
11        }
12    }
}
```

- **Lines 6** is forced to be wrapped within a **try-catch** block, since it may *throw* an InvalidRadiusException object.
- If an InvalidRadiusException object is thrown from **Line 6**, then the normal flow of execution is *interrupted* and we go to the catch block starting from **Line 9**.

11 of 41

Exceptions in Java (1.4.1)



Exercise: Extend `CircleCalculator1`: repetitively prompt for a new radius value until a valid one is entered (i.e., the `InvalidRadiusException` does not occur).

12 of 41

Exceptions in Java (1.4.2)



```
1 public class CircleCalculator2 {
2     public static void main(String[] args) {
3         Scanner input = new Scanner(System.in);
4         boolean inputRadiusIsValid = false;
5         while (!inputRadiusIsValid) {
6             System.out.println("Enter a radius:");
7             double r = input.nextDouble();
8             Circle c = new Circle();
9             try { c.setRadius(r);
10                inputRadiusIsValid = true;
11                System.out.print("Circle with radius " + r);
12                System.out.println(" has area: " + c.getArea()); }
13         catch (InvalidRadiusException e) { print("Try again!"); }
14     } }
```

- At L7, if the user's input value is:
 - Non-Negative: L8 – L12. [`inputRadiusIsValid` set **true**]
 - Negative: L8, L9, L13. [`inputRadiusIsValid` remains **false**]

13 of 41

Exceptions in Java (2.1)



```
public class InvalidTransactionException extends Exception {
    public InvalidTransactionException(String s) {
        super(s);
    }
}
```

- A new kind of Exception:
`InvalidTransactionException`
- For any method that can have this kind of error, we declare at that method's *signature* that it may **throw** an `InvalidTransactionException` object.

14 of 41

Exceptions in Java (2.2)



```
class Account {
    int id; double balance;
    Account() { /* balance defaults to 0 */ }
    void withdraw(double a) throws InvalidTransactionException {
        if (a < 0 || balance - a < 0) {
            throw new InvalidTransactionException("Invalid withdraw."); }
        else { balance -= a; }
    }
}
```

- As part of the *signature* of `withdraw`, we declare that it may **throw** an `InvalidTransactionException` object at runtime.
- Any method that calls `withdraw` will be forced to **deal with this potential error**.

15 of 41

Exceptions in Java (2.3)



```
class Bank {
    Account[] accounts; int numberOfAccounts;
    Account(int id) { ... }
    void withdraw(int id, double a)
        throws InvalidTransactionException {
        for(int i = 0; i < numberOfAccounts; i++) {
            if(accounts[i].id == id) {
                accounts[i].withdraw(a);
            }
        }
    } /* end for */ } /* end withdraw */ }
```

- As part of the *signature* of withdraw, we declare that it may *throw* an InvalidTransactionException object.
- Any method that calls withdraw will be forced to *deal with this potential error*.
- We are *propagating* the potential error for the right party (i.e., BankApplication) to handle.

16 of 41

Examples (1)



```
double r = ...;
double a = ...;
try{
    Bank b = new Bank();
    b.addAccount(new Account(34));
    b.deposit(34, 100);
    b.withdraw(34, a);
    Circle c = new Circle();
    c.setRadius(r);
    System.out.println(r.getArea());
}
catch(NegativeRadiusException e) {
    System.out.println(r + " is not a valid radius value.");
    e.printStackTrace();
}
catch(InvalidTransactionException e) {
    System.out.println(r + " is not a valid transaction value.");
    e.printStackTrace();
}
```

18 of 41

Exceptions in Java (2.4)



```
1 class BankApplication {
2     public static void main(String[] args) {
3         Bank b = new Bank();
4         Account acc1 = new Account(23);
5         b.addAccount(acc1);
6         Scanner input = new Scanner(System.in);
7         double a = input.nextDouble();
8         try {
9             b.withdraw(23, a);
10            System.out.println(acc1.balance); }
11        catch (InvalidTransactionException e) {
12            System.out.println(e); } }
```

- **Lines 9** is forced to be wrapped within a *try-catch* block, since it may *throw* an InvalidTransactionException object.
- If an InvalidTransactionException object is thrown from **Line 9**, then the normal flow of execution is interrupted and we go to the catch block starting from **Line 11**.

17 of 41

Example (2.1)



The Integer class supports a method for parsing Strings:

```
public static int parseInt(String s)
    throws NumberFormatException
```

e.g., Integer.parseInt("23") returns 23

e.g., Integer.parseInt("twenty-three") throws a NumberFormatException

Write a fragment of code that prompts the user to enter a string (using nextLine from Scanner) that represents an integer.

If the user input is not a valid integer, then prompt them to enter again.

19 of 41

Example (2.2)



```
Scanner input = new Scanner(System.in);
boolean validInteger = false;
while (!validInteger) {
    System.out.println("Enter an integer:");
    String userInput = input.nextLine();
    try {
        int userInteger = Integer.parseInt(userInput);
        validInteger = true;
    }
    catch(NumberFormatException e) {
        System.out.println(userInput + " is not a valid integer.");
        /* validInteger remains false */
    }
}
```

20 of 41

Example: to Handle or Not to Handle? (1.2)



- We assume the following kind of error for negative values:

```
class NegValException extends Exception {
    NegValException(String s) { super(s); }
}
```

- The above kind of exception may be thrown by calling A.ma.
- We will see three kinds of possibilities of handling this exception:

Version 1:

Handle it in B.mb

Version 2:

Pass it from B.mb and handle it in Tester.main

Version 3:

Pass it from B.mb, then from Tester.main, then throw it to the console.

22 of 41

Example: to Handle or Not to Handle? (1.1)



Consider the following three classes:

```
class A {
    ma(int i) {
        if(i < 0) { /* Error */ }
        else { /* Do something. */ }
    }
}
```

```
class B {
    mb(int i) {
        A oa = new A();
        oa.ma(i); /* Error occurs if i < 0 */
    }
}
```

```
class Tester {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        int i = input.nextInt();
        B ob = new B();
        ob.mb(i); /* Where can the error be handled? */
    }
}
```

21 of 41

Example: to Handle or Not to Handle? (2.1)



Version 1: Handle the exception in B.mb.

```
class A {
    ma(int i) throws NegValException {
        if(i < 0) { throw new NegValException("Error."); }
        else { /* Do something. */ }
    }
}
```

```
class B {
    mb(int i) {
        A oa = new A();
        try { oa.ma(i); }
        catch(NegValException nve) { /* Do something. */ }
    }
}
```

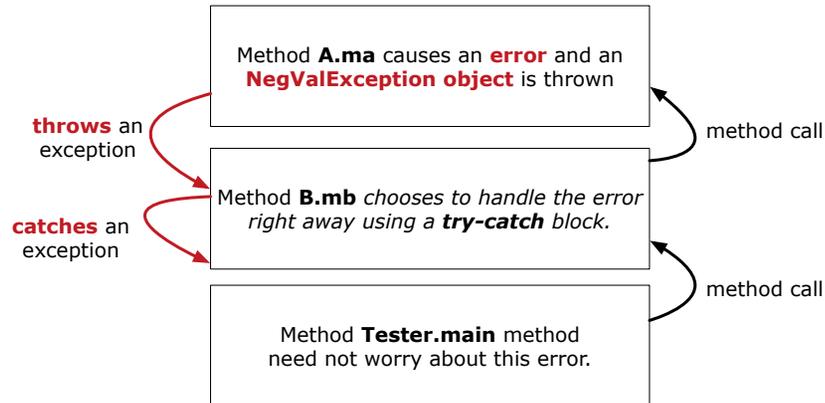
```
class Tester {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        int i = input.nextInt();
        B ob = new B();
        ob.mb(i); /* Error, if any, would have been handled in B.mb. */
    }
}
```

23 of 41

Example: to Handle or Not to Handle? (2.2)



Version 1: Handle the exception in `B.mb`.

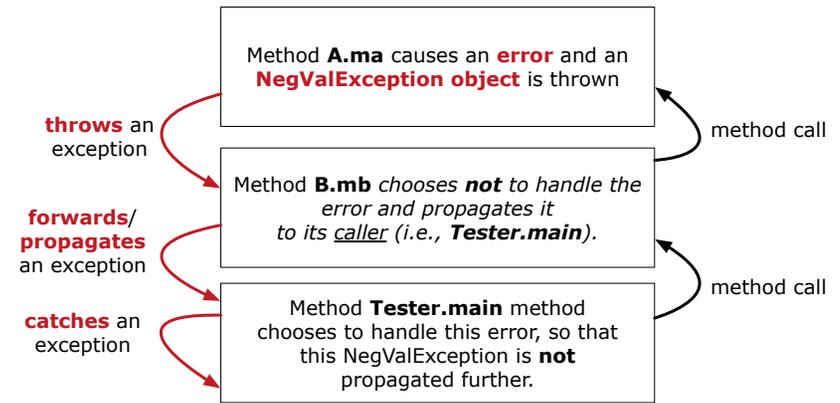


24 of 41

Example: to Handle or Not to Handle? (3.2)



Version 2: Handle the exception in `Tester.main`.



26 of 41

Example: to Handle or Not to Handle? (3.1)



Version 2: Handle the exception in `Tester.main`.

```
class A {
    ma(int i) throws NegValException {
        if(i < 0) { throw new NegValException("Error."); }
        else { /* Do something. */ }
    }
}
```

```
class B {
    mb(int i) throws NegValException {
        A oa = new A();
        oa.ma(i);
    }
}
```

```
class Tester {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        int i = input.nextInt();
        B ob = new B();
        try { ob.mb(i); }
        catch(NegValException nve) { /* Do something. */ }
    }
}
```

25 of 41

Example: to Handle or Not to Handle? (4.1)



Version 3: Handle in neither of the classes.

```
class A {
    ma(int i) throws NegValException {
        if(i < 0) { throw new NegValException("Error."); }
        else { /* Do something. */ }
    }
}
```

```
class B {
    mb(int i) throws NegValException {
        A oa = new A();
        oa.ma(i);
    }
}
```

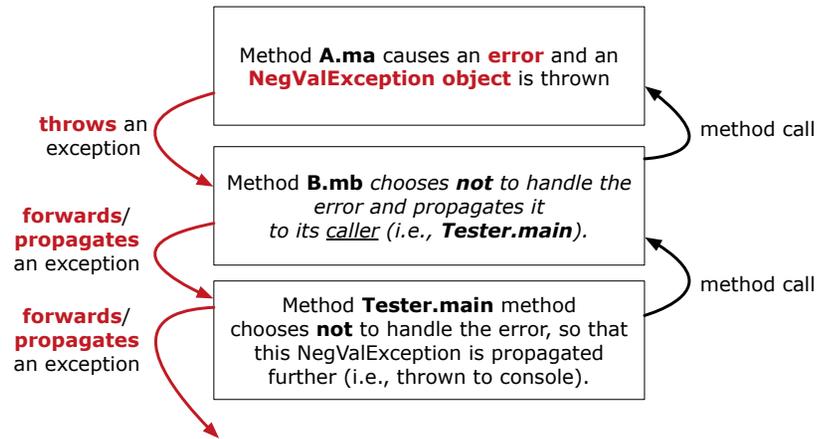
```
class Tester {
    public static void main(String[] args) throws NegValException {
        Scanner input = new Scanner(System.in);
        int i = input.nextInt();
        B ob = new B();
        ob.mb(i);
    }
}
```

27 of 41

Example: to Handle or Not to Handle? (4.2)

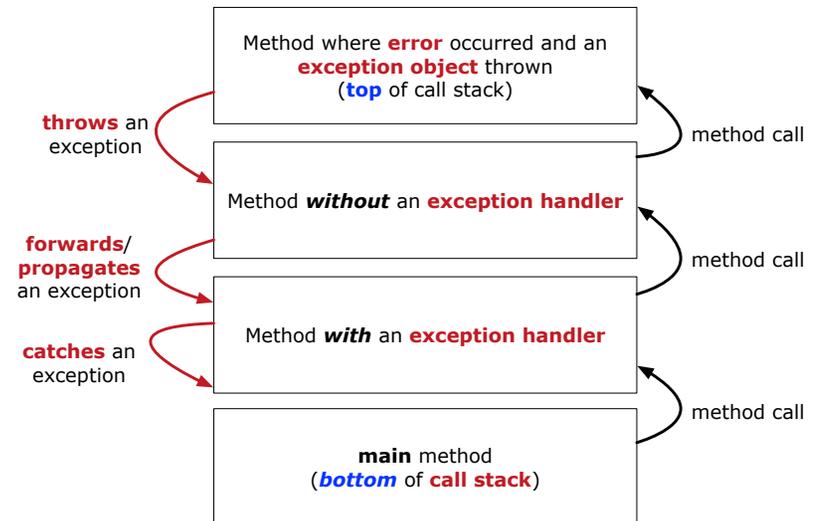


Version 3: Handle in neither of the classes.



28 of 41

What to Do When an Exception Is Thrown? (1)



30 of 41

Stack of Method Calls



- Execution of a Java project *starts* from the **main method** of some class (e.g., `CircleTester`, `BankApplication`).
- Each line of *method call* involves the execution of that method's *body implementation*
 - That method's body implementation may also involve *method calls*, which may in turn involve more *method calls*, and *etc.*
 - It is typical that we end up with **a chain of method calls**!
 - We call this chain of method calls a **call stack**. For example:
 - `Account.withdraw` [top of stack; latest called]
 - `Bank.withdrawFrom`
 - `BankApplication.main` [bottom of stack; earliest called]
 - The closer a method is to the *top* of the call stack, the *later* its call was made.

29 of 41

What to Do When an Exception Is Thrown? (2)



- After a method *throws an exception*, the *runtime system* searches the corresponding **call stack** for a method that contains a block of code to *handle* the exception.
 - This block of code is called an **exception handler**.
 - An exception handler is **appropriate** if the *type* of the *exception object* *thrown* matches the *type* that can be handled by the handler.
 - The exception handler chosen is said to *catch* the exception.
 - The search goes from the *top* to the *bottom* of the call stack:
 - The method in which the *error* occurred is searched first.
 - The *exception handler* is not found in the current method being searched ⇒ Search the method that calls the current method, and *etc.*
 - When an appropriate *handler* is found, the *runtime system* passes the exception to the handler.
 - The *runtime system* searches all the methods on the **call stack** without finding an **appropriate exception handler** ⇒ The program terminates and the exception object is directly "thrown" to the console!

31 of 41

The Catch or Specify Requirement (1)



Code (e.g., a method call) that might throw certain exceptions must be enclosed by one of the two ways:

1. The “Catch” Solution: A `try` statement that *catches and handles the exception*.

```
main(...) {
    Circle c = new Circle();
    try {
        c.setRadius(-10);
    }
    catch(NegativeRadiusException e) {
        ...
    }
}
```

32 of 41

The Catch or Specify Requirement (2)



Code (e.g., a method call) that might throw certain exceptions must be enclosed by one of the two ways:

2. The “Specify” Solution: A method that specifies as part of its *signature* that it *can throw* the exception (without handling that exception).

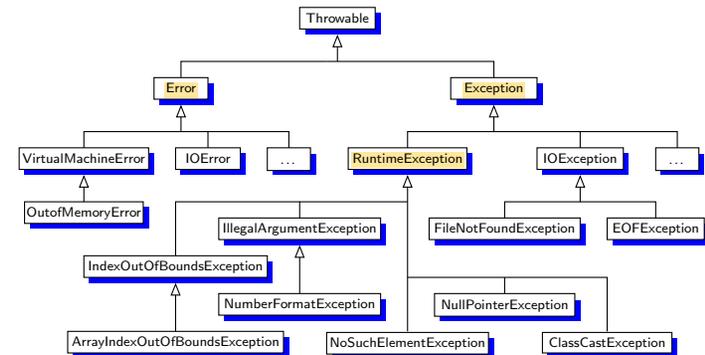
```
class Bank {
    void withdraw (double amount)
        throws InvalidTransactionException {
        ...
        accounts[i].withdraw(amount);
        ...
    }
}
```

33 of 41

The Catch or Specify Requirement (3)



There are *three* basic categories of exceptions



Only one category of exceptions is subject to the **Catch or Specify Requirement**.

34 of 41

Exception Category (1): Checked Exceptions



- **Checked exceptions** are exceptional conditions that a well-written application should anticipate and recover from.
 - An application prompts a user for a circle radius, a deposit/withdraw amount, or the name of a file to open.
 - *Normally*, the user enters a positive number for radius/deposit, a not-too-big positive number for withdraw, and existing file to open.
 - When the user enters invalid numbers or file names, `NegativeRadiusException`, `InvalidTransactionException`, or `FileNotFoundException` is thrown.
 - A well-written program will *catch* this exception and notify the user of the mistake.
- **Checked exceptions** are:
 - subject to the **Catch or Specify Requirement**.
 - subclasses of `Exception` that are *not descendant classes* of `RuntimeException`.

35 of 41

Exception Category (2): Errors



- **Errors** are exceptional conditions that are *external* to the application, and that the application usually cannot anticipate or recover from.
 - An application successfully opens a file for input.
 - But the file cannot be read because of a hardware or system malfunction.
 - The unsuccessful read will throw `java.io.IOException`
- **Errors** are:
 - *not* subject to the **Catch or Specify Requirement**.
 - subclasses of `Error`

36 of 41

Catching and Handling Exceptions



- To construct an **exception handler**:
 1. Enclose the code that might throw an exception within a `try` block.
 2. Associate *each possible kind of exception* that might occur within the `try` block with a `catch` block.
 3. Append an optional `finally` block.

```
try { /* code that might throw exceptions */ }
catch (ExceptionType1 e) { ... }
catch (ExceptionType2 e) { ... }
...
finally { ... }
```

- When an exception is thrown from Line *i* in the `try` block:
 - Normal flow of execution is *interrupted*: the rest of `try` block starting from Line *i* + 1 is skipped.
 - Each `catch` block performs an `instanceof` check on the thrown exception: the first matched `catch` block is executed.
 - The `finally` block is always executed after the matched `catch` block is executed.

38 of 41

Exception Category (3): Runtime Exceptions



- **Runtime exceptions** are exceptional conditions that are *internal* to the application, and that the application usually cannot anticipate or recover from.
 - These usually indicate programming bugs, such as logic errors or improper use of an API.
- e.g., `NullPointerException`
- e.g., `ClassCastException`
- e.g., `ArrayIndexOutOfBoundsException`
- **Runtime exceptions** are:
 - *not* subject to the **Catch or Specify Requirement**.
 - subclasses of `RuntimeException`
- **Errors** and **Runtime exceptions** are collectively known as **unchecked exceptions**.

37 of 41

Examples (3)



```
double r = ...;
double a = ...;
try{
    Bank b = new Bank();
    b.addAccount(new Account(34));
    b.deposit(34, a);
    Circle c = new Circle();
    c.setRadius(r);
    System.out.println(r.getArea());
}
catch (NegativeRadiusException e) {
    System.out.println(r + " is not a valid radius value.");
    e.printStackTrace();
}
catch (InvalidTransactionException e) {
    System.out.println(r + " is not a valid transaction value.");
    e.printStackTrace();
}
catch (Exception e) { /* any other kinds of exceptions */
    e.printStackTrace();
}
```

39 of 41

Examples (4): Problem?



```
double r = ...; double a = ...;
try{
    Bank b = new Bank();
    b.addAccount(new Account(34));
    b.deposit(34, 100);
    b.withdraw(34, a);
    Circle c = new Circle();
    c.setRadius(r);
    System.out.println(r.getArea());
}
/* Every exception object is a descendant of Exception. */
catch (Exception e) {
    e.printStackTrace();
}
catch (NegativeRadiusException e) { /* Problem: Not reachable! */
    System.out.println(r + " is not a valid radius value.");
    e.printStackTrace();
}
catch (InvalidTransactionException e) { /* Problem: Not reachable! */
    System.out.println(r + " is not a valid transaction value.");
    e.printStackTrace();
}
}
```

Index (1)



- Caller vs. Callee
- Why Exceptions? (1.1)
- Why Exceptions? (1.2)
- Why Exceptions? (2.1)
- Why Exceptions? (2.2)
- Why Exceptions? (2.3)
- What is an Exception?
- Exceptions in Java (1.1)
- Exceptions in Java (1.2)
- Exceptions in Java (1.3)
- Exceptions in Java (1.4.1)
- Exceptions in Java (1.4.2)
- Exceptions in Java (2.1)
- Exceptions in Java (2.2)

Index (2)



- Exceptions in Java (2.3)
- Exceptions in Java (2.4)
- Examples (1)
- Example (2.1)
- Example (2.2)
- Example: to Handle or Not to Handle? (1.1)
- Example: to Handle or Not to Handle? (1.2)
- Example: to Handle or Not to Handle? (2.1)
- Example: to Handle or Not to Handle? (2.2)
- Example: to Handle or Not to Handle? (3.1)
- Example: to Handle or Not to Handle? (3.2)
- Example: to Handle or Not to Handle? (4.1)
- Example: to Handle or Not to Handle? (4.2)
- Stack of Method Calls

Index (3)



- What to Do When an Exception Is Thrown? (1)
- What to Do When an Exception Is Thrown? (2)
- The Catch or Specify Requirement (1)
- The Catch or Specify Requirement (2)
- The Catch or Specify Requirement (3)
- Exception Category (1): Checked Exceptions
- Exception Category (2): Errors
- Exception Category (3): Runtime Exceptions
- Catching and Handling Exceptions
- Examples (3)
- Examples (4): Problem?

Test-Driven Development (TDD) with JUnit



EECS2030 B: Advanced
Object Oriented Programming
Fall 2018

CHEN-WEI WANG

Motivating Example: Two Types of Errors (2)



Approach 1 – Specify: Indicate in the method signature that a specific exception might be thrown.

Example 1: Method that throws the exception

```
class C1 {
    void m1(int x) throws ValueTooSmallException {
        if(x < 0) {
            throw new ValueTooSmallException("val " + x);
        }
    }
}
```

Example 2: Method that calls another which throws the exception

```
class C2 {
    C1 c1;
    void m2(int x) throws ValueTooSmallException {
        c1.m1(x);
    }
}
```

3 of 39

Motivating Example: Two Types of Errors (1)



Consider two kinds of exceptions for a counter:

```
public class ValueTooLargeException extends Exception {
    ValueTooLargeException(String s) { super(s); }
}
public class ValueTooSmallException extends Exception {
    ValueTooSmallException(String s) { super(s); }
}
```

Any thrown object instantiated from these two classes must be handled (**catch-specify requirement**):

- Either **specify** throws ... in the method signature (i.e., propagating it to other caller)
- Or **handle** it in a try-catch block

2 of 39

Motivating Example: Two Types of Errors (3)



Approach 2 – Catch: Handle the thrown exception(s) in a try-catch block.

```
class C3 {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        int x = input.nextInt();
        C2 c2 = new C2();
        try {
            c2.m2(x);
        }
        catch(ValueTooSmallException e) { ... }
    }
}
```

4 of 39

A Simple Counter (1)

Consider a class for keeping track of an integer counter value:

```
public class Counter {
    public final static int MAX_VALUE = 3;
    public final static int MIN_VALUE = 0;
    private int value;
    public Counter() {
        this.value = Counter.MIN_VALUE;
    }
    public int getValue() {
        return value;
    }
    ... /* more later! */
}
```

- o Access **private** attribute `value` using **public** accessor `getValue`.
- o Two class-wide (i.e., `static`) constants (i.e., `final`) for lower and upper bounds of the counter value.
- o Initialize the counter value to its lower bound.
- o **Requirement** :

The counter value must be between its lower and upper bounds.

5 of 39

A Simple Counter (2)

```
/* class Counter */
public void increment() throws ValueTooLargeException {
    if (value == Counter.MAX_VALUE) {
        throw new ValueTooLargeException("counter value is " + value);
    }
    else { value++; }
}

public void decrement() throws ValueTooSmallException {
    if (value == Counter.MIN_VALUE) {
        throw new ValueTooSmallException("counter value is " + value);
    }
    else { value--; }
}
```

- o Change the counter value via two mutator methods.
- o Changes on the counter value may **trigger an exception**:
 - Attempt to **increment** when counter already reaches its **maximum**.
 - Attempt to **decrement** when counter already reaches its **minimum**.

7 of 39

Exceptional Scenarios

Consider the two possible exceptional scenarios:

- An attempt to increment **above** the counter's upper bound.
- An attempt to decrement **below** the counter's lower bound.

6 of 39

Components of a Test

- Manipulate the relevant object(s).
e.g., Initialize a counter object `c`, then call `c.increment()`.
- What do you **expect to happen**?
e.g., value of counter is such that `Counter.MIN_VALUE + 1`
- What does your program **actually produce**?
e.g., call `c.getValue` to find out.
- A test:
 - o **Passes** if expected value **matches** actual value
 - o **Fails** if expected value **does not match** actual value
- So far, you ran tests via a tester class with the `main` method.

8 of 39

Testing Counter from Console (V1): Case 1



Consider a class for testing the Counter class:

```
public class CounterTester1 {
    public static void main(String[] args) {
        Counter c = new Counter();
        println("Init val: " + c.getValue());
        try {
            c.decrement();
            println("ValueTooSmallException NOT thrown as expected.");
        }
        catch (ValueTooSmallException e) {
            println("ValueTooSmallException thrown as expected.");
        }
    }
}
```

Executing it as Java Application gives this Console Output:

```
Init val: 0
ValueTooSmallException thrown as expected.
```

9 of 39

Testing Counter from Console (V2)



Consider a different class for testing the Counter class:

```
import java.util.Scanner;
public class CounterTester3 {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        String cmd = null; Counter c = new Counter();
        boolean userWantsToContinue = true;
        while (userWantsToContinue) {
            println("Enter \"inc\", \"dec\", or \"val\":");
            cmd = input.nextLine();
            try {
                if (cmd.equals("inc")) { c.increment(); }
                else if (cmd.equals("dec")) { c.decrement(); }
                else if (cmd.equals("val")) { println(c.getValue()); }
                else { userWantsToContinue = false; println("Bye!"); }
            }
            catch (ValueTooLargeException e) { println("Value too big!"); }
            catch (ValueTooSmallException e) { println("Value too small!"); }
        }
    }
}
```

11 of 39

Testing Counter from Console (V1): Case 2



Consider another class for testing the Counter class:

```
public class CounterTester2 {
    public static void main(String[] args) {
        Counter c = new Counter();
        println("Current val: " + c.getValue());
        try { c.increment(); c.increment(); c.increment(); }
        catch (ValueTooLargeException e) {
            println("ValueTooLargeException thrown unexpectedly."); }
        println("Current val: " + c.getValue());
        try {
            c.increment();
            println("ValueTooLargeException NOT thrown as expected."); }
        catch (ValueTooLargeException e) {
            println("ValueTooLargeException thrown as expected."); } }
}
```

Executing it as Java Application gives this Console Output:

```
Current val: 0
Current val: 3
ValueTooLargeException thrown as expected.
```

10 of 39

Testing Counter from Console (V2): Test 1



Test Case 1: Decrement when the counter value is too small.

```
Enter "inc", "dec", or "val":
val
0
Enter "inc", "dec", or "val":
dec
Value too small!
Enter "inc", "dec", or "val":
exit
Bye!
```

12 of 39

Testing Counter from Console (V2): Test 2



Test Case 2: Increment when the counter value is too big.

```
Enter "inc", "dec", or "val":
inc
Enter "inc", "dec", or "val":
inc
Enter "inc", "dec", or "val":
inc
Enter "inc", "dec", or "val":
val
3
Enter "inc", "dec", or "val":
inc
Value too big!
Enter "inc", "dec", or "val":
exit
Bye!
```

13 of 39

Why JUnit?



- **Automate** the *testing of correctness* of your Java classes.
- Once you derive the list of tests, translate it into a JUnit test case, which is just a Java class that you can execute upon.
- JUnit tests are **helpful callers/clients** of your classes, where each test may:
 - Either attempt to use a method in a *legal* way (i.e., *satisfying* its precondition), and report:
 - **Success** if the result is as expected
 - **Failure** if the result is *not* as expected
 - Or attempt to use a method in an *illegal* way (i.e., *not satisfying* its precondition), and report:
 - **Success** if the expected exception (e.g., `ValueTooSmallException`) occurs.
 - **Failure** if the expected exception does *not* occur.

15 of 39

Limitations of Testing from the Console



- Do **Test Cases 1 & 2** suffice to test `Counter`'s *correctness*?
 - Is it plausible to claim that the implementation of `Counter` is *correct* because it passes the two test cases?
- What other test cases can you think of?

c.getValue ()	c.increment ()	c.decrement ()
0	1	ValueTooSmall
1	2	0
2	3	1
3	ValueTooLarge	2

- So in total we need 8 test cases. ⇒ 6 more separate
 - `CounterTester` classes to create (like `CounterTester1`)!
 - Console interactions with `CounterTester3`!
- Problems? It is inconvenient to:
 - Run each TC by executing `main` of a `CounterTester` and comparing console outputs *with your eyes*.
 - **Re-run manually** all TCs whenever `Counter` is changed.
- **Regression Testing**: Any **change** introduced to your software *must not compromise* its established **correctness**.

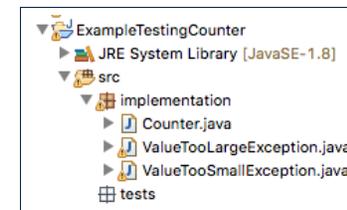
14 of 39

How to Use JUnit: Packages



Step 1:

- In Eclipse, create a Java project `ExampleTestingCounter`
- **Separation of concerns**:
 - Group classes for *implementation* (i.e., `Counter`) into package `implementation`.
 - Group classes for *testing* (to be created) into package `tests`.

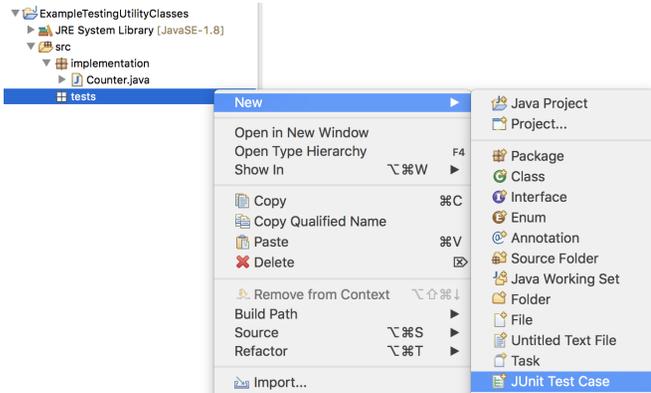


16 of 39

How to Use JUnit: New JUnit Test Case (1)



Step 2: Create a new **JUnit Test Case** in `tests` package.



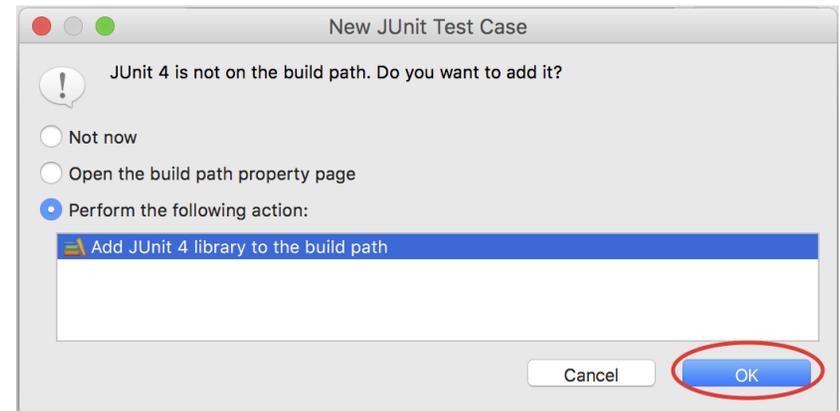
Create one JUnit Test Case to test one Java class only.
⇒ If you have *n Java classes to test*, create *n JUnit test cases*.

17 of 39

How to Use JUnit: Adding JUnit Library



Upon creating the very first test case, you will be prompted to add the JUnit library to your project's build path.

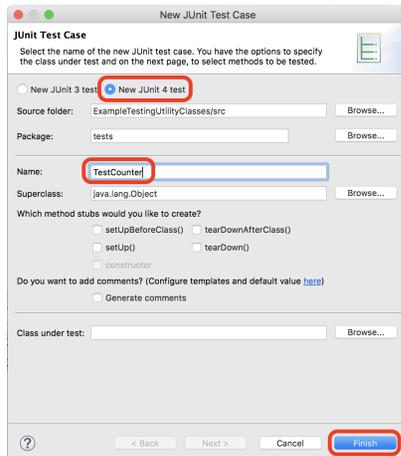


19 of 39

How to Use JUnit: New JUnit Test Case (2)



Step 3: Select the version of JUnit (JUnit 4); Enter the name of test case (`TestCounter`); Finish creating the new test case.



18 of 39

How to Use JUnit: Generated Test Case



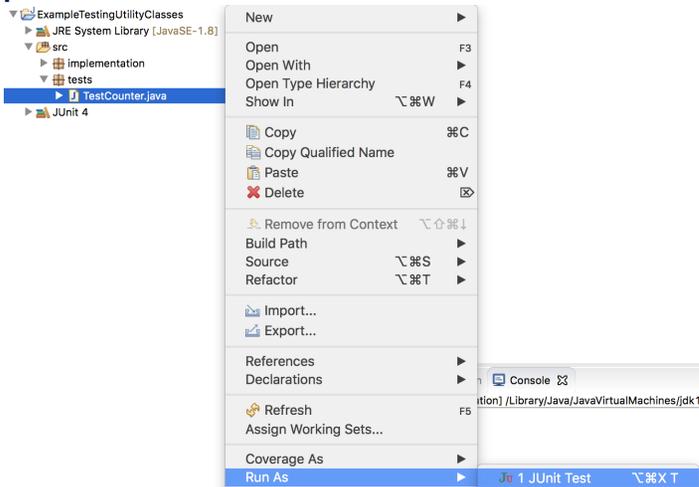
```
TestCounter.java
1 package tests;
2 import static org.junit.Assert.*;
3 import org.junit.Test;
4 public class TestCounter {
5     @Test
6     public void test() {
7         fail("Not yet implemented");
8     }
9 }
```

- Lines 6 – 8: `test` is just an **ordinary mutator method** that has a one-line implementation body.
- Line 5 is critical: Prepend the tag `@Test` verbatim, requiring that **the method is to be treated as a JUnit test**.
⇒ When `TestCounter` is run as a JUnit Test Case, only **those methods prepended by the `@Test` tags** will be run and reported.
- Line 7: By default, we deliberately fail the test with a message “Not yet implemented”.

20 of 39

How to Use JUnit: Running Test Case

Step 4: Run the `TestCounter` class as a JUnit Test.



21 of 39

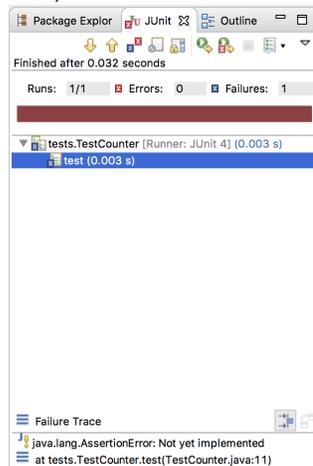
How to Use JUnit: Interpreting Test Report

- A **test** is a method prepended with the `@Test` tag.
- The result of running a test is considered:
 - **Failure** if either
 - an assertion failure (e.g., caused by `fail`, `assertTrue`, `assertEquals`) occurs; or
 - an **unexpected** exception (e.g., `NullPointerException`, `ArrayIndexOutOfBoundsException`) is thrown.
 - **Success** if neither assertion failures nor **unexpected** exceptions occur.
- After running all tests:
 - A **green** bar means that **all** tests succeed.
⇒ Keep challenging yourself if **more tests** may be added.
 - A **red** bar means that **at least one** test fails.
⇒ Keep fixing the class under test and re-running all tests, until you receive a **green** bar.
- **Question:** What is the easiest way to making test a **success**?
Answer: Delete the call `fail("Not yet implemented")`.

23 of 39

How to Use JUnit: Generating Test Report

A **report** is generated after running all tests (i.e., methods prepended with `@Test`) in `TestCounter`.



22 of 39

How to Use JUnit: Revising Test Case

```
TestCounter.java ☒
1 package tests;
2 import static org.junit.Assert.*;
3 import org.junit.Test;
4 public class TestCounter {
5     @Test
6     public void test() {
7         // fail("Not yet implemented");
8     }
9 }
```

Now, the body of `test` simply does nothing.
⇒ Neither assertion failures nor exceptions will occur.
⇒ The execution of `test` will be considered as a **success**.

∴ There is currently only one test in `TestCounter`.
∴ We will receive a **green** bar!

Caution: `test` which passes at the moment is **not useful** at all!

24 of 39

How to Use JUnit: Re-Running Test Case

A new report is generated after re-running all tests (i.e., methods prepended with @Test) in TestCounter.



How to Use JUnit: Assertion Methods

method name / parameters	description
assertTrue(<i>test</i>) assertTrue("message", <i>test</i>)	Causes this test method to fail if the given boolean test is not true.
assertFalse(<i>test</i>) assertFalse("message", <i>test</i>)	Causes this test method to fail if the given boolean test is not false.
assertEquals(<i>expectedValue</i> , <i>value</i>) assertEquals("message", <i>expectedValue</i> , <i>value</i>)	Causes this test method to fail if the given two values are not equal to each other. (For objects, it uses the equals method to compare them.) The first of the two values is considered to be the result that you expect; the second is the actual result produced by the class under test.
assertNotEquals(<i>value1</i> , <i>value2</i>) assertNotEquals("message", <i>value1</i> , <i>value2</i>)	Causes this test method to fail if the given two values are equal to each other. (For objects, it uses the equals method to compare them.)
assertNull(<i>value</i>) assertNull("message", <i>value</i>)	Causes this test method to fail if the given value is not null.
assertNotNull(<i>value</i>) assertNotNull("message", <i>value</i>)	Causes this test method to fail if the given value is null.
assertSame(<i>expectedValue</i> , <i>value</i>) assertSame("message", <i>expectedValue</i> , <i>value</i>) assertNotSame(<i>value1</i> , <i>value2</i>) assertNotSame("message", <i>value1</i> , <i>value2</i>)	Identical to assertEquals and assertNotEquals respectively, except that for objects, it uses the == operator rather than the equals method to compare them. (The difference is that two objects that have the same state might be equals to each other, but not == to each other. An object is only == to itself.)
fail() fail("message")	Causes this test method to fail.

How to Use JUnit: Adding More Tests (1)

- Recall the complete list of cases for testing Counter:

c.getValue()	c.increment()	c.decrement()
0	1	ValueTooSmall
1	2	0
2	3	1
3	ValueTooLarge	2

- Let's turn the two cases in the 1st row into two JUnit tests:
 - Test for the green cell *succeeds* if:
 - No failures and exceptions occur; and
 - The new counter value is 1.
 - Tests for red cells *succeed* if the **expected exceptions** occur (ValueTooSmallException & ValueTooLargeException).
- Common JUnit assertion methods:
 - void assertNull(Object o)
 - void assertEquals(expected, actual)
 - void assertEquals(expecteds, actuals)
 - void assertTrue(boolean condition)
 - void fail(String message)

How to Use JUnit: Adding More Tests (2.1)

```

1  @Test
2  public void testIncAfterCreation() {
3      Counter c = new Counter();
4      assertEquals(Counter.MIN_VALUE, c.getValue());
5      try {
6          c.increment();
7          assertEquals(1, c.getValue());
8      } catch (ValueTooBigException e) {
9          /* Exception is not expected to be thrown. */
10         fail("ValueTooBigException is not expected."); } }

```

- Lines 5 & 8: We need a try-catch block because of Line 6. Method increment from class Counter may throw the ValueTooBigException.
- Lines 4, 7 & 10 are all assertions:
 - Lines 4 & 7 assert that c.getValue() returns the expected values.
 - Line 10: an assertion failure ∴ unexpected ValueTooBigException
 - Line 7 can be rewritten as assertTrue(1 == c.getValue()).

How to Use JUnit: Adding More Tests (2.2)



- Don't lose the big picture!
- JUnit test in previous slide automates this console interaction:

```
Enter "inc", "dec", or "val":
val
0
Enter "inc", "dec", or "val":
inc
Enter "inc", "dec", or "val":
val
1
Enter "inc", "dec", or "val":
exit
Bye!
```

- **Automation** is exactly rationale behind using JUnit!

29 of 39

How to Use JUnit: Adding More Tests (3.2)



- Again, don't lose the big picture!
- JUnit test in previous slide automates CounterTester1 and the following console interaction for CounterTester3:

```
Enter "inc", "dec", or "val":
val
0
Enter "inc", "dec", or "val":
dec
Value too small!
Enter "inc", "dec", or "val":
exit
Bye!
```

- Again, **automation** is exactly rationale behind using JUnit!

31 of 39

How to Use JUnit: Adding More Tests (3.1)



```
1 @Test
2 public void testDecFromMinValue() {
3     Counter c = new Counter();
4     assertEquals(Counter.MIN_VALUE, c.getValue());
5     try {
6         c.decrement();
7         fail("ValueTooSmallException is expected.");
8     } catch (ValueTooSmallException e) {
9         /* Exception is expected to be thrown. */
10    }
```

- **Lines 5 & 8:** We need a try-catch block because of **Line 6**. Method decrement from class Counter may throw the ValueTooSmallException.
- **Lines 4 & 7** are both assertions:
 - **Lines 4** asserts that c.getValue() returns the expected value (i.e., Counter.MIN_VALUE).
 - **Line 7:** an assertion failure ∴ expected ValueTooSmallException not thrown

30 of 39

How to Use JUnit: Adding More Tests (4.1)



```
1 @Test
2 public void testIncFromMaxValue() {
3     Counter c = new Counter();
4     try {
5         c.increment(); c.increment(); c.increment();
6     } catch (ValueTooLargeException e) {
7         fail("ValueTooLargeException was thrown unexpectedly.");
8     }
9     assertEquals(Counter.MAX_VALUE, c.getValue());
10    try {
11        c.increment();
12        fail("ValueTooLargeException was NOT thrown as expected.");
13    } catch (ValueTooLargeException e) {
14        /* Do nothing: ValueTooLargeException thrown as expected. */
15    }
```

- **Lines 4 – 8:** We use a try-catch block to express that a VTLE *is not* expected.
- **Lines 9 – 15:** We use a try-catch block to express that a VTLE *is* expected.

32 of 39

How to Use JUnit: Adding More Tests (4.2)



- JUnit test in previous slide **automates** CounterTester2 and the following console interaction for CounterTester3:

```
Enter "inc", "dec", or "val":
inc
Enter "inc", "dec", or "val":
inc
Enter "inc", "dec", or "val":
inc
Enter "inc", "dec", or "val":
val
3
Enter "inc", "dec", or "val":
inc
Value too big!
Enter "inc", "dec", or "val":
exit
Bye!
```

33 of 39

How to Use JUnit: Adding More Tests (5)



Loops can make it effective on generating test cases:

```
1 @Test
2 public void testIncDecFromMiddleValues() {
3     Counter c = new Counter();
4     try {
5         for(int i = Counter.MIN_VALUE; i < Counter.MAX_VALUE; i++) {
6             int currentValue = c.getValue();
7             c.increment();
8             assertEquals(currentValue + 1, c.getValue());
9         }
10        for(int i = Counter.MAX_VALUE; i > Counter.MIN_VALUE; i--) {
11            int currentValue = c.getValue();
12            c.decrement();
13            assertEquals(currentValue - 1, c.getValue());
14        }
15    } catch (ValueTooLargeException e) {
16        fail("ValueTooLargeException is thrown unexpectedly");
17    } catch (ValueTooSmallException e) {
18        fail("ValueTooSmallException is thrown unexpectedly");
19    } }
```

35 of 39

How to Use JUnit: Adding More Tests (4.3)



Q: Can we rewrite testIncFromMaxValue to:

```
1 @Test
2 public void testIncFromMaxValue() {
3     Counter c = new Counter();
4     try {
5         c.increment();
6         c.increment();
7         c.increment();
8         assertEquals(Counter.MAX_VALUE, c.getValue());
9         c.increment();
10        fail("ValueTooLargeException was NOT thrown as expected.");
11    } catch (ValueTooLargeException e) { }
```

No!

At Line 9, we would not know which line throws the VTLE:

- If it was any of the calls in L5 – L7, then it's *not right*.
- If it was L9, then it's *right*.

34 of 39

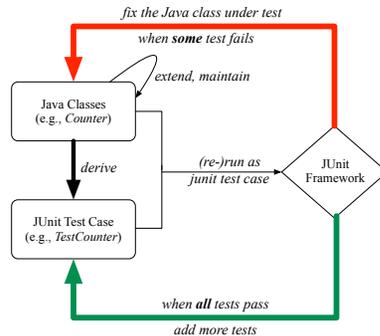
Exercises



- Run all 8 tests and make sure you receive a *green* bar.
- Now, introduce an error to the implementation: Change the line value ++ in Counter.increment to --.
 - Re-run all 8 tests and you should receive a *red* bar. [Why?]
 - Undo the error injection, and re-run all 8 tests. [What happens?]

36 of 39

Test-Driven Development (TDD)



Maintain a collection of tests which define the *correctness* of your Java class under development (CUD):

- Derive and run tests as soon as your CUD is **testable**.
i.e., A Java class is testable when defined with method signatures.
- **Red** bar reported: Fix the class under test (CUT) until **green** bar.
- **Green** bar reported: Add more tests and Fix CUT when necessary.

37 of 39

Resources

- Official Site of JUnit 4:

<http://junit.org/junit4/>

- API of JUnit assertions:

<http://junit.sourceforge.net/javadoc/org/junit/Assert.html>

- Another JUnit Tutorial example:

<https://courses.cs.washington.edu/courses/cse143/11wi/eclipse-tutorial/junit.shtml>

38 of 39

Index (1)

Motivating Example: Two Types of Errors (1)
Motivating Example: Two Types of Errors (2)
Motivating Example: Two Types of Errors (3)
A Simple Counter (1)
Exceptional Scenarios
A Simple Counter (2)
Components of a Test
Testing Counter from Console (V1): Case 1
Testing Counter from Console (V1): Case 2
Testing Counter from Console (V2)
Testing Counter from Console (V2): Test 1
Testing Counter from Console (V2): Test 2
Limitations of Testing from the Console
Why JUnit?

39 of 39

Index (2)

How to Use JUnit: Packages
How to Use JUnit: New JUnit Test Case (1)
How to Use JUnit: New JUnit Test Case (2)
How to Use JUnit: Adding JUnit Library
How to Use JUnit: Generated Test Case
How to Use JUnit: Running Test Case
How to Use JUnit: Generating Test Report
How to Use JUnit: Interpreting Test Report
How to Use JUnit: Revising Test Case
How to Use JUnit: Re-Running Test Case
How to Use JUnit: Adding More Tests (1)
How to Use JUnit: Assertion Methods
How to Use JUnit: Adding More Tests (2.1)
How to Use JUnit: Adding More Tests (2.2)

40 of 39

Index (3)

How to Use JUnit: Adding More Tests (3.1)

How to Use JUnit: Adding More Tests (3.2)

How to Use JUnit: Adding More Tests (4.1)

How to Use JUnit: Adding More Tests (4.2)

How to Use JUnit: Adding More Tests (4.3)

How to Use JUnit: Adding More Tests (5)

Exercises

Test-Driven Development (TDD)

Resources

41 of 39

Advanced Topics on Classes and Objects

Equality (1)

- Recall that
 - A **primitive** variable stores a primitive *value*
e.g., `double d1 = 7.5; double d2 = 7.5;`
 - A **reference** variable stores the *address* to some object (rather than storing the object itself)
e.g., `Point p1 = new Point(2, 3)` assigns to `p1` the address of the new `Point` object
e.g., `Point p2 = new Point(2, 3)` assigns to `p2` the address of *another* new `Point` object
- The binary operator `==` may be applied to compare:
 - Primitive** variables: their *contents* are compared
e.g., `d1 == d2` evaluates to *true*
 - Reference** variables: the *addresses* they store are compared (**rather than** comparing contents of the objects they refer to)
e.g., `p1 == p2` evaluates to *false* because `p1` and `p2` are addresses of *different* objects, even if their contents are *identical*.

2 of 60

Equality (2.1)

- Implicitly:
 - Every class is a *child/sub* class of the **Object** class.
 - The **Object** class is the *parent/super* class of every class.
- There is a useful *accessor method* that every class *inherits* from the **Object** class:

```
boolean equals(Object other)
```

Indicates whether some other object is "equal to" this one.

- The default definition inherited from `Object`:

```
boolean equals(Object other) {
    return (this == other);
}
```

e.g., Say `p1` and `p2` are of type `Point` *via* without the `equals` method redefined, then `p1.equals(p2)` boils down to `(p1 == p2)`.

- Very often when you define new classes, you want to **redefine / override** the inherited definition of `equals`.

3 of 60

Equality (2.2): Common Error



```
int i = 10;
int j = 12;
boolean sameValue = i.equals(j);
```

Compilation Error:

the equals method is only applicable to reference types.

Fix: write `i == j` instead.

4 of 60

Equality (3)



```
class PointV1 {
    double x; double y;
    PointV1(double x, double y) { this.x = x; this.y = y; }
}
```

```
1 PointV1 p1 = new PointV1(2, 3);
2 PointV1 p2 = new PointV1(2, 3);
3 System.out.println(p1 == p2); /* false */
4 System.out.println(p1.equals(p2)); /* false */
```

- At L4, given that the equals method is not explicitly redefined/overridden in class PointV1, the default version inherited from class Object is called. Executing `p1.equals(p2)` boils down to `(p1 == p2)`.
- If we wish to compare contents of two PointV1 objects, need to explicitly redefine/override the equals method in that class.

5 of 60

Requirements of equals



Given that reference variables `x`, `y`, `z` are not null:

- $\neg x.equals(\text{null})$
- Reflexive:**
 $x.equals(x)$
- Symmetric**
 $x.equals(y) \iff y.equals(x)$
- Transitive**
 $x.equals(y) \wedge y.equals(z) \implies x.equals(z)$

6 of 60

API of equals

Inappropriate Def. of equals using hashCode

Equality (4.1)



- How do we compare *contents* rather than addresses?
- Define the **accessor method** equals, e.g.,

```
class PointV2 {
    double x; double y;
    public boolean equals(Object obj) {
        if(this == obj) { return true; }
        if(obj == null) { return false; }
        if(this.getClass() != obj.getClass()) { return false; }
        PointV2 other = (PointV2) obj;
        return this.x == other.x && this.y == other.y; } }
}
```

```
String s = "(2, 3)";
PointV2 p1 = new PointV2(2, 3); PointV2 p2 = new PointV2(2, 3);
System.out.println(p1.equals(p1)); /* true */
System.out.println(p1.equals(null)); /* false */
System.out.println(p1.equals(s)); /* false */
System.out.println(p1 == p2); /* false */
System.out.println(p1.equals(p2)); /* true */
```

7 of 60

Equality (4.2)

- When making a method call `p.equals(o)`:
 - Variable `p` is declared of type `Point V2`
 - Variable `o` can be declared of any type (e.g., `Point V2`, `String`)
- We define `p` and `o` as **equal** if:
 - Either `p` and `o` refer to the same object;
 - Or:
 - `o` is not null.
 - `p` and `o` at runtime point to objects of the same type.
 - The `x` and `y` coordinates are the same.
- Q:** In the `equals` method of `Point`, why is there no such a line:

```
class PointV2 {
    boolean equals(Object obj) {
        if(this == null) { return false; }
    }
}
```

A: If `this` was `null`, a `NullPointerException` would have occurred and prevent the body of `equals` from being executed.

8 of 60

Equality (5)

Two notions of **equality** for variables of **reference** types:

- Reference Equality**: use `==` to compare **addresses**
- Object Equality**: define `equals` method to compare **contents**

```
1 PointV2 p1 = new PointV2(3, 4);
2 PointV2 p2 = new PointV2(3, 4);
3 PointV2 p3 = new PointV2(4, 5);
4 System.out.println(p1 == p1); /* true */
5 System.out.println(p1.equals(p1)); /* true */
6 System.out.println(p1 == p2); /* false */
7 System.out.println(p1.equals(p2)); /* true */
8 System.out.println(p2 == p3); /* false */
9 System.out.println(p2.equals(p3)); /* false */
```

- Being **reference-equal** implies being **object-equal**.
- Being **object-equal** does **not** imply being **reference-equal**.

10 of 60

Equality (4.3)

```
1 class PointV2 {
2     boolean equals(Object obj) { ...
3         if(this.getClass() != obj.getClass()) { return false; }
4         PointV2 other = (PointV2) obj;
5         return this.x == other.x && this.y == other.y; } }
```

- `Object obj` at **L2** declares a parameter `obj` of type `Object`.
- `PointV2 other` at **L4** declares a variable `p` of type `PointV2`. We call such types declared at compile time as **static type**.
- The list of **applicable attributes/methods** that we may call on a variable depends on its **static type**.
 - e.g., We may only call the small list of methods defined in `Object` class on `obj`, which does not include `x` and `y` (specific to `Point`).
- If we are **SURE** that an object's "actual" type is different from its **static type**, then we can **cast** it.
 - e.g., Given that `this.getClass() == obj.getClass()`, we are sure that `obj` is also a `Point`, so we can cast it to `Point`.
- Such cast allows more attributes/methods to be called upon `(Point) obj` at **L5**.

9 of 60

Equality (6.1)

Exercise: Persons are **equal** if names and measures are equal.

```
1 class Person {
2     String firstName; String lastName; double weight; double height;
3     boolean equals(Object obj) {
4         if(this == obj) { return true; }
5         if(obj == null || this.getClass() != obj.getClass()) {
6             return false; }
7         Person other = (Person) obj;
8         return
9             this.weight == other.weight && this.height == other.height
10            && this.firstName.equals(other.firstName)
11            && this.lastName.equals(other.lastName); } }
```

Q: At **L5**, will we get `NullPointerException` if `obj` is `Null`?

A: **No** ∵ Short-Circuit Effect of `||`

`obj` is `null`, then `obj == null` evaluates to **true**

⇒ no need to evaluate the RHS

The left operand `obj == null` acts as a **guard constraint** for the right operand `this.getClass() != obj.getClass()`.

11 of 60

Equality (6.2)

Exercise: Persons are *equal* if names and measures are equal.

```
1 class Person {
2   String firstName; String lastName; double weight; double height;
3   boolean equals (Object obj) {
4     if(this == obj) { return true; }
5     if(obj == null || this.getClass() != obj.getClass()) {
6       return false; }
7     Person other = (Person) obj;
8     return
9       this.weight == other.weight && this.height == other.height
10    && this.firstName.equals (other.firstName)
11    && this.lastName.equals (other.lastName); } }
```

Q: At L5, if swapping the order of two operands of disjunction:

`this.getClass() != obj.getClass() || obj == null`

Will we get `NullPointerException` if `obj` is `Null`?

A: **Yes** ∴ Evaluation of operands is from left to right.

12 of 60

Equality (6.4)

Person collectors are equal if containing equal lists of persons.

```
class PersonCollector {
  Person[] persons; int nop; /* number of persons */
  public PersonCollector() { ... }
  public void addPerson(Person p) { ... }
}
```

Redefine/Override the equals method in PersonCollector.

```
1 boolean equals (Object obj) {
2   if(this == obj) { return true; }
3   if(obj == null || this.getClass() != obj.getClass()) {
4     return false; }
5   PersonCollector other = (PersonCollector) obj;
6   boolean equal = false;
7   if(this.nop == other.nop) {
8     equal = true;
9     for(int i = 0; equal && i < this.nop; i++) {
10      equal = this.persons[i].equals (other.persons[i]); } }
11   return equal;
12 }
```

14 of 60

Equality (6.3)

Exercise: Persons are *equal* if names and measures are equal.

```
1 class Person {
2   String firstName; String lastName; double weight; double height;
3   boolean equals (Object obj) {
4     if(this == obj) { return true; }
5     if(obj == null || this.getClass() != obj.getClass()) {
6       return false; }
7     Person other = (Person) obj;
8     return
9       this.weight == other.weight && this.height == other.height
10    && this.firstName.equals (other.firstName)
11    && this.lastName.equals (other.lastName); } }
```

L10 & L11 call equals method defined in the `String` class.

When defining equals method for your own class, **reuse** equals methods defined in other classes wherever possible.

13 of 60

Equality in JUnit (7.1)

- **assertSame**(obj1, obj2)
 - Passes if `obj1` and `obj2` are references to the same object
 - \approx `assertTrue(obj1 == obj2)`
 - \approx `assertFalse(obj1 != obj2)`

```
PointV1 p1 = new PointV1(3, 4); PointV1 p2 = new PointV1(3, 4);
PointV1 p3 = p1;
assertSame(p1, p3); /* pass */ assertEquals(p2, p3); /* fail */
```

- **assertEquals**(exp1, exp2)
 - \approx `exp1 == exp2` if `exp1` and `exp2` are **primitive type**

```
int i = 10; int j = 20; assertEquals(i, j); /* fail */
```

- \approx `exp1.equals(exp2)` if `exp1` and `exp2` are **reference type**
 - Q:** What if equals is not explicitly defined in `obj1`'s declared type?
 - A:** \approx `assertSame(obj1, obj2)`

```
PointV2 p4 = new PointV2(3, 4); PointV2 p5 = new PointV2(3, 4);
assertEquals(p4, p5); /* pass */
assertEquals(p1, p2); /* fail ∴ different PointV1 objects */
assertEquals(p4, p2); /* fail ∴ different types */
```

15 of 60

Equality in JUnit (7.2)

```
@Test
public void testEqualityOfPointV1() {
    PointV1 p1 = new PointV1(3, 4); PointV1 p2 = new PointV1(3, 4);
    assertFalse(p1 == p2); assertFalse(p2 == p1);
    /* assertEquals(p1, p2); assertEquals(p2, p1); */ /* both fail */
    assertEquals(p1.equals(p2)); assertFalse(p2.equals(p1));
    assertTrue(p1.x == p2.x && p2.y == p2.y);
}

@Test
public void testEqualityOfPointV2() {
    PointV2 p3 = new PointV2(3, 4); PointV2 p4 = new PointV2(3, 4);
    assertFalse(p3 == p4); assertFalse(p4 == p3);
    /* assertEquals(p3, p4); assertEquals(p4, p3); */ /* both fail */
    assertTrue(p3.equals(p4)); assertTrue(p4.equals(p3));
    assertEquals(p3, p4); assertEquals(p4, p3);
}

@Test
public void testEqualityOfPointV1andPointV2() {
    PointV1 p1 = new PointV1(3, 4); PointV2 p2 = new PointV2(3, 4);
    /* These two assertions do not compile because p1 and p2 are of different types. */
    /* assertFalse(p1 == p2); assertFalse(p2 == p1); */
    /* assertEquals can take objects of different types and fail. */
    /* assertEquals(p1, p2); */ /* compiles, but fails */
    /* assertEquals(p2, p1); */ /* compiles, but fails */
    /* version of equals from Object is called */
    assertFalse(p1.equals(p2));
    /* version of equals from PointP2 is called */
    assertFalse(p2.equals(p1));
}
```

16 of 60

Equality in JUnit (7.3)

```
@Test
public void testPersonCollector() {
    Person p1 = new Person("A", "a", 180, 1.8); Person p2 = new Person("A", "a", 180, 1.8);
    Person p3 = new Person("B", "b", 200, 2.1); Person p4 = p3;
    assertFalse(p1 == p2); assertTrue(p1.equals(p2));
    assertTrue(p3 == p4); assertTrue(p3.equals(p4));

    PersonCollector pc1 = new PersonCollector(); PersonCollector pc2 = new PersonCollector();
    assertFalse(pc1 == pc2); assertTrue(pc1.equals(pc2));

    pc1.addPerson(p1);
    assertFalse(pc1.equals(pc2));

    pc2.addPerson(p2);
    assertFalse(pc1.persons[0] == pc2.persons[0]);
    assertTrue(pc1.persons[0].equals(pc2.persons[0]));
    assertTrue(pc1.equals(pc2));

    pc1.addPerson(p3); pc2.addPerson(p4);
    assertTrue(pc1.persons[1] == pc2.persons[1]);
    assertTrue(pc1.persons[1].equals(pc2.persons[1]));
    assertTrue(pc1.equals(pc2));

    pc1.addPerson(new Person("A", "a", 175, 1.75));
    pc2.addPerson(new Person("A", "a", 165, 1.55));
    assertFalse(pc1.persons[2] == pc2.persons[2]);
    assertFalse(pc1.persons[2].equals(pc2.persons[2]));
    assertFalse(pc1.equals(pc2));
}
```

17 of 60

Why Ordering Between Objects? (1)

Each employee has their numerical id and salary.

e.g., (*alan*, 2, 4500.34), (*mark*, 3, 3450.67), (*tom*, 1, 3450.67)

- **Problem:** To facilitate an annual review on their statuses, we want to arrange them so that ones with smaller id's come before ones with larger id's.
e.g., (*tom*, *alan*, *mark*)
- Even better, arrange them so that ones with larger salaries come first; only compare id's for employees with equal salaries.
e.g., (*alan*, *tom*, *mark*)
- **Solution:**
 - Define **ordering** of Employee objects.
[Comparable interface, compareTo method]
 - Use the library method `Arrays.sort`.

18 of 60

Why Ordering Between Objects? (2)

```
class Employee {
    int id; double salary;
    Employee(int id) { this.id = id; }
    void setSalary(double salary) { this.salary = salary; } }
```

```
1 @Test
2 public void testUncomparableEmployees() {
3     Employee alan = new Employee(2);
4     Employee mark = new Employee(3);
5     Employee tom = new Employee(1);
6     Employee[] es = {alan, mark, tom};
7     Arrays.sort(es);
8     Employee[] expected = {tom, alan, mark};
9     assertEquals(expected, es); }
```

L8 triggers a **java.lang.ClassCastException**:

Employee cannot be cast to java.lang.Comparable

∴ `Arrays.sort` expects an array whose element type defines a precise **ordering** of its instances/objects.

17 of 60

Defining Ordering Between Objects (1.1)



```
class CEmployee1 implements Comparable<CEmployee1> {
    ... /* attributes, constructor, mutator similar to Employee */
    @Override
    public int compareTo(CEmployee1 e) { return this.id - e.id; }
}
```

- Given two CEmployee1 objects ce1 and ce2:
 - `ce1.compareTo(ce2) > 0` [ce1 "is greater than" ce2]
 - `ce1.compareTo(ce2) == 0` [ce1 "is equal to" ce2]
 - `ce1.compareTo(ce2) < 0` [ce1 "is smaller than" ce2]
- Say ces is an array of CEmployee1 (CEmployee1[] ces), calling `Arrays.sort(ces)` re-arranges ces, so that:

$\underbrace{ces[0]}_{\text{CEmployee1 object}} \leq \underbrace{ces[1]}_{\text{CEmployee1 object}} \leq \dots \leq \underbrace{ces[ces.length - 1]}_{\text{CEmployee1 object}}$

20 of 60

Defining Ordering Between Objects (2.1)



Let's now make the comparison more sophisticated:

- Employees with higher salaries come before those with lower salaries.
- When two employees have same salary, whoever with lower id comes first.

```
1 class CEmployee2 implements Comparable<CEmployee2> {
2     ... /* attributes, constructor, mutator similar to Employee */
3     @Override
4     public int compareTo(CEmployee2 other) {
5         int salaryDiff = Double.compare(this.salary, other.salary);
6         int idDiff = this.id - other.id;
7         if(salaryDiff != 0) { return -salaryDiff; }
8         else { return idDiff; } } }
```

- L5:** `Double.compare(d1, d2)` returns $-(d1 < d2)$, 0 ($d1 == d2$), or $+(d1 > d2)$.
- L7:** Why inverting the sign of `salaryDiff`?
 - $this.salary > other.salary \Rightarrow Double.compare(this.salary, other.salary) > 0$
 - But we should consider employee with **higher** salary as "smaller".
 \therefore We want that employee to come **before** the other one!

22 of 60

Defining Ordering Between Objects (1.2)



```
@Test
public void testComparableEmployees_1() {
    /*
     * CEmployee1 implements the Comparable interface.
     * Method compareTo compares id's only.
     */
    CEmployee1 alan = new CEmployee1(2);
    CEmployee1 mark = new CEmployee1(3);
    CEmployee1 tom = new CEmployee1(1);
    alan.setSalary(4500.34);
    mark.setSalary(3450.67);
    tom.setSalary(3450.67);
    CEmployee1[] es = {alan, mark, tom};
    /* When comparing employees,
     * their salaries are irrelevant.
     */
    Arrays.sort(es);
    CEmployee1[] expected = {tom, alan, mark};
    assertEquals(expected, es);
}
```

21 of 60

Defining Ordering Between Objects (2.2)



Alternatively, we can use extra `if` statements to express the logic more clearly.

```
1 class CEmployee2 implements Comparable<CEmployee2> {
2     ... /* attributes, constructor, mutator similar to Employee */
3     @Override
4     public int compareTo(CEmployee2 other) {
5         if(this.salary > other.salary) {
6             return -1;
7         }
8         else if (this.salary < other.salary) {
9             return 1;
10        }
11        else { /* equal salaries */
12            return this.id - other.id;
13        }
14    }
```

23 of 60

Defining Ordering Between Objects (2.3)

```

1 @Test
2 public void testComparableEmployees_2() {
3     /*
4      * CEmployee2 implements the Comparable interface.
5      * Method compareTo first compares salaries, then
6      * compares id's for employees with equal salaries.
7      */
8     CEmployee2 alan = new CEmployee2(2);
9     CEmployee2 mark = new CEmployee2(3);
10    CEmployee2 tom = new CEmployee2(1);
11    alan.setSalary(4500.34);
12    mark.setSalary(3450.67);
13    tom.setSalary(3450.67);
14    CEmployee2[] es = {alan, mark, tom};
15    Arrays.sort(es);
16    CEmployee2[] expected = {alan, tom, mark};
17    assertEquals(expected, es);
18 }
    
```

24 of 60

Defining Ordering Between Objects (3)

When you have your class `C` implement the interface `Comparable<C>`, you should design the `compareTo` method, such that given objects `c1`, `c2`, `c3` of type `C`:

- Asymmetric** :

$$\neg(c1.compareTo(c2) < 0 \wedge c2.compareTo(c1) < 0)$$

$$\neg(c1.compareTo(c2) > 0 \wedge c2.compareTo(c1) > 0)$$

\therefore We don't have $c1 < c2$ and $c2 < c1$ at the same time!

- Transitive** :

$$c1.compareTo(c2) < 0 \wedge c2.compareTo(c3) < 0 \Rightarrow c1.compareTo(c3) < 0$$

$$c1.compareTo(c2) > 0 \wedge c2.compareTo(c3) > 0 \Rightarrow c1.compareTo(c3) > 0$$

\therefore We have $c1 < c2 \wedge c2 < c3 \Rightarrow c1 < c3$

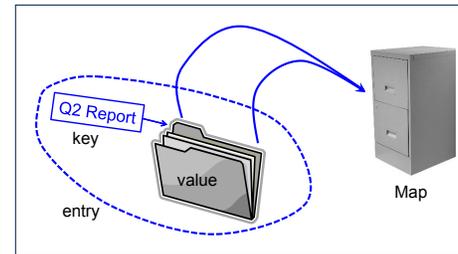
Q. How would you define the `compareTo` method for the

`Player` class of a rock-paper-scissor game? **[Hint: Transitivity]**

25 of 60

Hashing: What is a Map?

- A **map** (a.k.a. table or dictionary) stores a collection of **entries**.



ENTRY	
(SEARCH) KEY	VALUE
1	D
25	C
3	F
14	Z
6	A
39	C
7	Q

- Each **entry** is a pair: a **value** and its (**search**) **key**.
- Each **search key** :
 - Uniquely** identifies an object in the map
 - Should be used to **efficiently** retrieve the associated value
- Search keys must be **unique** (i.e., do not contain duplicates).

26 of 60

Hashing: Arrays are Maps

- Each array **entry** is a pair: an object and its **numerical** index.
e.g., say `String[] a = {"A", "B", "C"}`, how many entries?
3 entries: `(0, "A")`, `(1, "B")`, `(2, "C")`
- Search keys** are the set of numerical index values.
- The set of index values are **unique** [e.g., $0 \dots (a.length - 1)$]
- Given a **valid** index value i , we can
 - Uniquely** determines where the object is $[(i + 1)^{th}$ item]
 - Efficiently** retrieves that object $[a[i] \approx \text{fast memory access}]$
- Maps in general may have **non-numerical** key values:
 - Student ID [student record]
 - Social Security Number [resident record]
 - Passport Number [citizen record]
 - Residential Address [household record]
 - Media Access Control (MAC) Address [PC/Laptop record]
 - Web URL [web page]

27 of 60

Hashing: Naive Implementation of Map

- **Problem:** Support the construction of this simple map:

ENTRY	
(SEARCH) KEY	VALUE
1	D
25	C
3	F
14	Z
6	A
39	C
7	Q

Let's just assume that the maximum map capacity is 100.

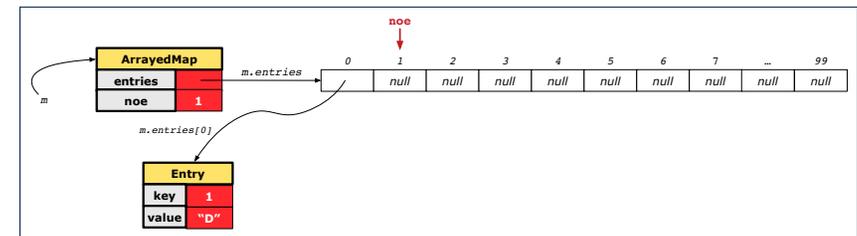
- **Naive Solution:**

Let's understand the expected runtime structures before seeing the Java code!

Hashing: Naive Implementation of Map (1)

After executing `m.put(new Entry(1, "D"))`:

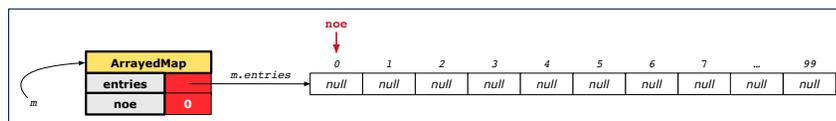
- Attribute `m.entries` has 99 null slots.
- Attribute `m.noE` is 1, meaning:
 - Current number of entries stored in the map is 1.
 - Index for storing the next new entry is 1.



Hashing: Naive Implementation of Map (0)

After executing `ArrayedMap m = new ArrayedMap()`:

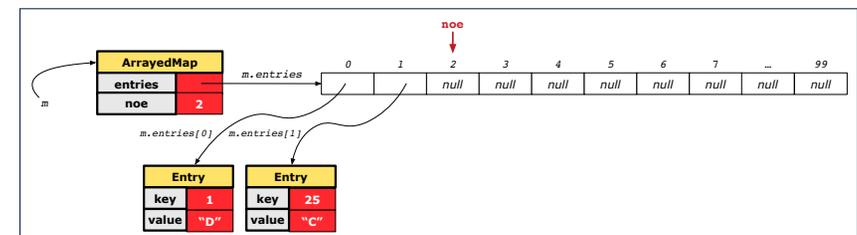
- Attribute `m.entries` initialized as an array of 100 null slots.
- Attribute `m.noE` is 0, meaning:
 - Current number of entries stored in the map is 0.
 - Index for storing the next new entry is 0.



Hashing: Naive Implementation of Map (2)

After executing `m.put(new Entry(25, "C"))`:

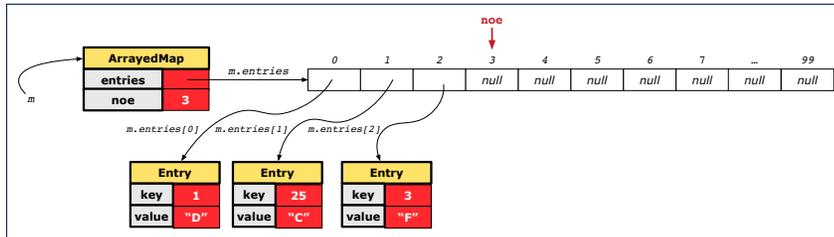
- Attribute `m.entries` has 98 null slots.
- Attribute `m.noE` is 2, meaning:
 - Current number of entries stored in the map is 2.
 - Index for storing the next new entry is 2.



Hashing: Naive Implementation of Map (3)

After executing `m.put(new Entry(3, "F"))`:

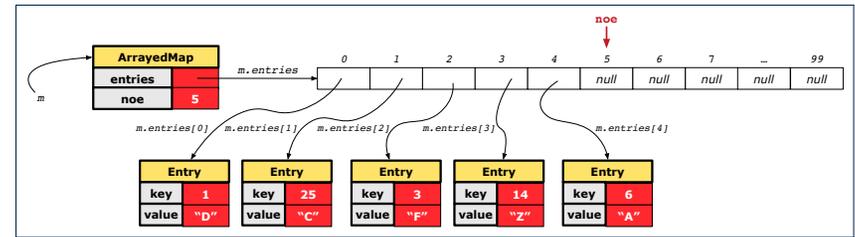
- Attribute `m.entries` has 97 null slots.
- Attribute `m.noe` is 3, meaning:
 - Current number of entries stored in the map is 3.
 - Index for storing the next new entry is 3.



Hashing: Naive Implementation of Map (5)

After executing `m.put(new Entry(6, "A"))`:

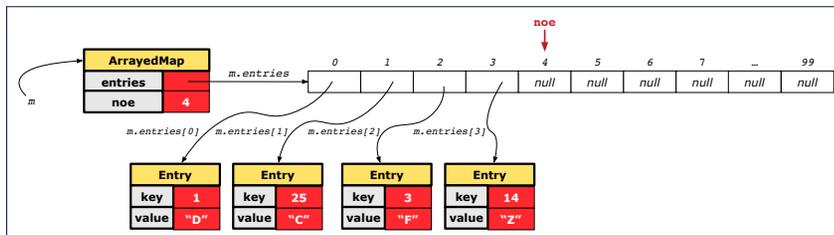
- Attribute `m.entries` has 95 null slots.
- Attribute `m.noe` is 5, meaning:
 - Current number of entries stored in the map is 5.
 - Index for storing the next new entry is 5.



Hashing: Naive Implementation of Map (4)

After executing `m.put(new Entry(14, "Z"))`:

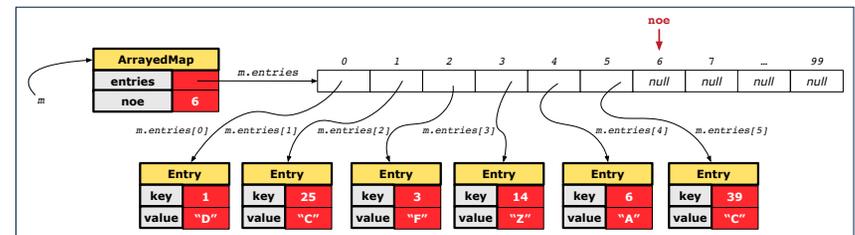
- Attribute `m.entries` has 96 null slots.
- Attribute `m.noe` is 4, meaning:
 - Current number of entries stored in the map is 4.
 - Index for storing the next new entry is 4.



Hashing: Naive Implementation of Map (6)

After executing `m.put(new Entry(39, "C"))`:

- Attribute `m.entries` has 94 null slots.
- Attribute `m.noe` is 6, meaning:
 - Current number of entries stored in the map is 6.
 - Index for storing the next new entry is 6.

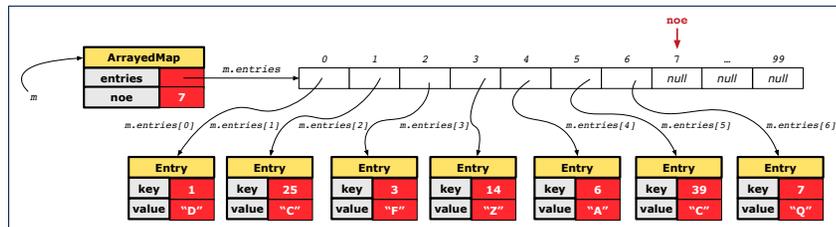


Hashing: Naive Implementation of Map (7)



After executing `m.put(new Entry(7, "Q"))`:

- Attribute `m.entries` has 93 null slots.
- Attribute `m.noe` is 7, meaning:
 - Current number of entries stored in the map is 7.
 - Index for storing the next new entry is 7.



36 of 60

Hashing: Naive Implementation of Map (8.2)



```
public class ArrayedMap {
    private final int MAX_CAPACITY = 100;
    private Entry[] entries;
    private int noe; /* number of entries */
    public ArrayedMap() {
        entries = new Entry[MAX_CAPACITY];
        noe = 0;
    }
    public int size() {
        return noe;
    }
    public void put(int key, String value) {
        Entry e = new Entry(key, value);
        entries[noe] = e;
        noe++;
    }
}
```

Required Reading: Point and PointCollector

38 of 60

Hashing: Naive Implementation of Map (8.1)



```
public class Entry {
    private int key;
    private String value;

    public Entry(int key, String value) {
        this.key = key;
        this.value = value;
    }
    /* Getters and Setters for key and value */
}
```

37 of 60

Hashing: Naive Implementation of Map (8.3)



```
@Test
public void testArrayedMap() {
    ArrayedMap m = new ArrayedMap();
    assertTrue(m.size() == 0);
    m.put(1, "D");
    m.put(25, "C");
    m.put(3, "F");
    m.put(14, "Z");
    m.put(6, "A");
    m.put(39, "C");
    m.put(7, "Q");
    assertTrue(m.size() == 7);
    /* inquiries of existing key */
    assertTrue(m.get(1).equals("D"));
    assertTrue(m.get(7).equals("Q"));
    /* inquiry of non-existing key */
    assertTrue(m.get(31) == null);
}
```

39 of 60

Hashing: Naive Implementation of Map (8.4)



```
public class ArrayedMap {
    private final int MAX_CAPACITY = 100;
    public String get (int key) {
        for (int i = 0; i < noe; i++) {
            Entry e = entries[i];
            int k = e.getKey();
            if (k == key) { return e.getValue(); }
        }
        return null;
    }
}
```

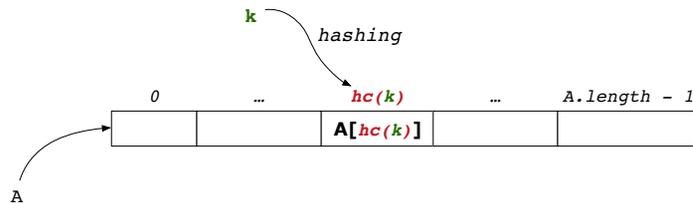
Say entries is: {(1, D), (25, C), (3, F), (14, Z), (6, A), (39, C), (7, Q), null, ...}

- How efficient is `m.get(1)`? [1 iteration]
 - How efficient is `m.get(7)`? [7 iterations]
 - If `m` is full, worst case of `m.get(k)`? [100 iterations]
 - If `m` with 10^6 entries, worst case of `m.get(k)`? [10^6 iterations]
- ⇒ `get`'s worst-case performance is **linear** on size of `m.entries`!

A much **faster** (and **correct**) solution is possible!

40 of 60

Hashing: Hash Table (1)



- Given a (numerical or non-numerical) search key k :
 - Apply a function **hc** so that **hc(k)** returns an integer.
 - We call **hc(k)** the **hash code** of key k .
 - Value of **hc(k)** denotes a **valid index** of some array A .
 - Rather than searching through array A , go directly to $A[hc(k)]$ to get the associated value.
- Both computations are fast:
 - Converting k to **hc(k)**
 - Indexing into $A[hc(k)]$

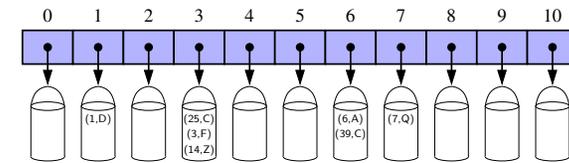
41 of 60

Hashing: Hash Table as a Bucket Array (2.1)



For illustration, assume `A.length` is 11 and $hc(k) = k \% 11$.

$hc(k) = k \% 11$	(SEARCH) KEY	VALUE
1	1	D
3	25	C
3	3	F
3	14	Z
6	6	A
6	39	C
7	7	Q



- Collision**: unequal keys have same hash code (e.g., 25, 3, 14)
 - ⇒ Unavoidable as number of entries \uparrow , but a **good** hash function should have sizes of the buckets uniformly distributed.

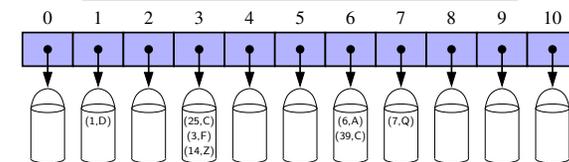
42 of 60

Hashing: Hash Table as a Bucket Array (2.2)



For illustration, assume `A.length` is 10 and $hc(k) = k \% 11$.

$hc(k) = k \% 11$	(SEARCH) KEY	VALUE
1	1	D
3	25	C
3	3	F
3	14	Z
6	6	A
6	39	C
7	7	Q



- Collision**: unequal keys have same hash code (e.g., 25, 3, 14)
 - ⇒ When there are **multiple entries** in the **same bucket**, we distinguish between them using their **unequal** keys.

43 of 60

Hashing: Contract of Hash Function

- Principle of defining a hash function hc :

$$k1.equals(k2) \Rightarrow hc(k1) == hc(k2)$$

Equal keys always have the same hash code.

- Equivalently, according to contrapositive:

$$hc(k1) \neq hc(k2) \Rightarrow \neg k1.equals(k2)$$

Different hash codes must be generated from unequal keys.

- What if $\neg k1.equals(k2)$?
 - $hc(k1) == hc(k2)$ [collision e.g., 25 and 3]
 - $hc(k1) \neq hc(k2)$ [no collision e.g., 25 and 1]
- What if $hc(k1) == hc(k2)$?
 - $\neg k1.equals(k2)$ [collision e.g., 25 and 3]
 - $k1.equals(k2)$ [sound hash function]

inconsistent hashCode and equals

Hashing: Defining Hash Function in Java (2)

```
@Test
public void testCustomizedHashFunction() {
    IntegerKey ik1 = new IntegerKey(1);
    /* 1 % 11 == 1 */
    assertTrue(ik1.hashCode() == 1);

    IntegerKey ik39_1 = new IntegerKey(39); /* 39 % 11 == 6 */
    IntegerKey ik39_2 = new IntegerKey(39);
    IntegerKey ik6 = new IntegerKey(6); /* 6 % 11 == 6 */

    assertTrue(ik39_1.hashCode() == 6);
    assertTrue(ik39_2.hashCode() == 6);
    assertTrue(ik6.hashCode() == 6);

    assertTrue(ik39_1.hashCode() == ik39_2.hashCode());
    assertTrue(ik39_1.equals(ik39_2));

    assertTrue(ik39_1.hashCode() == ik6.hashCode());
    assertFalse(ik39_1.equals(ik6));
}
```

Hashing: Defining Hash Function in Java (1)

The `Object` class (common super class of all classes) has the method for redefining the hash function for your own class:

```
1 public class IntegerKey {
2     private int k;
3     public IntegerKey(int k) { this.k = k; }
4     @Override
5     public int hashCode() { return k % 11; }
6     @Override
7     public boolean equals(Object obj) {
8         if(this == obj) { return true; }
9         if(obj == null) { return false; }
10        if(this.getClass() != obj.getClass()) { return false; }
11        IntegerKey other = (IntegerKey) obj;
12        return this.k == other.k;
13    } }
```

Q: Can we replace L12 by `return this.hashCode() == other.hashCode()`?

A: *No* ∵ When collision happens, keys with same hash code (i.e., in the same bucket) cannot be distinguished.

Hashing: Using Hash Table in Java

```
@Test
public void testHashTable() {
    Hashtable<IntegerKey, String> table = new Hashtable<>();
    IntegerKey k1 = new IntegerKey(39);
    IntegerKey k2 = new IntegerKey(39);
    assertTrue(k1.equals(k2));
    assertTrue(k1.hashCode() == k2.hashCode());
    table.put(k1, "D");
    assertTrue(table.get(k2).equals("D"));
}
```

Hashing: Defining Hash Function in Java (3)



- When you are given instructions as to how the `hashCode` method of a class should be defined, override it manually.
- Otherwise, use Eclipse to generate the `equals` and `hashCode` methods for you.
 - Right click on the class.
 - Select Source.
 - Select Generate `hashCode()` and `equals()`.
 - Select the relevant attributes that will be used to compute the hash value.

48 of 60

Hashing: Defining Hash Function in Java (4.1.1)



Caveat: Always make sure that the `hashCode` and `equals` are redefined/overridden to work together consistently.

e.g., Consider an alternative version of the `IntegerKey` class:

```
public class IntegerKey {
    private int k;
    public IntegerKey(int k) { this.k = k; }
    /* hashCode() inherited from Object NOT overridden. */
    @Override
    public boolean equals(Object obj) {
        if(this == obj) { return true; }
        if(obj == null) { return false; }
        if(this.getClass() != obj.getClass()) { return false; }
        IntegerKey other = (IntegerKey) obj;
        return this.k == other.k;
    }
}
```

49 of 60

Hashing: Defining Hash Function in Java (4.1.2)



```
public class IntegerKey {
    private int k;
    public IntegerKey(int k) { this.k = k; }
    /* hashCode() inherited from Object NOT overridden. */
    @Override
    public boolean equals(Object obj) {
        if(this == obj) { return true; }
        if(obj == null) { return false; }
        if(this.getClass() != obj.getClass()) { return false; }
        IntegerKey other = (IntegerKey) obj;
        return this.k == other.k;
    }
}
```

- **Problem?**
 - Default implementation of `hashCode()` from the `Object` class: Objects with *distinct* addresses have *distinct* hash code values.
 - Violation of the Contract of `hashCode()`:
 $hc(k1) \neq hc(k2) \Rightarrow \neg k1.equals(k2)$
- What about `equal` objects with different addresses?

50 of 60

Hashing: Defining Hash Function in Java (4.2)



```
1 @Test
2 public void testDefaultHashFunction() {
3     IntegerKey ik39_1 = new IntegerKey(39);
4     IntegerKey ik39_2 = new IntegerKey(39);
5     assertTrue(ik39_1.equals(ik39_2));
6     assertTrue(ik39_1.hashCode() != ik39_2.hashCode()); }
7 @Test
8 public void testHashTable() {
9     Hashtable<IntegerKey, String> table = new Hashtable<>();
10    IntegerKey k1 = new IntegerKey(39);
11    IntegerKey k2 = new IntegerKey(39);
12    assertTrue(k1.equals(k2));
13    assertTrue(k1.hashCode() != k2.hashCode());
14    table.put(k1, "D");
15    assertTrue(table.get(k2) == null); }
```

L3, 4, 10, 11: Default version of `hashCode`, inherited from `Object`, returns a *distinct* integer for every new object, *despite its contents*. [**Fix:** Override `hashCode` of your classes!]

51 of 60

Call by Value (1)

- Consider the general form of a call to some *mutator method* `m`, with *context object* `co` and *argument value* `arg`:

```
co.m (arg)
```

- Argument variable `arg` is **not** passed directly for the method call.
- Instead, argument variable `arg` is passed **indirectly**: a **copy** of the value stored in `arg` is made and passed for the method call.
- What can be the type of variable `arg`? [Primitive or Reference]
 - `arg` is primitive type (e.g., `int`, `char`, `boolean`, etc.):
 - Call by Value**: Copy of `arg`'s **stored value** (e.g., `2`, `'j'`, `true`) is made and passed.
 - `arg` is reference type (e.g., `String`, `Point`, `Person`, etc.):
 - Call by Value**: Copy of `arg`'s **stored reference/address** (e.g., `Point@5cb0d902`) is made and passed.

Call by Value (2.2.1)

```
public class Util {
    void reassignInt(int j) {
        j = j + 1; }
    void reassignRef(Point q) {
        Point np = new Point(6, 8);
        q = np; }
    void changeViaRef(Point q) {
        q.moveHorizontally(3);
        q.moveVertically(4); } }

1 @Test
2 public void testCallByVal() {
3     Util u = new Util();
4     int i = 10;
5     assertTrue(i == 10);
6     u.reassignInt(i);
7     assertTrue(i == 10);
8 }
```

- Before** the mutator call at L6, **primitive** variable `i` stores 10.
- When** executing the mutator call at L6, due to **call by value**, a copy of variable `i` is made.
 - ⇒ The assignment `i = i + 1` is only effective on this copy, not the original variable `i` itself.
- ∴ **After** the mutator call at L6, variable `i` still stores 10.

Call by Value (2.1)

For illustration, let's assume the following variant of the `Point` class:

```
class Point {
    int x;
    int y;
    Point(int x, int y) {
        this.x = x;
        this.y = y;
    }
    void moveVertically(int y) {
        this.y += y;
    }
    void moveHorizontally(int x) {
        this.x += x;
    }
}
```

Call by Value (2.2.2)



Call by Value (2.3.1)

```

public class Util {
    void reassignInt(int j) {
        j = j + 1; }
    void reassignRef(Point q) {
        Point np = new Point(6, 8);
        q = np; }
    void changeViaRef(Point q) {
        q.moveHorizontally(3);
        q.moveVertically(4); } }
1  @Test
2  public void testCallByRef_1() {
3      Util u = new Util();
4      Point p = new Point(3, 4);
5      Point refOfPBefore = p;
6      u.reassignRef(p);
7      assertTrue(p==refOfPBefore);
8      assertTrue(p.x==3 && p.y==4);
9  }

```

- **Before** the mutator call at L6, **reference** variable `p` stores the **address** of some `Point` object (whose `x` is 3 and `y` is 4).
- **When** executing the mutator call at L6, due to **call by value**, a **copy of address** stored in `p` is made.
 - ⇒ The assignment `p = np` is only effective on this copy, not the original variable `p` itself.
- ∴ **After** the mutator call at L6, variable `p` still stores the original address (i.e., same as `refOfPBefore`).

56 of 60

Call by Value (2.4.1)

```

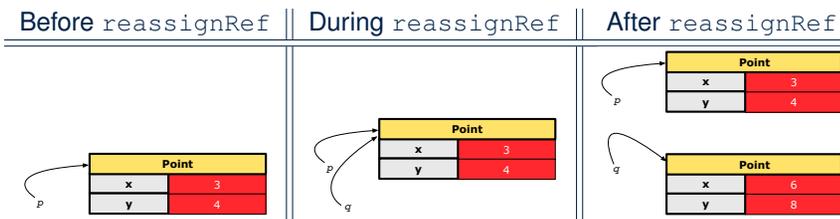
public class Util {
    void reassignInt(int j) {
        j = j + 1; }
    void reassignRef(Point q) {
        Point np = new Point(6, 8);
        q = np; }
    void changeViaRef(Point q) {
        q.moveHorizontally(3);
        q.moveVertically(4); } }
1  @Test
2  public void testCallByRef_2() {
3      Util u = new Util();
4      Point p = new Point(3, 4);
5      Point refOfPBefore = p;
6      u.changeViaRef(p);
7      assertTrue(p==refOfPBefore);
8      assertTrue(p.x==6 && p.y==8);
9  }

```

- **Before** the mutator call at L6, **reference** variable `p` stores the **address** of some `Point` object (whose `x` is 3 and `y` is 4).
- **When** executing the mutator call at L6, due to **call by value**, a **copy of address** stored in `p` is made. **[Alias: `p` and `q` store same address.]**
 - ⇒ Calls to `q.moveHorizontally` and `q.moveVertically` are effective on both `p` and `q`.
- ∴ **After** the mutator call at L6, variable `p` still stores the original address (i.e., same as `refOfPBefore`), but its `x` and `y` have been modified via `q`.

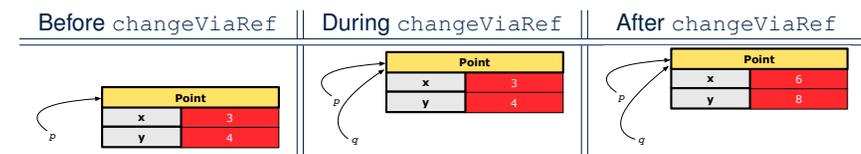
58 of 60

Call by Value (2.3.2)



57 of 60

Call by Value (2.4.2)



59 of 60

Index (1)

- Equality (1)
- Equality (2.1)
- Equality (2.2): Common Error
- Equality (3)
- Requirements of equals
- Equality (4.1)
- Equality (4.2)
- Equality (4.3)
- Equality (5)
- Equality (6.1)
- Equality (6.2)
- Equality (6.3)
- Equality (6.4)
- Equality in JUnit (7.1)

60 of 60

Index (3)

- Hashing: Naive Implementation of Map (1)
- Hashing: Naive Implementation of Map (2)
- Hashing: Naive Implementation of Map (3)
- Hashing: Naive Implementation of Map (4)
- Hashing: Naive Implementation of Map (5)
- Hashing: Naive Implementation of Map (6)
- Hashing: Naive Implementation of Map (7)
- Hashing: Naive Implementation of Map (8.1)
- Hashing: Naive Implementation of Map (8.2)
- Hashing: Naive Implementation of Map (8.3)
- Hashing: Naive Implementation of Map (8.4)
- Hashing: Hash Table (1)
- Hashing: Hash Table as a Bucket Array (2.1)
- Hashing: Hash Table as a Bucket Array (2.2)

62 of 60

Index (2)

- Equality in JUnit (7.2)
- Equality in JUnit (7.3)
- Why Ordering Between Objects? (1)
- Why Ordering Between Objects? (2)
- Defining Ordering Between Objects (1.1)
- Defining Ordering Between Objects (1.2)
- Defining Ordering Between Objects (2.1)
- Defining Ordering Between Objects (2.2)
- Defining Ordering Between Objects (2.3)
- Defining Ordering Between Objects (3)
- Hashing: What is a Map?
- Hashing: Arrays are Maps
- Hashing: Naive Implementation of Map
- Hashing: Naive Implementation of Map (0)

61 of 60

Index (4)

- Hashing: Contract of Hash Function
- Hashing: Defining Hash Function in Java (1)
- Hashing: Defining Hash Function in Java (2)
- Hashing: Using Hash Table in Java
- Hashing: Defining Hash Function in Java (3)
- Hashing: Defining Hash Function in Java (4.1.1)
- Hashing: Defining Hash Function in Java (4.1.2)
- Hashing: Defining Hash Function in Java (4.2)
- Call by Value (1)
- Call by Value (2.1)
- Call by Value (2.2.1)
- Call by Value (2.2.2)

63 of 60

Index (5)

Call by Value (2.3.1)

Call by Value (2.3.2)

Call by Value (2.4.1)

Call by Value (2.4.2)

64 of 60



Algorithm and Data Structure



- A **data structure** is:
 - A systematic way to store and organize data in order to facilitate **access** and **modifications**
 - Never suitable for all purposes: it is important to know its **strengths** and **limitations**
- A **well-specified computational problem** precisely describes the desired **input/output relationship**.
 - **Input**: A sequence of n numbers $\{a_1, a_2, \dots, a_n\}$
 - **Output**: A permutation (reordering) $\{a'_1, a'_2, \dots, a'_n\}$ of the input sequence such that $a'_1 \leq a'_2 \leq \dots \leq a'_n$
 - An **instance** of the problem: $\{3, 1, 2, 5, 4\}$
- An **algorithm** is:
 - A solution to a well-specified **computational problem**
 - A **sequence of computational steps** that takes value(s) as **input** and produces value(s) as **output**
- Steps in an **algorithm** manipulate well-chosen **data structure(s)**.

2 of 40

Asymptotic Analysis of Algorithms

Measuring “Goodness” of an Algorithm



1. **Correctness**:
 - Does the algorithm produce the expected output?
 - Use JUnit to ensure this.
2. Efficiency:
 - **Time Complexity**: processor time required to complete
 - **Space Complexity**: memory space required to store data

Correctness is always the priority.

How about efficiency? Is time or space more of a concern?

3 of 40

Measuring Efficiency of an Algorithm



- **Time** is more of a concern than is **storage**.
- Solutions that are meant to be run on a computer should run **as fast as possible**.
- Particularly, we are interested in how **running time** depends on two **input factors**:
 1. size
e.g., sorting an array of 10 elements vs. 1m elements
 2. structure
e.g., sorting an already-sorted array vs. a hardly-sorted array
- **How do you determine the running time of an algorithm?**
 1. Measure time via **experiments**
 2. Characterize time as a **mathematical function** of the input size

4 of 40

Measure Running Time via Experiments



- Once the algorithm is implemented in Java:
 - Execute the program on **test inputs** of various **sizes** and **structures**.
 - For each test, record the **elapsed time** of the execution.

```
long startTime = System.currentTimeMillis();  
/* run the algorithm */  
long endTime = System.currentTimeMillis();  
long elapsed = endTime - startTime;
```

- **Visualize** the result of each test.
- To make **sound statistical claims** about the algorithm's **running time**, the set of input tests must be "reasonably" **complete**.

5 of 40

Example Experiment



- **Computational Problem**:
 - **Input**: A character c and an integer n
 - **Output**: A string consisting of n repetitions of character c
e.g., Given input `*` and 15, output *****
- **Algorithm 1** using **String** Concatenations:

```
public static String repeat1(char c, int n) {  
    String answer = "";  
    for (int i = 0; i < n; i++) { answer += c; }  
    return answer; }  
}
```

- **Algorithm 2** using **StringBuilder** append's:

```
public static String repeat2(char c, int n) {  
    StringBuilder sb = new StringBuilder();  
    for (int i = 0; i < n; i++) { sb.append(c); }  
    return sb.toString(); }  
}
```

6 of 40

Example Experiment: Detailed Statistics

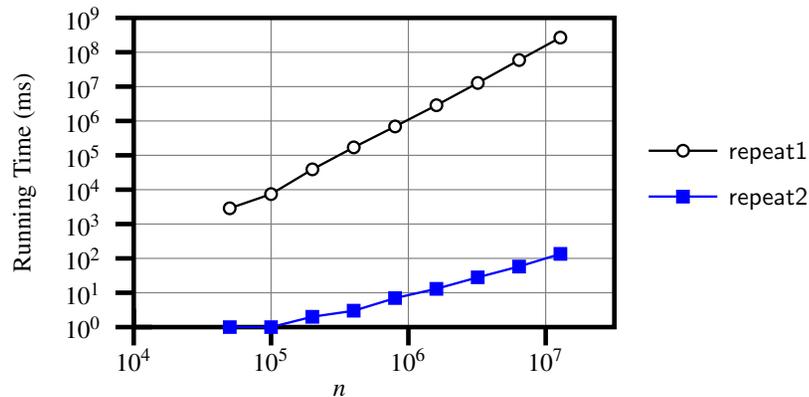


n	repeat1 (in ms)	repeat2 (in ms)
50,000	2,884	1
100,000	7,437	1
200,000	39,158	2
400,000	170,173	3
800,000	690,836	7
1,600,000	2,847,968	13
3,200,000	12,809,631	28
6,400,000	59,594,275	58
12,800,000	265,696,421 (\approx 3 days)	135

- As **input size** is doubled, **rates of increase** for both algorithms are **linear**:
 - **Running time** of repeat1 increases by \approx 5 times.
 - **Running time** of repeat2 increases by \approx 2 times.

7 of 40

Example Experiment: Visualization



8 of 40

Moving Beyond Experimental Analysis

- A better approach to analyzing the *efficiency* (e.g., *running times*) of algorithms should be one that:
 - Allows us to calculate the *relative efficiency* (rather than absolute elapsed time) of algorithms in a way that is *independent of* the hardware and software environment.
 - Can be applied using a *high-level description* of the algorithm (without fully implementing it).
 - Considers *all* possible inputs.
- We will learn a better approach that contains 3 ingredients:
 1. Counting *primitive operations*
 2. Approximating running time as *a function of input size*
 3. Focusing on the *worst-case* input (requiring the most running time)

10 of 40

Experimental Analysis: Challenges

1. An algorithm must be *fully implemented* (i.e., translated into valid Java syntax) in order to study its runtime behaviour *experimentally*.
 - What if our purpose is to *choose among alternative* data structures or algorithms to implement?
 - Can there be a *higher-level analysis* to determine that one algorithm or data structure is *superior* than others?
2. Comparison of multiple algorithms is only *meaningful* when experiments are conducted under the same environment of:
 - *Hardware*: CPU, running processes
 - *Software*: OS, JVM version
3. Experiments can be done only on *a limited set of test inputs*.
 - What if *“important”* inputs were not included in the experiments?

9 of 40

Counting Primitive Operations

A *primitive operation* corresponds to a low-level instruction with a *constant execution time*.

- Assignment [e.g., `x = 5;`]
- Indexing into an array [e.g., `a[i]`]
- Arithmetic, relational, logical op. [e.g., `a + b`, `z > w`, `b1 && b2`]
- Accessing an attribute of an object [e.g., `acc.balance`]
- Returning from a method [e.g., `return result;`]

Q: Why is a *method call* in general *not* a primitive operation?

A: It may be a call to:

- a *“cheap”* method (e.g., printing `Hello World`), or
- an *“expensive”* method (e.g., sorting an array of integers)

11 of 40

Example: Counting Primitive Operations



```

1 findMax (int[] a, int n) {
2   currentMax = a[0];
3   for (int i = 1; i < n; ) {
4     if (a[i] > currentMax) {
5       currentMax = a[i]; }
6     i ++ }
7   return currentMax; }

```

of times $i < n$ in **Line 3** is executed? $[n]$

of times the loop body (**Line 4 to Line 6**) is executed? $[n - 1]$

- **Line 2:** 2 [1 indexing + 1 assignment]
- **Line 3:** $n + 1$ [1 assignment + n comparisons]
- **Line 4:** $(n - 1) \cdot 2$ [1 indexing + 1 comparison]
- **Line 5:** $(n - 1) \cdot 2$ [1 indexing + 1 assignment]
- **Line 6:** $(n - 1) \cdot 2$ [1 addition + 1 assignment]
- **Line 7:** 1 [1 return]
- **Total # of Primitive Operations:** $7n - 2$

12 of 40

Example: Approx. # of Primitive Operations



- Given # of primitive operations counted precisely as $7n^1 - 2$, we view it as

$$7 \cdot n - 2 \cdot n^0$$

- We say
 - n is the **highest power**
 - 7 and 2 are the **multiplicative constants**
 - 2 is the **lower term**
- When approximating a function (considering that input size may be very large):
 - **Only** the **highest power** matters.
 - **multiplicative constants** and **lower terms** can be dropped.

$\Rightarrow 7n - 2$ is approximately n

Exercise: Consider $7n + 2n \cdot \log n + 3n^2$:

- **highest power?** $[n^2]$
- **multiplicative constants?** $[7, 2, 3]$
- **lower terms?** $[7n + 2n \cdot \log n]$

14 of 40

From Absolute RT to Relative RT



- Each **primitive operation** (PO) takes approximately the same, constant amount of time to execute. [say t]
- The **number of primitive operations** required by an algorithm should be **proportional** to its **actual running time** on a specific environment.
e.g., findMax (int[] a, int n) has $7n - 2$ POs

$$RT = (7n - 2) \cdot t$$

Say two algorithms with RT $(7n - 2) \cdot t$ and RT $(10n + 3) \cdot t$.

\Rightarrow It suffices to compare their **relative** running time:
 $7n - 2$ vs. $10n + 3$.

- To determine the **time efficiency** of an algorithm, we only focus on their **number of POs**.

13 of 40

Approximating Running Time as a Function of Input Size

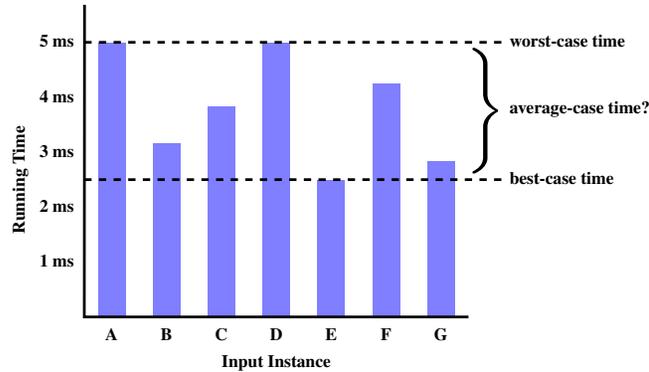


Given the **high-level description** of an algorithm, we associate it with a function f , such that **$f(n)$** returns the **number of primitive operations** that are performed on an **input of size n** .

- $f(n) = 5$ [constant]
- $f(n) = \log_2 n$ [logarithmic]
- $f(n) = 4 \cdot n$ [linear]
- $f(n) = n^2$ [quadratic]
- $f(n) = n^3$ [cubic]
- $f(n) = 2^n$ [exponential]

15 of 40

Focusing on the Worst-Case Input



- **Average-case** analysis calculates the *expected running times* based on the probability distribution of input values.
- **worst-case** analysis or **best-case** analysis?

16 of 40

Three Notions of Asymptotic Bounds

We may consider three kinds of *asymptotic bounds* for the *running time* of an algorithm:

- Asymptotic **upper** bound [O]
- Asymptotic lower bound [Ω]
- Asymptotic tight bound [Θ]

18 of 40

What is Asymptotic Analysis?

Asymptotic analysis

- Is a method of describing *behaviour in the limit*:
 - How the *running time* of the algorithm under analysis changes as the *input size* changes without bound
 - e.g., contrast $RT_1(n) = n$ with $RT_2(n) = n^2$
- Allows us to compare the *relative* performance of alternative algorithms:
 - For large enough inputs, the *multiplicative constants* and *lower-order* terms of an exact running time can be disregarded.
 - e.g., $RT_1(n) = 3n^2 + 7n + 18$ and $RT_2(n) = 100n^2 + 3n - 100$ are considered **equally efficient**, *asymptotically*.
 - e.g., $RT_1(n) = n^3 + 7n + 18$ is considered **less efficient** than $RT_2(n) = 100n^2 + 100n + 2000$, *asymptotically*.

17 of 40

Asymptotic Upper Bound: Definition

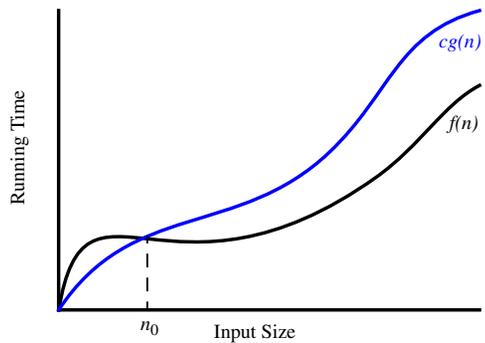
- Let $f(n)$ and $g(n)$ be functions mapping positive integers (input size) to positive real numbers (running time).
 - $f(n)$ characterizes the running time of some algorithm.
 - $O(g(n))$ denotes *a collection of* functions.
- $O(g(n))$ consists of *all* functions that can be upper bounded by $g(n)$, starting at some point, using some constant factor.
- $f(n) \in O(g(n))$ if there are:
 - A real *constant* $c > 0$
 - An integer *constant* $n_0 \geq 1$
 such that:

$$f(n) \leq c \cdot g(n) \quad \text{for } n \geq n_0$$

- For each member function $f(n)$ in $O(g(n))$, we say that:
 - $f(n) \in O(g(n))$ [f(n) is a member of "big-Oh of g(n)"]
 - $f(n)$ **is** $O(g(n))$ [f(n) is "big-Oh of g(n)"]
 - $f(n)$ **is order of** $g(n)$

19 of 40

Asymptotic Upper Bound: Visualization



From n_0 , $f(n)$ is upper bounded by $c \cdot g(n)$, so $f(n)$ is $O(g(n))$.

Asymptotic Upper Bound: Example (2)

Prove: The function $f(n) = 5n^4 + 3n^3 + 2n^2 + 4n + 1$ is $O(n^4)$.

Strategy: Choose a real constant $c > 0$ and an integer constant $n_0 \geq 1$, such that for every integer $n \geq n_0$:

$$5n^4 + 3n^3 + 2n^2 + 4n + 1 \leq c \cdot n^4$$

$$f(1) = 5 + 3 + 2 + 4 + 1 = 15$$

Choose $c = 15$ and $n_0 = 1$!

Asymptotic Upper Bound: Example (1)

Prove: The function $8n + 5$ is $O(n)$.

Strategy: Choose a real constant $c > 0$ and an integer constant $n_0 \geq 1$, such that for every integer $n \geq n_0$:

$$8n + 5 \leq c \cdot n$$

Can we choose $c = 9$? What should the corresponding n_0 be?

n	8n + 5	9n
1	13	9
2	21	18
3	29	27
4	37	36
5	45	45
6	53	54

...

Therefore, we prove it by choosing $c = 9$ and $n_0 = 5$.

We may also prove it by choosing $c = 13$ and $n_0 = 1$. Why?

Asymptotic Upper Bound: Proposition (1)

If $f(n)$ is a polynomial of degree d , i.e.,

$$f(n) = a_0 \cdot n^0 + a_1 \cdot n^1 + \dots + a_d \cdot n^d$$

and a_0, a_1, \dots, a_d are integers (i.e., negative, zero, or positive),

then $f(n)$ is $O(n^d)$.

- We prove by choosing

$$\begin{aligned} c &= |a_0| + |a_1| + \dots + |a_d| \\ n_0 &= 1 \end{aligned}$$

- We know that for $n \geq 1$: $n^0 \leq n^1 \leq n^2 \leq \dots \leq n^d$
- Upper-bound effect starts when $n_0 = 1$? $[f(1) \leq 1^d]$

$$a_0 \cdot 1^0 + a_1 \cdot 1^1 + \dots + a_d \cdot 1^d \leq |a_0| \cdot 1^d + |a_1| \cdot 1^d + \dots + |a_d| \cdot 1^d$$

- Upper-bound effect holds? $[f(n) \leq n^d]$

$$a_0 \cdot n^0 + a_1 \cdot n^1 + \dots + a_d \cdot n^d \leq |a_0| \cdot n^d + |a_1| \cdot n^d + \dots + |a_d| \cdot n^d$$

Asymptotic Upper Bound: Proposition (2)



$$O(n^0) \subset O(n^1) \subset O(n^2) \subset \dots$$

If a function $f(n)$ is *upper bounded* by another function $g(n)$ of degree d , $d \geq 0$, then $f(n)$ is also upper bounded by all other functions of a *strictly higher degree* (i.e., $d + 1$, $d + 2$, etc.).

e.g., Family of $O(n)$ contains:

$n^0, 2n^0, 3n^0, \dots$ [functions with degree 0]
 $n, 2n, 3n, \dots$ [functions with degree 1]

e.g., Family of $O(n^2)$ contains:

$n^0, 2n^0, 3n^0, \dots$ [functions with degree 0]
 $n, 2n, 3n, \dots$ [functions with degree 1]
 $n^2, 2n^2, 3n^2, \dots$ [functions with degree 2]

Using Asymptotic Upper Bound Accurately



- Use the big-Oh notation to characterize a function (of an algorithm's running time) *as closely as possible*.

For example, say $f(n) = 4n^3 + 3n^2 + 5$:

- Recall: $O(n^3) \subset O(n^4) \subset O(n^5) \subset \dots$
- It is the **most accurate** to say that $f(n)$ is $O(n^3)$.
- It is **true**, but not very useful, to say that $f(n)$ is $O(n^4)$ and that $f(n)$ is $O(n^5)$.
- It is **false** to say that $f(n)$ is $O(n^2)$, $O(n)$, or $O(1)$.
- Do not include *constant factors* and *lower-order terms* in the big-Oh notation.

For example, say $f(n) = 2n^2$ is $O(n^2)$, do not say $f(n)$ is $O(4n^2 + 6n + 9)$.

Asymptotic Upper Bound: More Examples



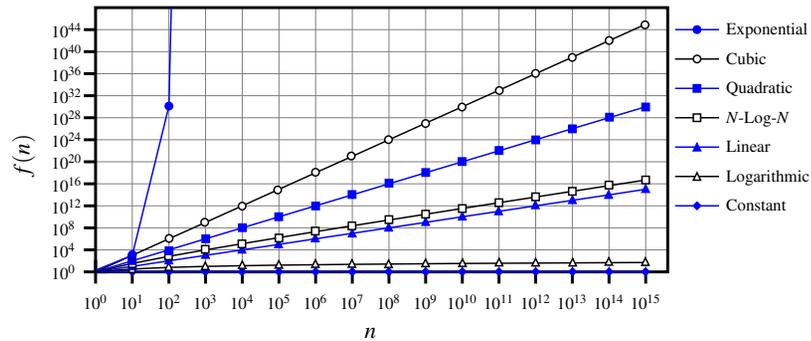
- $5n^2 + 3n \cdot \log n + 2n + 5$ is $O(n^2)$ [$c = 15, n_0 = 1$]
- $20n^3 + 10n \cdot \log n + 5$ is $O(n^3)$ [$c = 35, n_0 = 1$]
- $3 \cdot \log n + 2$ is $O(\log n)$ [$c = 5, n_0 = 2$]
- Why can't n_0 be 1?
 - Choosing $n_0 = 1$ means $\Rightarrow f(\boxed{1})$ **is** upper-bounded by $c \cdot \log \boxed{1}$:
 - We have $f(\boxed{1}) = 3 \cdot \log 1 + 2$, which is 2.
 - We have $c \cdot \log \boxed{1}$, which is 0.
- $\Rightarrow f(\boxed{1})$ **is not** upper-bounded by $c \cdot \log \boxed{1}$ [Contradiction!]
- 2^{n+2} is $O(2^n)$ [$c = 4, n_0 = 1$]
- $2n + 100 \cdot \log n$ is $O(n)$ [$c = 102, n_0 = 1$]

Classes of Functions



upper bound	class	cost
$O(1)$	constant	<i>cheapest</i>
$O(\log(n))$	logarithmic	
$O(n)$	linear	
$O(n \cdot \log(n))$	"n-log-n"	
$O(n^2)$	quadratic	
$O(n^3)$	cubic	
$O(n^k), k \geq 1$	polynomial	
$O(a^n), a > 1$	exponential	<i>most expensive</i>

Rates of Growth: Comparison



28 of 40

Upper Bound of Algorithm: Example (2)

```
1 findMax (int[] a, int n) {
2   currentMax = a[0];
3   for (int i = 1; i < n; ) {
4     if (a[i] > currentMax) {
5       currentMax = a[i]; }
6     i ++ }
7   return currentMax; }
```

- From last lecture, we calculated that the # of primitive operations is $7n - 2$.
- Therefore, the running time is $O(n)$.
- That is, this is a *linear-time* algorithm.

30 of 40

Upper Bound of Algorithm: Example (1)

```
1 maxOf (int x, int y) {
2   int max = x;
3   if (y > x) {
4     max = y;
5   }
6   return max;
7 }
```

- # of primitive operations: 4
2 assignments + 1 comparison + 1 return = 4
- Therefore, the running time is $O(1)$.
- That is, this is a *constant-time* algorithm.

29 of 40

Upper Bound of Algorithm: Example (3)

```
1 containsDuplicate (int[] a, int n) {
2   for (int i = 0; i < n; ) {
3     for (int j = 0; j < n; ) {
4       if (i != j && a[i] == a[j]) {
5         return true; }
6       j ++; }
7     i ++; }
8   return false; }
```

- Worst case is when we reach Line 8.
- # of primitive operations $\approx c_1 + n \cdot n \cdot c_2$, where c_1 and c_2 are some constants.
- Therefore, the running time is $O(n^2)$.
- That is, this is a *quadratic* algorithm.

31 of 40

Upper Bound of Algorithm: Example (4)



```
1 sumMaxAndCrossProducts (int[] a, int n) {
2   int max = a[0];
3   for(int i = 1; i < n; i++) {
4     if (a[i] > max) { max = a[i]; }
5   }
6   int sum = max;
7   for (int j = 0; j < n; j++) {
8     for (int k = 0; k < n; k++) {
9       sum += a[j] * a[k]; } }
10  return sum; }
```

- # of primitive operations $\approx (c_1 \cdot n + c_2) + (c_3 \cdot n \cdot n + c_4)$, where c_1, c_2, c_3 , and c_4 are some constants.
- Therefore, the running time is $O(n + n^2) = O(n^2)$.
- That is, this is a *quadratic* algorithm.

32 of 40

Upper Bound of Algorithm: Example (5)



```
1 triangularSum (int[] a, int n) {
2   int sum = 0;
3   for (int i = 0; i < n; i++) {
4     for (int j = i; j < n; j++) {
5       sum += a[j]; } }
6   return sum; }
```

- # of primitive operations $\approx n + (n - 1) + \dots + 2 + 1 = \frac{n \cdot (n+1)}{2}$
- Therefore, the running time is $O(\frac{n^2+n}{2}) = O(n^2)$.
- That is, this is a *quadratic* algorithm.

33 of 40

Basic Data Structure: Arrays



- An array is a sequence of indexed elements.
- *Size* of an array is **fixed** at the time of its construction.
- Supported *operations* on an array:
 - *Accessing*: e.g., `int max = a[0];`
Time Complexity: $O(1)$ [constant operation]
 - *Updating*: e.g., `a[i] = a[i + 1];`
Time Complexity: $O(1)$ [constant operation]
 - *Inserting/Removing*:

```
String[] insertAt(String[] a, int n, String e, int i)
String[] result = new String[n + 1];
for(int j = 0; j <= i - 1; j++){ result[j] = a[j]; }
result[i] = e;
for(int j = i + 1; j <= n - 1; j++){ result[j] = a[j-1]; }
return result;
```

Time Complexity: $O(n)$ [linear operation]

34 of 40

Array Case Study: Comparing Two Sorting Strategies



- Problem:
 - Input:** An array a of n numbers $\langle a_1, a_2, \dots, a_n \rangle$
 - Output:** A permutation (reordering) $\langle a'_1, a'_2, \dots, a'_n \rangle$ of the input sequence such that $a'_1 \leq a'_2 \leq \dots \leq a'_n$
- We propose two *alternative implementation strategies* for solving this problem.
- At the end, we want to know which one to choose, based on *time complexity*.

35 of 40

Sorting: Strategy 1 – Selection Sort



- Maintain a (initially empty) *sorted portion* of array *a*.
- From left to right in array *a*, select and insert *the minimum element* to the end of this sorted portion, so it remains sorted.

```

1 selectionSort(int[] a, int n)
2   for (int i = 0; i <= (n - 2); i++)
3     int minIndex = i;
4     for (int j = i; j <= (n - 1); j++)
5       if (a[j] < a[minIndex]) { minIndex = j; }
6     int temp = a[i];
7     a[i] = a[minIndex];
8     a[minIndex] = temp;

```

- How many times does the body of *for loop* (Line 4) run?
 - Running time? $[O(n^2)]$
- $$\underbrace{n}_{\text{find } \{a[0], \dots, a[n-1]\}} + \underbrace{(n-1)}_{\text{find } \{a[1], \dots, a[n-1]\}} + \dots + \underbrace{2}_{\text{find } \{a[n-2], a[n-1]\}}$$
- So selection sort is a *quadratic-time algorithm*.

36 of 40

Sorting: Alternative Implementations?



- In the Java implementations for *selection* sort and *insertion* sort, we maintain the “sorted portion” from the *left* end.
 - For *selection* sort, we select the *minimum* element from the “unsorted portion” and insert it to the *end* in the “sorted portion”.
- For *insertion* sort, we choose the *left-most* element from the “unsorted portion” and insert it at the “*right spot*” in the “sorted portion”.
- **Question:** Can we modify the Java implementations, so that the “sorted portion” is maintained and grown from the *right* end instead?

38 of 40

Sorting: Strategy 2 – Insertion Sort



- Maintain a (initially empty) *sorted portion* of array *a*.
- From left to right in array *a*, insert *one element at a time* into the “right” spot in this sorted portion, so it remains sorted.

```

1 insertionSort(int[] a, int n)
2   for (int i = 1; i < n; i++)
3     int current = a[i];
4     int j = i;
5     while (j > 0 && a[j - 1] > current)
6       a[j] = a[j - 1];
7       j--;
8     a[j] = current;

```

- *while loop* (L5) exits when? $j \leq 0$ or $a[j - 1] \leq \text{current}$
 - Running time? $[O(n^2)]$
- $$O(\underbrace{1}_{\text{insert into } \{a[0]\}} + \underbrace{2}_{\text{insert into } \{a[0], a[1]\}} + \dots + \underbrace{(n-1)}_{\text{insert into } \{a[0], \dots, a[n-2]\}})$$
- So insertion sort is a *quadratic-time algorithm*.

37 of 40

Comparing Insertion & Selection Sorts



- *Asymptotically*, running times of selection sort and insertion sort are both $O(n^2)$.
- We will later see that there exist better algorithms that can perform better than quadratic: $O(n \cdot \log n)$.

39 of 40

Index (1)

Algorithm and Data Structure
Measuring “Goodness” of an Algorithm
Measuring Efficiency of an Algorithm
Measure Running Time via Experiments
Example Experiment
Example Experiment: Detailed Statistics
Example Experiment: Visualization
Experimental Analysis: Challenges
Moving Beyond Experimental Analysis
Counting Primitive Operations
Example: Counting Primitive Operations
From Absolute RT to Relative RT
Example: Approx. # of Primitive Operations

40 of 40

Index (2)

Approximating Running Time
as a Function of Input Size
Focusing on the Worst-Case Input
What is Asymptotic Analysis?
Three Notions of Asymptotic Bounds
Asymptotic Upper Bound: Definition
Asymptotic Upper Bound: Visualization
Asymptotic Upper Bound: Example (1)
Asymptotic Upper Bound: Example (2)
Asymptotic Upper Bound: Proposition (1)
Asymptotic Upper Bound: Proposition (2)
Asymptotic Upper Bound: More Examples
Using Asymptotic Upper Bound Accurately
Classes of Functions

41 of 40

Index (3)

Rates of Growth: Comparison
Upper Bound of Algorithm: Example (1)
Upper Bound of Algorithm: Example (2)
Upper Bound of Algorithm: Example (3)
Upper Bound of Algorithm: Example (4)
Upper Bound of Algorithm: Example (5)
Basic Data Structure: Arrays
Array Case Study:
Comparing Two Sorting Strategies
Sorting: Strategy 1 – Selection Sort
Sorting: Strategy 2 – Insertion Sort
Sorting: Alternative Implementations?
Comparing Insertion & Selection Sorts

42 of 40

Aggregation and Composition

Call by Value (1)

- Consider the general form of a call to some **mutator method** `m1`, with **context object** `s` and **argument value** `arg`:

```
class Supplier {
    void m1(T par) {
        /* manipulate par */
    }
}
```

```
class Client {
    Supplier s = new Supplier();
    T arg = ...;
    s.m1(arg)
}
```

- To execute `s.m1(arg)`, an implicit `par := arg` is done.
⇒ A **copy** of value stored in `arg` is passed for the method call.
- What can the type `T` be? [Primitive or Reference]
 - `T` is primitive type (e.g., int, char, boolean, etc.):
Call by Value: Copy of `arg`'s **value** (e.g., 2, 'j') is passed.
 - `T` is reference type (e.g., String, Point, Person, etc.):
Call by Value: Copy of `arg`'s **stored reference/address** (e.g., Point@5cb0d902) is passed.

2 of 31

Call by Value (2.2.1)

```
public class Util {
    void reassignInt(int j) {
        j = j + 1; }
    void reassignRef(Point q) {
        Point np = new Point(6, 8);
        q = np; }
    void changeViaRef(Point q) {
        q.moveHorizontally(3);
        q.moveVertically(4); } }
}
```

```
1 @Test
2 public void testCallByVal() {
3     Util u = new Util();
4     int i = 10;
5     assertTrue(i == 10);
6     u.reassignInt(i);
7     assertTrue(i == 10);
8 }
```

- Before** the mutator call at L6, **primitive** variable `i` stores 10.
- When** executing the mutator call at L6, due to **call by value**, a copy of variable `i` is made.
⇒ The assignment `i = i + 1` is only effective on this copy, not the original variable `i` itself.
- ∴ **After** the mutator call at L6, variable `i` still stores 10.

4 of 31

Call by Value (2.1)

For illustration, let's assume the following variant of the `Point` class:

```
class Point {
    int x;
    int y;
    Point(int x, int y) {
        this.x = x;
        this.y = y;
    }
    void moveVertically(int y) {
        this.y += y;
    }
    void moveHorizontally(int x) {
        this.x += x;
    }
}
```

3 of 31

Call by Value (2.2.2)



5 of 31

Call by Value (2.3.1)

```

1  @Test
2  public void testCallByRef_1() {
3      Util u = new Util();
4      Point p = new Point(3, 4);
5      Point refOfPBefore = p;
6      u.reassignRef(p);
7      assertTrue(p==refOfPBefore);
8      assertTrue(p.x==3 && p.y==4);
9  }
    
```

```

public class Util {
    void reassignInt(int j) {
        j = j + 1; }
    void reassignRef(Point q) {
        Point np = new Point(6, 8);
        q = np; }
    void changeViaRef(Point q) {
        q.moveHorizontally(3);
        q.moveVertically(4); } }
    
```

- **Before** the mutator call at L6, **reference** variable `p` stores the **address** of some `Point` object (whose `x` is 3 and `y` is 4).
- **When** executing the mutator call at L6, due to **call by value**, a **copy of address** stored in `p` is made.
 ⇒ The assignment `p = np` is only effective on this copy, not the original variable `p` itself.
- ∴ **After** the mutator call at L6, variable `p` still stores the original address (i.e., same as `refOfPBefore`).

6 of 31

Call by Value (2.4.1)

```

1  @Test
2  public void testCallByRef_2() {
3      Util u = new Util();
4      Point p = new Point(3, 4);
5      Point refOfPBefore = p;
6      u.changeViaRef(p);
7      assertTrue(p==refOfPBefore);
8      assertTrue(p.x==6 && p.y==8);
9  }
    
```

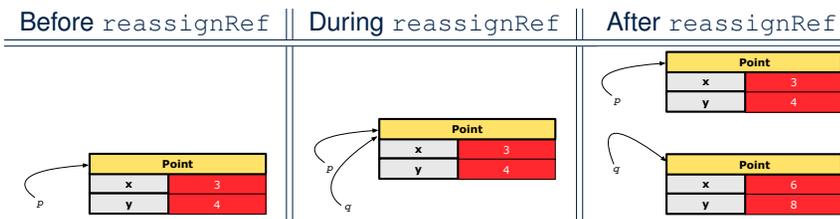
```

public class Util {
    void reassignInt(int j) {
        j = j + 1; }
    void reassignRef(Point q) {
        Point np = new Point(6, 8);
        q = np; }
    void changeViaRef(Point q) {
        q.moveHorizontally(3);
        q.moveVertically(4); } }
    
```

- **Before** the mutator call at L6, **reference** variable `p` stores the **address** of some `Point` object (whose `x` is 3 and `y` is 4).
- **When** executing the mutator call at L6, due to **call by value**, a **copy of address** stored in `p` is made. [Alias: `p` and `q` store same address.]
 ⇒ Calls to `q.moveHorizontally` and `q.moveVertically` are effective on both `p` and `q`.
- ∴ **After** the mutator call at L6, variable `p` still stores the original address (i.e., same as `refOfPBefore`), but its `x` and `y` have been modified via `q`.

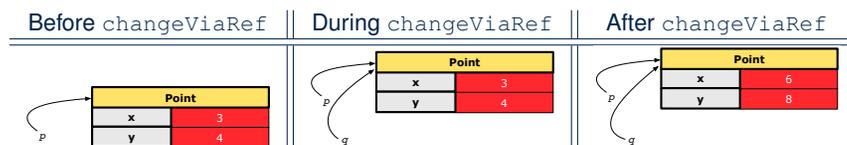
8 of 31

Call by Value (2.3.2)



7 of 31

Call by Value (2.4.2)



9 of 31

Aggregation vs. Composition: Terminology



Container object: an object that contains others.

Containee object: an object that is contained within another.

- e.g., Each course has a faculty member as its instructor.
 - Container:** Course **Containee:** Faculty.
- e.g., Each student is registered in a list of courses; Each faculty member teaches a list of courses.
 - Container:** Student, Faculty **Containees:** Course.
 - e.g., eeecs2030 taken by jim (student) and taught by tom (faculty).
 - ⇒ **Containees** may be **shared** by different instances of **containers**.
 - e.g., When EECS2030 is finished, jim and jackie still exist!
 - ⇒ **Containees** may exist **independently** without their **containers**.
- e.g., In a file system, each directory contains a list of files.
 - Container:** Directory **Containees:** File.
 - e.g., Each file has exactly one parent directory.
 - ⇒ A **containee** may be **owned** by only one **container**.
 - e.g., Deleting a directory also deletes the files it contains.
 - ⇒ **Containees** may **co-exist** with their **containers**.

Aggregation: Independent Containees Shared by Containers (1.2)



```
@Test
public void testAggregation1() {
    Course eeecs2030 = new Course("Advanced OOP");
    Course eeecs3311 = new Course("Software Design");
    Faculty prof = new Faculty("Jackie");
    eeecs2030.setProf(prof);
    eeecs3311.setProf(prof);
    assertTrue(eeecs2030.getProf() == eeecs3311.getProf());
    /* aliasing */
    prof.setName("Jeff");
    assertTrue(eeecs2030.getProf() == eeecs3311.getProf());
    assertTrue(eeecs2030.getProf().getName().equals("Jeff"));

    Faculty prof2 = new Faculty("Jonathan");
    eeecs3311.setProf(prof2);
    assertTrue(eeecs2030.getProf() != eeecs3311.getProf());
    assertTrue(eeecs2030.getProf().getName().equals("Jeff"));
    assertTrue(eeecs3311.getProf().getName().equals("Jonathan"));
}
```

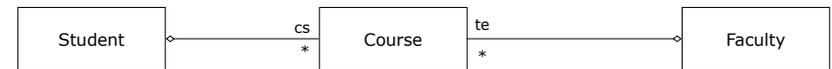
Aggregation: Independent Containees Shared by Containers (1.1)



```
class Course {
    String title;
    Faculty prof;
    Course(String title) {
        this.title = title;
    }
    void setProf(Faculty prof) {
        this.prof = prof;
    }
    Faculty getProf() {
        return this.prof;
    }
}
```

```
class Faculty {
    String name;
    Faculty(String name) {
        this.name = name;
    }
    void setName(String name) {
        this.name = name;
    }
    String getName() {
        return this.name;
    }
}
```

Aggregation: Independent Containees Shared by Containers (2.1)



```
class Student {
    String id; ArrayList<Course> cs; /* courses */
    Student(String id) { this.id = id; cs = new ArrayList<>(); }
    void addCourse(Course c) { cs.add(c); }
    ArrayList<Course> getCS() { return cs; }
}
```

```
class Course { String title; }
```

```
class Faculty {
    String name; ArrayList<Course> te; /* teaching */
    Faculty(String name) { this.name = name; te = new ArrayList<>(); }
    void addTeaching(Course c) { te.add(c); }
    ArrayList<Course> getTE() { return te; }
}
```

Aggregation: Independent Containees Shared by Containers (2.2)

```
@Test
public void testAggregation2() {
    Faculty p = new Faculty("Jackie");
    Student s = new Student("Jim");
    Course eecs2030 = new Course("Advanced OOP");
    Course eecs3311 = new Course("Software Design");
    eecs2030.setProf(p);
    eecs3311.setProf(p);
    p.addTeaching(eecs2030);
    p.addTeaching(eecs3311);
    s.addCourse(eecs2030);
    s.addCourse(eecs3311);

    assertTrue(eecs2030.getProf() == s.getCS().get(0).getProf());
    assertTrue(s.getCS().get(0).getProf() == s.getCS().get(1).getProf());
    assertTrue(eecs3311 == s.getCS().get(1));
    assertTrue(s.getCS().get(1) == p.getTE().get(1));
}
```

The Dot Notation (3.2)

```
class Student {
    String id;
    ArrayList<Course> cs;
}
```

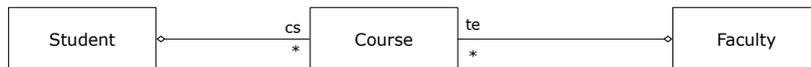
```
class Course {
    String title;
    Faculty prof;
}
```

```
class Faculty {
    String name;
    ArrayList<Course> te;
}
```

```
class Student {
    ... /* attributes */
    /* Get the student's id */
    String getID() { return this.id; }
    /* Get the title of the ith course */
    String getCourseTitle(int i) {
        return this.cs.get(i).title;
    }
    /* Get the instructor's name of the ith course */
    String getInstructorName(int i) {
        return this.cs.get(i).prof.name;
    }
}
```

The Dot Notation (3.1)

In real life, the relationships among classes are sophisticated.



```
class Student {
    String id;
    ArrayList<Course> cs;
}
```

```
class Course {
    String title;
    Faculty prof;
}
```

```
class Faculty {
    String name;
    ArrayList<Course> te;
}
```

Aggregation links between classes constrain how you can **navigate** among these classes.

e.g., In the context of class Student:

- Writing **cs** denotes the list of registered courses.
- Writing **cs[i]** (where **i** is a valid index) navigates to the class Course, which changes the context to class Course.

The Dot Notation (3.3)

```
class Student {
    String id;
    ArrayList<Course> cs;
}
```

```
class Course {
    String title;
    Faculty prof;
}
```

```
class Faculty {
    String name;
    ArrayList<Course> te;
}
```

```
class Course {
    ... /* attributes */
    /* Get the course's title */
    String getTitle() { return this.title; }
    /* Get the instructor's name */
    String getInstructorName() {
        return this.prof.name;
    }
    /* Get title of ith teaching course of the instructor */
    String getCourseTitleOfInstructor(int i) {
        return this.prof.te.get(i).title;
    }
}
```

The Dot Notation (3.4)

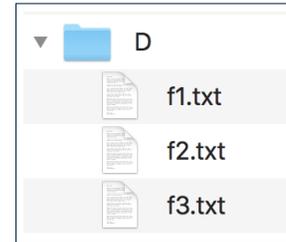
```
class Student {
    String id;
    ArrayList<Course> cs;
}
```

```
class Course {
    String title;
    Faculty prof;
}
```

```
class Faculty {
    String name;
    ArrayList<Course> te;
}
```

```
class Faculty {
    ... /* attributes */
    /* Get the instructor's name */
    String getName() {
        return this.name;
    }
    /* Get the title of ith teaching course */
    String getCourseTitle(int i) {
        return this.te.get(i).title;
    }
}
```

Composition: Dependent Containees Owned by Containers (1.2.1)



```
1 @Test
2 public void testComposition() {
3     Directory d1 = new Directory("D");
4     d1.addFile("f1.txt");
5     d1.addFile("f2.txt");
6     d1.addFile("f3.txt");
7     assertTrue(
8         d1.files[0].name.equals("f1.txt"));
9 }
```

- **L4:** 1st File object is created and **owned exclusively** by d1. No other directories are sharing this File object with d1.
- **L5:** 2nd File object is created and **owned exclusively** by d1. No other directories are sharing this File object with d1.
- **L6:** 3rd File object is created and **owned exclusively** by d1. No other directories are sharing this File object with d1.

Composition: Dependent Containees Owned by Containers (1.1)



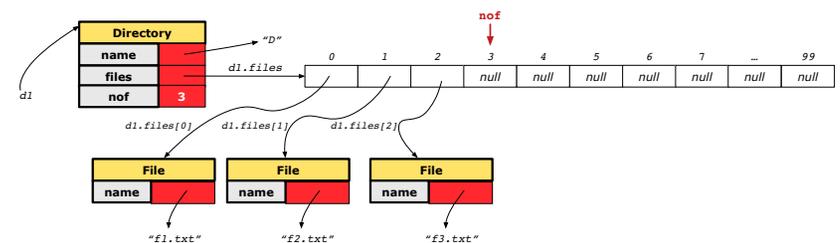
Assumption: Files are not shared among directories.

```
class File {
    String name;
    File(String name) {
        this.name = name;
    }
}
```

```
class Directory {
    String name;
    File[] files;
    int nof; /* num of files */
    Directory(String name) {
        this.name = name;
        files = new File[100];
    }
    void addFile(String fileName) {
        files[nof] = new File(fileName);
        nof++;
    }
}
```

Composition: Dependent Containees Owned by Containers (1.2.2)

Right before test method `testComposition` terminates:



Composition: Dependent Containees Owned by Containers (1.3)



Problem: Implement a **copy constructor** for Directory.

A **copy constructor** is a constructor which initializes attributes from the argument object other.

```
class Directory {
    Directory(Directory other) {
        /* Initialize attributes via attributes of 'other'. */
    }
}
```

Hints:

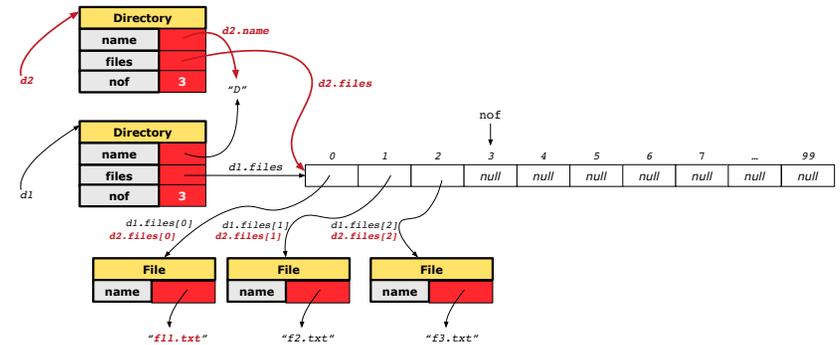
- The implementation should be consistent with the effect of copying and pasting a directory.
- Separate copies of files are created.

22 of 31

Composition: Dependent Containees Owned by Containers (1.4.2)



Right before test method testShallowCopyConstructor terminates:



24 of 31

Composition: Dependent Containees Owned by Containers (1.4.1)



Version 1: **Shallow Copy** by copying all attributes using =.

```
class Directory {
    Directory(Directory other) {
        /* value copying for primitive type */
        nof = other.nof;
        /* address copying for reference type */
        name = other.name; files = other.files; } }
}
```

Is a shallow copy satisfactory to support composition?

i.e., Does it still forbid sharing to occur?

[NO]

```
@Test
void testShallowCopyConstructor() {
    Directory d1 = new Directory("D");
    d1.addFile("f1.txt"); d1.addFile("f2.txt"); d1.addFile("f3.txt");
    Directory d2 = new Directory(d1);
    assertTrue(d1.files == d2.files); /* violation of composition */
    d2.files[0].changeName("f11.txt");
    assertFalse(d1.files[0].name.equals("f1.txt")); }
}
```

23 of 31

Composition: Dependent Containees Owned by Containers (1.5.1)



Version 2: a **Deep Copy**

```
class File {
    File(File other) {
        this.name =
            new String(other.name);
    }
}
```

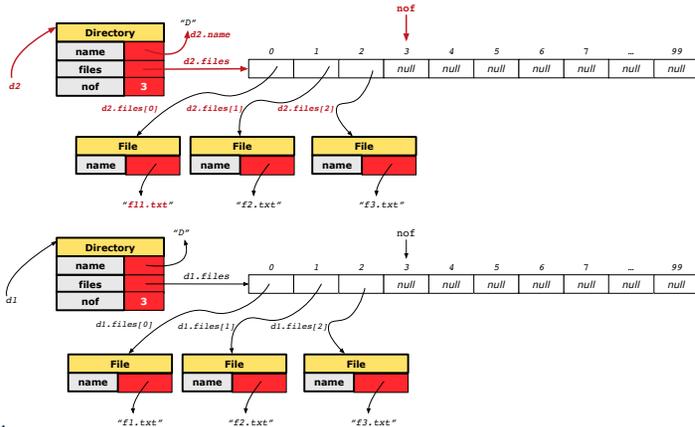
```
class Directory {
    Directory(String name) {
        this.name = new String(name);
        files = new File[100]; }
    Directory(Directory other) {
        this (other.name);
        for(int i = 0; i < nof; i++) {
            File src = other.files[i];
            File nf = new File(src);
            this.addFile(nf); } }
    void addFile(File f) { ... } }
}
```

```
@Test
void testDeepCopyConstructor() {
    Directory d1 = new Directory("D");
    d1.addFile("f1.txt"); d1.addFile("f2.txt"); d1.addFile("f3.txt");
    Directory d2 = new Directory(d1);
    assertTrue(d1.files != d2.files); /* composition preserved */
    d2.files[0].changeName("f11.txt");
    assertTrue(d1.files[0].name.equals("f1.txt")); }
}
```

25 of 31

Composition: Dependent Containees Owned by Containers (1.5.2)

Right before test method `testDeepCopyConstructor` terminates:



26 of 31

Composition: Dependent Containees Owned by Containers (1.6)

Exercise: Implement the accessor in class `Directory`

```
class Directory {
    File[] files;
    int nof;
    File[] getFiles() {
        /* Your Task */
    }
}
```

so that it **preserves composition**, i.e., does not allow references of files to be shared.

26 of 31

Composition: Dependent Containees Owned by Containers (1.5.3)

Q: Composition Violated?

```
class File {
    File(File other) {
        this.name =
            new String(other.name);
    }
}
```

```
class Directory {
    Directory(String name) {
        this.name = new String(name);
        files = new File[100];
    }
    Directory(Directory other) {
        this(other.name);
        for(int i = 0; i < nof; i++) {
            File src = other.files[i];
            this.addFile(src);
        }
    }
    void addFile(File f) { ... }
}
```

```
@Test
void testDeepCopyConstructor() {
    Directory d1 = new Directory("D");
    d1.addFile("f1.txt"); d1.addFile("f2.txt"); d1.addFile("f3.txt");
    Directory d2 = new Directory(d1);
    assertTrue(d1.files != d2.files); /* composition preserved */
    d2.files[0].changeName("f11.txt");
    assertTrue(d1.files[0] == d2.files[0]); /* composition violated! */
}
```

27 of 31

Aggregation vs. Composition (1)

Terminology:

- **Container** object: an object that contains others.
- **Containee** object: an object that is contained within another.

Aggregation :

- Containees (e.g., `Course`) may be **shared** among containers (e.g., `Student`, `Faculty`).
- Containees **exist independently** without their containers.
- When a container is destroyed, its containees still exist.

Composition :

- Containers (e.g, `Directory`, `Department`) **own** exclusive access to their containees (e.g., `File`, `Faculty`).
- Containees cannot exist without their containers.
- Destroying a container destroys its containees **cascadingly**.

29 of 31

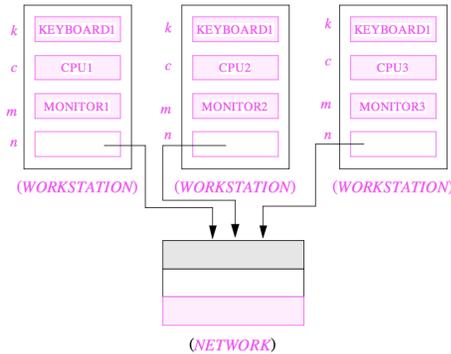
Aggregation vs. Composition (2)



Aggregations and *Compositions* may exist at the same time!

e.g., Consider a workstation:

- Each workstation owns CPU, monitor, keyboard. [*compositions*]
- All workstations share the same network. [*aggregations*]



30 of 31

Index (2)



Aggregation: Independent Containees Shared by Containers (2.2)

The Dot Notation (3.1)

The Dot Notation (3.2)

The Dot Notation (3.3)

The Dot Notation (3.4)

Composition: Dependent Containees Owned by Containers (1.1)

Composition: Dependent Containees Owned by Containers (1.2.1)

Composition: Dependent Containees Owned by Containers (1.2.2)

Composition: Dependent Containees Owned by Containers (1.3)

32 of 31

Index (1)



Call by Value (1)

Call by Value (2.1)

Call by Value (2.2.1)

Call by Value (2.2.2)

Call by Value (2.3.1)

Call by Value (2.3.2)

Call by Value (2.4.1)

Call by Value (2.4.2)

Aggregation vs. Composition: Terminology

Aggregation: Independent Containees

Shared by Containers (1.1)

Aggregation: Independent Containees

Shared by Containers (1.2)

Aggregation: Independent Containees

Shared by Containers (2.1)

31 of 31

Index (3)



Composition: Dependent Containees Owned by Containers (1.4.1)

Composition: Dependent Containees Owned by Containers (1.4.2)

Composition: Dependent Containees Owned by Containers (1.5.1)

Composition: Dependent Containees Owned by Containers (1.5.2)

Composition: Dependent Containees Owned by Containers (1.5.3)

Composition: Dependent Containees Owned by Containers (1.6)

Aggregation vs. Composition (1)

Aggregation vs. Composition (2)

33 of 31

Inheritance



EECS2030 B: Advanced
Object Oriented Programming
Fall 2018

CHEN-WEI WANG

No Inheritance: ResidentStudent Class



```
class ResidentStudent {
    String name;
    Course[] registeredCourses;
    int numberOfCourses;
    double premiumRate; /* there's a mutator method for this */
    ResidentStudent(String name) {
        this.name = name;
        registeredCourses = new Course[10];
    }
    void register(Course c) {
        registeredCourses[numberOfCourses] = c;
        numberOfCourses++;
    }
    double getTuition() {
        double tuition = 0;
        for(int i = 0; i < numberOfCourses; i++) {
            tuition += registeredCourses[i].fee;
        }
        return tuition * premiumRate;
    }
} 3 of 86
```

Why Inheritance: A Motivating Example



Problem: A *student management system* stores data about students. There are two kinds of university students: *resident* students and *non-resident* students. Both kinds of students have a *name* and a list of *registered courses*. Both kinds of students are restricted to *register* for no more than 10 courses. When *calculating the tuition* for a student, a base amount is first determined from the list of courses they are currently registered (each course has an associated fee). For a non-resident student, there is a *discount rate* applied to the base amount to waive the fee for on-campus accommodation. For a resident student, there is a *premium rate* applied to the base amount to account for the fee for on-campus accommodation and meals.

Tasks: Write Java classes that satisfy the above problem statement. At runtime, each type of student must be able to register a course and calculate their tuition fee.

No Inheritance: NonResidentStudent Class



```
class NonResidentStudent {
    String name;
    Course[] registeredCourses;
    int numberOfCourses;
    double discountRate; /* there's a mutator method for this */
    NonResidentStudent(String name) {
        this.name = name;
        registeredCourses = new Course[10];
    }
    void register(Course c) {
        registeredCourses[numberOfCourses] = c;
        numberOfCourses++;
    }
    double getTuition() {
        double tuition = 0;
        for(int i = 0; i < numberOfCourses; i++) {
            tuition += registeredCourses[i].fee;
        }
        return tuition * discountRate;
    }
} 4 of 86
```

No Inheritance: Testing Student Classes



```
class Course {
    String title;
    double fee;
    Course(String title, double fee) {
        this.title = title; this.fee = fee; }
}
```

```
class StudentTester {
    static void main(String[] args) {
        Course c1 = new Course("EECS2030", 500.00); /* title and fee */
        Course c2 = new Course("EECS3311", 500.00); /* title and fee */
        ResidentStudent jim = new ResidentStudent("J. Davis");
        jim.setPremiumRate(1.25);
        jim.register(c1); jim.register(c2);
        NonResidentStudent jeremy = new NonResidentStudent("J. Gibbons");
        jeremy.setDiscountRate(0.75);
        jeremy.register(c1); jeremy.register(c2);
        System.out.println("Jim pays " + jim.getTuition());
        System.out.println("Jeremy pays " + jeremy.getTuition());
    }
}
```

5 of 86

No Inheritance: Issues with the Student Classes



- Implementations for the two student classes seem to work. But can you see any potential problems with it?
- The code of the two student classes share a lot in common.
- **Duplicates of code make it hard to maintain your software!**
- This means that when there is a change of policy on the common part, we need modify *more than one places*.

6 of 86

No Inheritance: Maintainability of Code (1)



What if the way for registering a course changes?

e.g.,

```
void register(Course c) {
    if (numberOfCourses >= MAX_ALLOWANCE) {
        throw new IllegalArgumentException("Maximum allowance reached.");
    }
    else {
        registeredCourses[numberOfCourses] = c;
        numberOfCourses++;
    }
}
```

We need to change the register method in *both* student classes!

7 of 86

No Inheritance: Maintainability of Code (2)



What if the way for calculating the base tuition changes?

e.g.,

```
double getTuition() {
    double tuition = 0;
    for(int i = 0; i < numberOfCourses; i++) {
        tuition += registeredCourses[i].fee;
    }
    /* ... can be premiumRate or discountRate */
    return tuition * inflationRate * ...;
}
```

We need to change the getTuition method in *both* student classes.

8 of 86

No Inheritance: A Collection of Various Kinds of Students

How do you define a class StudentManagementSystem that contains a list of *resident* and *non-resident* students?

```
class StudentManagementSystem {
    ResidentStudent[] rss;
    NonResidentStudent[] nrss;
    int nors; /* number of resident students */
    int nonrs; /* number of non-resident students */
    void addRS (ResidentStudent rs){ rss[nors]=rs; nors++; }
    void addNRS (NonResidentStudent nrs){ nrss[nonrs]=nrs; nonrs++; }
    void registerAll (Course c) {
        for(int i = 0; i < nors; i ++){ rss[i].register(c); }
        for(int i = 0; i < nonrs; i ++){ nrss[i].register(c); }
    }
}
```

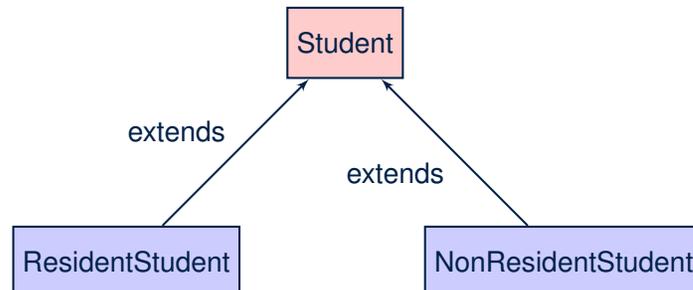
But what if we later on introduce *more kinds of students*?
Very *inconvenient* to handle each list of students *separately*!

a polymorphic collection of students

Inheritance: The Student Parent/Super Class

```
class Student {
    String name;
    Course[] registeredCourses;
    int numberOfCourses;
    Student (String name) {
        this.name = name;
        registeredCourses = new Course[10];
    }
    void register(Course c) {
        registeredCourses[numberOfCourses] = c;
        numberOfCourses ++;
    }
    double getTuition() {
        double tuition = 0;
        for(int i = 0; i < numberOfCourses; i ++){
            tuition += registeredCourses[i].fee;
        }
        return tuition; /* base amount only */
    }
}
```

Inheritance Architecture



Inheritance: The ResidentStudent Child/Sub Class

```
1 class ResidentStudent extends Student {
2     double premiumRate; /* there's a mutator method for this */
3     ResidentStudent (String name) { super (name); }
4     /* register method is inherited */
5     double getTuition() {
6         double base = super.getTuition();
7         return base * premiumRate;
8     }
9 }
```

- L1 declares that ResidentStudent inherits all attributes and methods (except constructors) from Student.
- There is no need to repeat the register method
- Use of *super* in L4 is as if calling Student (name)
- Use of *super* in L8 returns what getTuition() in Student returns.
- Use *super* to refer to attributes/methods defined in the super class:

`super.name`, `super.register(c)`.

Inheritance: The NonResidentStudent Child/Sub Class

```

1 class NonResidentStudent extends Student {
2     double discountRate; /* there's a mutator method for this */
3     NonResidentStudent (String name) { super(name); }
4     /* register method is inherited */
5     double getTuition() {
6         double base = super.getTuition();
7         return base * discountRate;
8     }
9 }

```

- L1 declares that NonResidentStudent inherits all attributes and methods (except constructors) from Student.
- There is no need to repeat the register method
- Use of *super* in L4 is as if calling Student(name)
- Use of *super* in L8 returns what getTuition() in Student returns.
- Use *super* to refer to attributes/methods defined in the super class:

```
super.name, super.register(c).
```

13 of 86

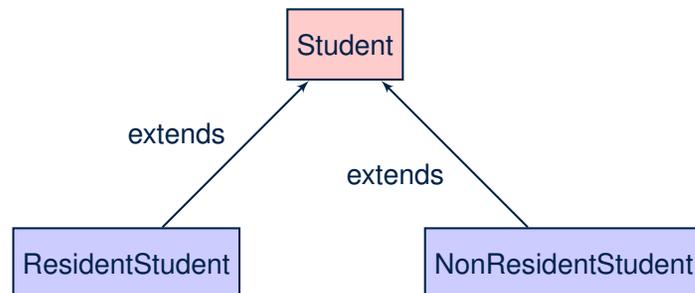
Using Inheritance for Code Reuse

Inheritance in Java allows you to:

- Define **common attributes and methods** in a separate class. e.g., the Student class
- Define an “extended” version of the class which:
 - **inherits** definitions of all attributes and methods e.g., name, registeredCourses, numberOfCourses e.g., register e.g., base amount calculation in getTuition
This means code reuse and elimination of code duplicates!
 - **defines new** attributes and methods if necessary e.g., setPremiumRate for ResidentStudent e.g., setDiscountRate for NonResidentStudent
 - **redefines/overrides** methods if necessary e.g., compounded tuition for ResidentStudent e.g., discounted tuition for NonResidentStudent

15 of 86

Inheritance Architecture Revisited



- The class that defines the common attributes and methods is called the **parent** or **super** class.
- Each “extended” class is called a **child** or **sub** class.

14 of 86

Visualizing Parent/Child Objects (1)

- A child class inherits **all** attributes from its parent class.
⇒ A child instance has **at least as many** attributes as an instance of its parent class.

Consider the following instantiations:

```

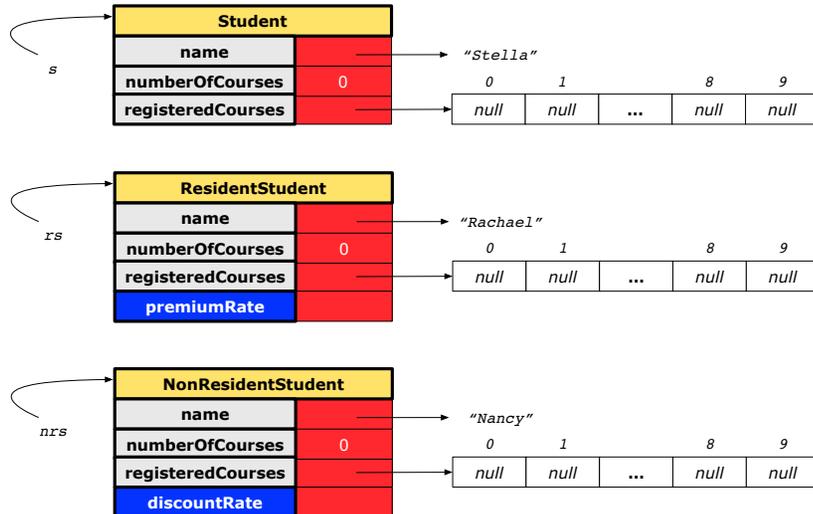
Student s = new Student("Stella");
ResidentStudent rs = new ResidentStudent("Rachael");
NonResidentStudent nrs = new NonResidentStudent("Nancy");

```

- How will these initial objects look like?

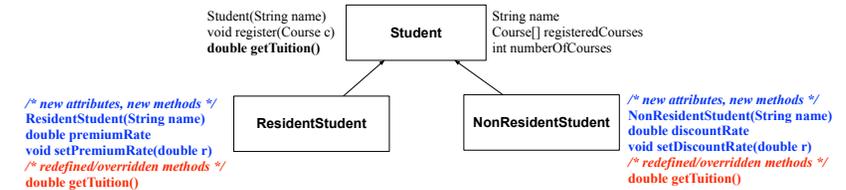
16 of 86

Visualizing Parent/Child Objects (2)



17 of 86

Inheritance Architecture: Static Types & Expectations



```

Student s = new Student("Stella");
ResidentStudent rs = new ResidentStudent("Rachael");
NonResidentStudent nrs = new NonResidentStudent("Nancy");
    
```

	name	rscs	noc	reg	getT	pr	setPR	dr	setDR
s.			✓					✗	
rs.			✓			✓			✗
nrs.			✓			✗			✓

19 of 86

Testing the Two Student Sub-Classes

```

class StudentTester {
    static void main(String[] args) {
        Course c1 = new Course("EECS2030", 500.00); /* title and fee */
        Course c2 = new Course("EECS3311", 500.00); /* title and fee */
        ResidentStudent jim = new ResidentStudent("J. Davis");
        jim.setPremiumRate(1.25);
        jim.register(c1); jim.register(c2);
        NonResidentStudent jeremy = new NonResidentStudent("J. Gibbons");
        jeremy.setDiscountRate(0.75);
        jeremy.register(c1); jeremy.register(c2);
        System.out.println("Jim pays " + jim.getTuition());
        System.out.println("Jeremy pays " + jeremy.getTuition());
    }
}
    
```

- The software can be used in exactly the same way as before (because we did not modify *method signatures*).
- But now the internal structure of code has been made *maintainable* using *inheritance*.

18 of 86

Polymorphism: Intuition (1)

```

1 Student s = new Student("Stella");
2 ResidentStudent rs = new ResidentStudent("Rachael");
3 rs.setPremiumRate(1.25);
4 s = rs; /* Is this valid? */
5 rs = s; /* Is this valid? */
    
```

- Which one of L4 and L5 is *valid*? Which one is *invalid*?
- Hints:
 - L1: What *kind* of address can *s* store? [Student]
∴ The context object *s* is *expected* to be used as:
 - s*.register(eecs2030) and *s*.getTuition()
 - L2: What *kind* of address can *rs* store? [ResidentStudent]
∴ The context object *rs* is *expected* to be used as:
 - rs*.register(eecs2030) and *rs*.getTuition()
 - rs*.setPremiumRate(1.50) [increase premium rate]

20 of 86

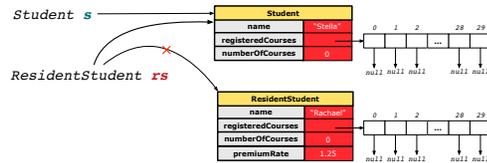
Polymorphism: Intuition (2)

```

1 Student s = new Student("Stella");
2 ResidentStudent rs = new ResidentStudent("Rachael");
3 rs.setPremiumRate(1.25);
4 s = rs; /* Is this valid? */
5 rs = s; /* Is this valid? */

```

- $rs = s$ (L5) should be *invalid*:



- Since rs is declared of type ResidentStudent, a subsequent call $rs.setPremiumRate(1.50)$ can be expected.
- rs is now pointing to a Student object.
- Then, what would happen to $rs.setPremiumRate(1.50)$?
CRASH $\because rs.premiumRate$ is *undefined*!!

21 of 86

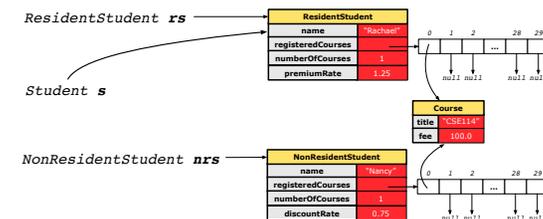
Dynamic Binding: Intuition (1)

```

1 Course eecs2030 = new Course("EECS2030", 100.0);
2 Student s;
3 ResidentStudent rs = new ResidentStudent("Rachael");
4 NonResidentStudent nrs = new NonResidentStudent("Nancy");
5 rs.setPremiumRate(1.25); rs.register(eecs2030);
6 nrs.setDiscountRate(0.75); nrs.register(eecs2030);
7 s = rs; System.out.println(s.getTuition()); /* output: 125.0 */
8 s = nrs; System.out.println(s.getTuition()); /* output: 75.0 */

```

After $s = rs$ (L7), s points to a ResidentStudent object.
 \Rightarrow Calling $s.getTuition()$ applies the premiumRate.



23 of 86

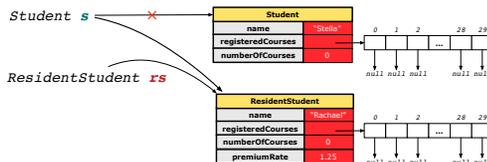
Polymorphism: Intuition (3)

```

1 Student s = new Student("Stella");
2 ResidentStudent rs = new ResidentStudent("Rachael");
3 rs.setPremiumRate(1.25);
4 s = rs; /* Is this valid? */
5 rs = s; /* Is this valid? */

```

- $s = rs$ (L4) should be *valid*:



- Since s is declared of type Student, a subsequent call $s.setPremiumRate(1.50)$ is *never* expected.
- s is now pointing to a ResidentStudent object.
- Then, what would happen to $s.getTuition()$?
OK $\because s.premiumRate$ is *never directly used*!!

22 of 86

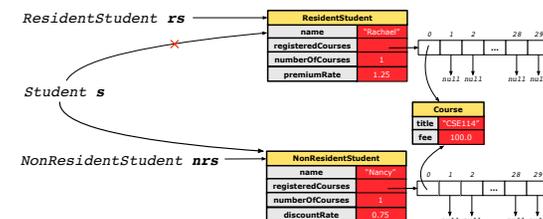
Dynamic Binding: Intuition (2)

```

1 Course eecs2030 = new Course("EECS2030", 100.0);
2 Student s;
3 ResidentStudent rs = new ResidentStudent("Rachael");
4 NonResidentStudent nrs = new NonResidentStudent("Nancy");
5 rs.setPremiumRate(1.25); rs.register(eecs2030);
6 nrs.setDiscountRate(0.75); nrs.register(eecs2030);
7 s = rs; System.out.println(s.getTuition()); /* output: 125.0 */
8 s = nrs; System.out.println(s.getTuition()); /* output: 75.0 */

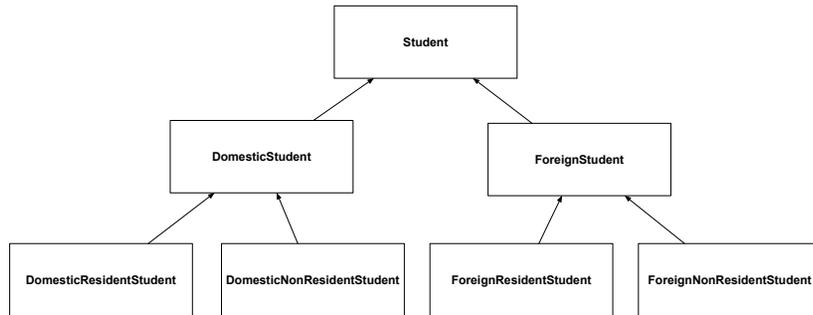
```

After $s = nrs$ (L8), s points to a NonResidentStudent object.
 \Rightarrow Calling $s.getTuition()$ applies the discountRate.



24 of 86

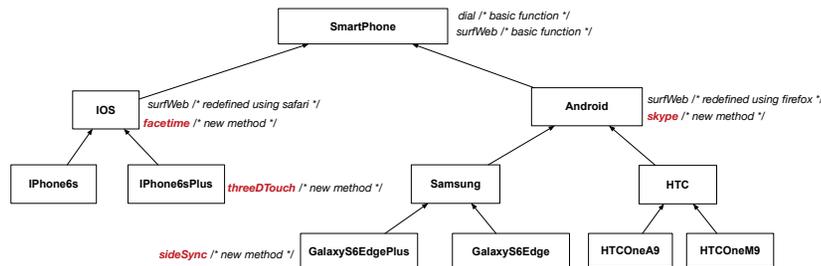
Multi-Level Inheritance Architecture



Inheritance Forms a Type Hierarchy

- A (data) **type** denotes a set of related *runtime values*.
 - Every *class* can be used as a type: the set of runtime *objects*.
- Use of *inheritance* creates a **hierarchy** of classes:
 - (Implicit) Root of the hierarchy is `Object`.
 - Each `extends` declaration corresponds to an upward arrow.
 - The `extends` relationship is *transitive*: when A extends B and B extends C, we say A *indirectly* extends C. e.g., Every class implicitly `extends` the `Object` class.
- **Ancestor** vs. **Descendant** classes:
 - The **ancestor classes** of a class A are: A itself and all classes that A directly, or indirectly, extends.
 - A *inherits* all code (attributes and methods) from its *ancestor classes*.
∴ A's instances have a **wider range of expected usages** (i.e., attributes and methods) than instances of its *ancestor* classes.
 - The **descendant classes** of a class A are: A itself and all classes that directly, or indirectly, extends A.
 - Code defined in A is *inherited to* all its *descendant classes*.

Multi-Level Inheritance Hierarchy: Smart Phones



Inheritance Accumulates Code for Reuse

- The *lower* a class is in the type hierarchy, the *more code* it accumulates from its *ancestor classes*:
 - A *descendant class* inherits all code from its *ancestor classes*.
 - A *descendant class* may also:
 - Declare new attributes
 - Define new methods
 - **Redefine / Override** inherited methods
- Consequently:
 - When being used as **context objects**, instances of a class' *descendant classes* have a **wider range of expected usages** (i.e., attributes and methods).
 - When expecting an object of a particular class, we may **substitute** it with (**re-assign** it to) an object of any of its *descendant classes*. e.g., When expecting a `Student` object, we may substitute it with either a `ResidentStudent` or a `NonResidentStudent` object.
 - **Justification:** A *descendant class* contains **at least as many** methods as defined in its *ancestor classes* (but not vice versa!).

Reference Variable: Static Type

- A reference variable's **static type** is what we declare it to be.
 - `Student jim` declares jim's ST as Student.
 - `SmartPhone myPhone` declares myPhone's ST as SmartPhone.
 - The **static type** of a reference variable **never changes**.
- For a reference variable v , its **static type** C defines the **expected usages of v as a context object**.
- A method call $v.m(\dots)$ is **compilable** if m is defined in C .
 - e.g., After declaring `Student jim`, we
 - may** call `register` and `getTuition` on `jim`
 - may not** call `setPremiumRate` (specific to a resident student) or `setDiscountRate` (specific to a non-resident student) on `jim`
 - e.g., After declaring `SmartPhone myPhone`, we
 - may** call `dial` and `surfWeb` on `myPhone`
 - may not** call `facetime` (specific to an IOS phone) or `skype` (specific to an Android phone) on `myPhone`

29 of 86

Rules of Substitution

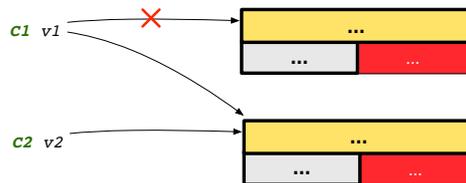
When expecting an object of **static type** A :

- It is **safe** to **substitute** it with an object whose **static type** is any of the **descendant class** of A (including A).
 - \therefore Each **descendant class** of A , being the new substitute, is guaranteed to contain all (non-private) attributes/methods defined in A .
 - e.g., When expecting an IOS phone, you **can** substitute it with either an iPhone6s or iPhone6sPlus.
- It is **unsafe** to **substitute** it with an object whose **static type** is any of the **ancestor classes of A 's parent** (excluding A).
 - \therefore Class A may have defined new methods that do not exist in any of its **parent's ancestor classes**.
 - e.g., When expecting IOS phone, **unsafe** to substitute it with a SmartPhone \therefore facetime not supported in Android phone.
- It is also **unsafe** to **substitute** it with an object whose **static type** is **neither an ancestor nor a descendant** of A .
 - e.g., When expecting IOS phone, **unsafe** to substitute it with an HTC \therefore facetime not supported in Android phone.

31 of 86

Substitutions via Assignments

- By declaring $C1$ $v1$, **reference variable** $v1$ will store the **address** of an object "of class $C1$ " at runtime.
- By declaring $C2$ $v2$, **reference variable** $v2$ will store the **address** of an object "of class $C2$ " at runtime.
- Assignment `v1 = v2` **copies address** stored in $v2$ into $v1$.
 - $v1$ will instead point to wherever $v2$ is pointing to. [**object alias**]



- In such assignment $v1 = v2$, we say that we **substitute** an object of (**static**) type $C1$ by an object of (**static**) type $C2$.
- Substitutions** are subject to **rules!**

30 of 86

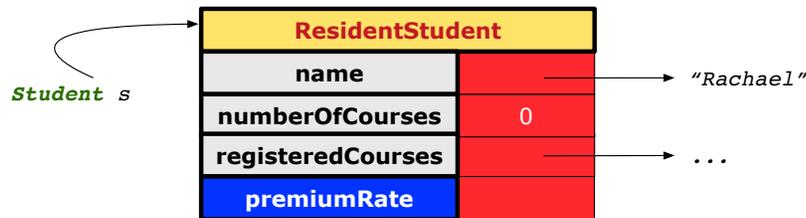
Reference Variable: Dynamic Type

A **reference variable's dynamic type** is the type of object that it is currently pointing to at **runtime**.

- The **dynamic type** of a reference variable **may change** whenever we **re-assign** that variable to a different object.
- There are two ways to re-assigning a reference variable.

32 of 86

Visualizing Static Type vs. Dynamic Type



- Each segmented box denotes a *runtime* object.
- Arrow denotes a variable (e.g., *s*) storing the object's address. Usually, when the context is clear, we leave the variable's *static type* implicit (*Student*).
- Title of box indicates type of runtime object, which denotes the *dynamic type* of the variable (*ResidentStudent*).

33 of 86

Reference Variable: Changing Dynamic Type (1)

Re-assigning a reference variable to a newly-created object:

- Substitution Principle: the new object's class must be a *descendant class* of the reference variable's *static type*.
- e.g., `Student jim = new ResidentStudent(...)` changes the *dynamic type* of *jim* to *ResidentStudent*.
- e.g., `Student jim = new NonResidentStudent(...)` changes the *dynamic type* of *jim* to *NonResidentStudent*.
- e.g., `ResidentStudent jim = new Student(...)` is illegal because *Student* is **not** a *descendant class* of the *static type* of *jim* (i.e., *ResidentStudent*).

34 of 86

Reference Variable: Changing Dynamic Type (2)

Re-assigning a reference variable *v* to an existing object that is referenced by another variable *other* (i.e., `v = other`):

- Substitution Principle: the static type of *other* must be a *descendant class* of *v*'s *static type*.
- e.g., Say we declare

```
Student jim = new Student(...);
ResidentStudent rs = new ResidentStudent(...);
NonResidentStudent nrs = new NonResidentStudent(...);
```

- `rs = jim` ✗
- `nrs = jim` ✗
- `jim = rs` ✓
changes the *dynamic type* of *jim* to the dynamic type of *rs*
- `jim = nrs` ✓
changes the *dynamic type* of *jim* to the dynamic type of *nrs*

35 of 86

Polymorphism and Dynamic Binding (1)

- *Polymorphism*: An object variable may have "*multiple possible shapes*" (i.e., allowable *dynamic types*).
 - Consequently, there are *multiple possible versions* of each method that may be called.
 - e.g., A *Student* variable may have the *dynamic type* of *Student*, *ResidentStudent*, or *NonResidentStudent*.
 - This means that there are *three possible versions* of the `getTuition()` that may be called.
- *Dynamic binding*: When a method *m* is called on an object variable, the version of *m* corresponding to its "*current shape*" (i.e., one defined in the *dynamic type* of *m*) will be called.

```
Student jim = new ResidentStudent(...);
jim.getTuition(); /* version in ResidentStudent */
jim = new NonResidentStudent(...);
jim.getTuition(); /* version in NonResidentStudent */
```

36 of 86

Polymorphism and Dynamic Binding (2.1)



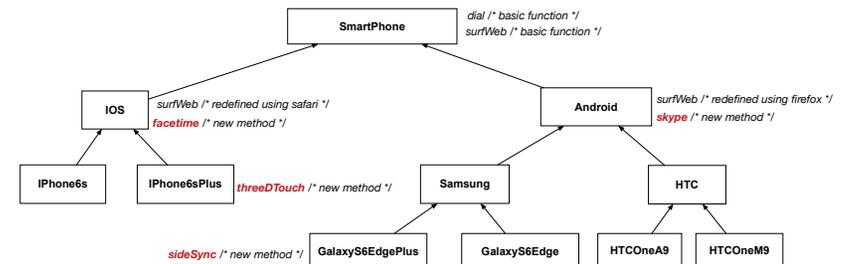
```
class Student {...}
class ResidentStudent extends Student {...}
class NonResidentStudent extends Student {...}
```

```
class StudentTester1 {
    public static void main(String[] args) {
        Student jim = new Student("J. Davis");
        ResidentStudent rs = new ResidentStudent("J. Davis");
        jim = rs; /* legal */
        rs = jim; /* illegal */

        NonResidentStudent nrs = new NonResidentStudent("J. Davis");
        jim = nrs; /* legal */
        nrs = jim; /* illegal */
    }
}
```

37 of 86

Polymorphism and Dynamic Binding (3.1)



39 of 86

Polymorphism and Dynamic Binding (2.2)



```
class Student {...}
class ResidentStudent extends Student {...}
class NonResidentStudent extends Student {...}
```

```
class StudentTester2 {
    public static void main(String[] args) {
        Course eeecs2030 = new Course("EECS2030", 500.0);
        Student jim = new Student("J. Davis");
        ResidentStudent rs = new ResidentStudent("J. Davis");
        rs.setPremiumRate(1.5);
        jim = rs;
        System.out.println(jim.getTuition()); /* 750.0 */
        NonResidentStudent nrs = new NonResidentStudent("J. Davis");
        nrs.setDiscountRate(0.5);
        jim = nrs;
        System.out.println(jim.getTuition()); /* 250.0 */
    }
}
```

38 of 86

Polymorphism and Dynamic Binding (3.2)



```
class SmartPhoneTest1 {
    public static void main(String[] args) {
        SmartPhone myPhone;
        IOS ip = new iPhone6sPlus();
        Samsung ss = new GalaxyS6Edge();
        myPhone = ip; /* legal */
        myPhone = ss; /* legal */

        IOS presentForHeeyeon;
        presentForHeeyeon = ip; /* legal */
        presentForHeeyeon = ss; /* illegal */
    }
}
```

40 of 86

Polymorphism and Dynamic Binding (3.3)



```
class SmartPhoneTest2 {
    public static void main(String[] args) {
        SmartPhone myPhone;
        IOS ip = new iPhone6sPlus();
        myPhone = ip;
        myPhone.surfWeb(); /* version of surfWeb in iPhone6sPlus */

        Samsung ss = new GalaxyS6Edge();
        myPhone = ss;
        myPhone.surfWeb(); /* version of surfWeb in GalaxyS6Edge */
    }
}
```

41 of 86

Reference Type Casting: Motivation (1.1)



```
1 Student jim = new ResidentStudent("J. Davis");
2 ResidentStudent rs = jim;
3 rs.setPremiumRate(1.5);
```

- **L1 is legal:** ResidentStudent is a **descendant class** of the **static type** of jim (i.e., Student).
- **L2 is illegal:** jim's **ST** (i.e., Student) is **not** a descendant class of rs's **ST** (i.e., ResidentStudent).
Java compiler is **unable to infer** that jim's **dynamic type** in L2 is ResidentStudent!
- Force the Java compiler to believe so via a cast in L2:
ResidentStudent rs = (**ResidentStudent**) jim;
 - The cast (**ResidentStudent**) jim on the **RHS of =** temporarily modifies jim's **ST** to ResidentStudent.
 - Alias rs of **ST** ResidentStudent is then created via an assignment.
- **dynamic binding:** After the **cast**, L3 will execute the correct version of setPremiumRate.

42 of 86

Reference Type Casting: Motivation (1.2)



```
ST: ResidentStudent      valid substitution      ST: Student
ResidentStudent rs      =      (ResidentStudent) jim ;
                               temporarily modify ST
                               ST: ResidentStudent
```

- Variable rs is declared of **static type (ST)** ResidentStudent.
- Variable jim is declared of **ST** Student.
- The cast expression (**ResidentStudent**) jim **temporarily** modifies jim's **ST** to ResidentStudent.
⇒ Such a cast makes the assignment **valid**.
∴ RHS's **ST** (ResidentStudent) is a **descendant** of LHS's **ST** (ResidentStudent).
⇒ The assignment creates an **alias** rs with **ST** ResidentStudent.
- **No** new object is created.
Only an **alias** rs with a different **ST** (ResidentStudent) is created.
- After the assignment, jim's **ST** **remains** Student.

43 of 86

Reference Type Casting: Motivation (2.1)

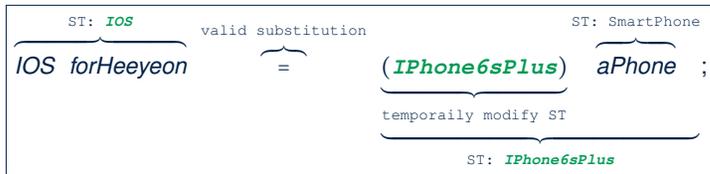


```
1 SmartPhone aPhone = new iPhone6sPlus();
2 IOS forHeeyeon = aPhone;
3 forHeeyeon.facetime();
```

- **L1 is legal:** iPhone6sPlus is a **descendant class** of the **static type** of aPhone (i.e., SmartPhone).
- **L2 is illegal:** aPhone's **ST** (i.e., SmartPhone) is **not** a descendant class of forHeeyeon's **ST** (i.e., IOS).
Java compiler is **unable to infer** that aPhone's **dynamic type** in L2 is iPhone6sPlus!
- Force Java compiler to believe so via a **cast** in L2:
IOS forHeeyeon = (**iPhone6sPlus**) aPhone;
 - The cast (**iPhone6sPlus**) aPhone on the **RHS of =** temporarily modifies aPhone's **ST** to iPhone6sPlus.
 - Alias forHeeyeon of **ST** IOS is then created via an assignment.
- **dynamic binding:** After the **cast**, L3 will execute the correct version of facetime.

44 of 86

Reference Type Casting: Motivation (2.2)



- Variable forHeeyeon is declared of **static type (ST)** IOS.
- Variable aPhone is declared of **ST** SmartPhone.
- The cast expression `(iPhone6sPlus) aPhone` **temporarily** modifies aPhone's **ST** to iPhone6sPlus.
 - ⇒ Such a cast makes the assignment valid.
 - ∴ RHS's **ST** (iPhone6sPlus) is a descendant of LHS's **ST** (IOS).
 - ⇒ The assignment creates an alias forHeeyeon with **ST** IOS.
- No** new object is created.
 - Only an alias forHeeyeon with a different **ST** (IOS) is created.
- After the assignment, aPhone's **ST** **remains** SmartPhone.

45 of 86

Notes on Type Cast (1)



- Given variable **v** of **static type** ST_v , it is **compilable** to cast **v** to **C**, as long as **C** is an **ancestor** or **descendant** of ST_v .
- Without cast, we can **only** call methods defined in ST_v on **v**.
- Casting **v** to **C** **temporarily** changes the **ST** of **v** from ST_v to **C**.
 - ⇒ All methods that are defined in **C** can be called.

```

Android myPhone = new GalaxyS6EdgePlus();
/* can call methods declared in Android on myPhone
 * dial, surfweb, skype ✓ sideSync × */
SmartPhone sp = (SmartPhone) myPhone;
/* Compiles OK ∴ SmartPhone is an ancestor class of Android
 * expectations on sp narrowed to methods in SmartPhone
 * sp.dial, sp.surfweb ✓ sp.skype, sp.sideSync × */
GalaxyS6EdgePlus ga = (GalaxyS6EdgePlus) myPhone;
/* Compiles OK ∴ GalaxyS6EdgePlus is a descendant class of Android
 * expectations on ga widened to methods in GalaxyS6EdgePlus
 * ga.dial, ga.surfweb, ga.skype, ga.sideSync ✓ */
  
```

47 of 86

Type Cast: Named or Anonymous



Named Cast: Use intermediate variable to store the cast result.

```

SmartPhone aPhone = new iPhone6sPlus();
IOS forHeeyeon = (iPhone6sPlus) aPhone;
forHeeyeon.facetime();
  
```

Anonymous Cast: Use the cast result directly.

```

SmartPhone aPhone = new iPhone6sPlus();
((iPhone6sPlus) aPhone).facetime();
  
```

Common Mistake:

```

1 SmartPhone aPhone = new iPhone6sPlus();
2 (iPhone6sPlus) aPhone.facetime();
  
```

L2 \equiv `(iPhone6sPlus) (aPhone.facetime())`: Call, then cast.

⇒ This does **not** compile ∴ `facetime()` is **not** declared in the **static type** of aPhone (SmartPhone).

46 of 86

Reference Type Casting: Danger (1)



```

1 Student jim = new NonResidentStudent("J. Davis");
2 ResidentStudent rs = (ResidentStudent) jim;
3 rs.setPremiumRate(1.5);
  
```

- L1** is **legal**: NonResidentStudent is a **descendant** of the static type of jim (Student).
- L2** is **legal** (where the cast type is ResidentStudent):
 - cast type is **descendant** of jim's ST (Student).
 - cast type is **descendant** of rs's ST (ResidentStudent).
- L3** is **legal** ∴ `setPremiumRate` is in rs' **ST** ResidentStudent.
- Java compiler is **unable to infer** that jim's **dynamic type** in L2 is actually NonResidentStudent.
- Executing **L2** will result in a **ClassCastException**.
 - ∴ Attribute `premiumRate` (expected from a **ResidentStudent**) is **undefined** on the **NonResidentStudent** object being cast.

48 of 86

Reference Type Casting: Danger (2)

```

1 SmartPhone aPhone = new GalaxyS6EdgePlus();
2 iPhone6sPlus forHeeyeon = (iPhone6sPlus) aPhone;
3 forHeeyeon.threeDTouch();

```

- **L1** is *legal*: GalaxyS6EdgePlus is a **descendant** of the static type of aPhone (SmartPhone).
- **L2** is *legal* (where the cast type is iPhone6sPlus):
 - cast type is **descendant** of aPhone's ST (SmartPhone).
 - cast type is **descendant** of forHeeyeon's ST (iPhone6sPlus).
- **L3** is *legal* ∴ threeDTouch is in forHeeyeon' **ST** iPhone6sPlus.
- Java compiler is *unable to infer* that aPhone's **dynamic type** in **L2** is actually NonResidentStudent.
- Executing **L2** will result in a **ClassCastException**.
 - ∴ Methods facetime, threeDTouch (expected from an **iPhone6sPlus**) is *undefined* on the **GalaxyS6EdgePlus** object being cast.

49 of 86

Notes on Type Cast (2.2)

Given a variable v of static type ST_v and dynamic type DT_v :

- $(C) v$ is **compilable** if C is ST_v 's **ancestor** or **descendant**.
- Casting v to C 's **ancestor/descendant** **narrows/widens** expectations.
- However, being **compilable** does not guarantee **runtime-error-free!**

```

1 SmartPhone myPhone = new Samsung();
2 /* ST of myPhone is SmartPhone; DT of myPhone is Samsung */
3 iPhone6sPlus ip = (iPhone6sPlus) myPhone;
4 /* Compiles OK ∴ iPhone6sPlus is a descendant class of SmartPhone
5 * can now call methods declared in iPhone6sPlus on ip
6 * ip.dial, ip.surfweb, ip.facetime, ip.threeDTouch ✓ */

```

- Type cast in **L3** is **compilable**.
- Executing **L3** will cause **ClassCastException**.
 - L3**: myPhone's **DT** Samsung cannot meet expectations of the temporary **ST** iPhone6sPlus (e.g., threeDTouch).

51 of 86

Notes on Type Cast (2.1)

Given a variable v of static type ST_v and dynamic type DT_v :

- $(C) v$ is **compilable** if C is ST_v 's **ancestor** or **descendant**.
- Casting v to C 's **ancestor/descendant** **narrows/widens** expectations.
- However, being **compilable** does not guarantee **runtime-error-free!**

```

1 SmartPhone myPhone = new Samsung();
2 /* ST of myPhone is SmartPhone; DT of myPhone is Samsung */
3 GalaxyS6EdgePlus ga = (GalaxyS6EdgePlus) myPhone;
4 /* Compiles OK ∴ GalaxyS6EdgePlus is a descendant class of SmartPhone
5 * can now call methods declared in GalaxyS6EdgePlus on ga
6 * ga.dial, ga.surfweb, ga.skype, ga.sideSync ✓ */

```

- Type cast in **L3** is **compilable**.
- Executing **L3** will cause **ClassCastException**.
 - L3**: myPhone's **DT** Samsung cannot meet expectations of the temporary **ST** GalaxyS6EdgePlus (e.g., sideSync).

50 of 86

Notes on Type Cast (2.3)

A cast $(C) v$ is **compilable** and **runtime-error-free** if C is located along the **ancestor path** of DT_v .

e.g., Given `Android myPhone = new Samsung();`

- Cast myPhone to a class along the **ancestor path** of its **DT Samsung**.
- Casting myPhone to a class with more expectations than its **DT Samsung** (e.g., GalaxyS6EdgePlus) will cause **ClassCastException**.
- Casting myPhone to a class irrelevant to its **DT Samsung** (e.g., HTCOneA9) will cause **ClassCastException**.

52 of 86

Required Reading: Static Types, Dynamic Types, Casts



https://www.eecs.yorku.ca/~jackie/teaching/lectures/2018/F/EECS2030/notes/EECS2030_F18_Notes_Static_Types_Cast.pdf

53 of 86

Compilable Cast vs. Exception-Free Cast



```
class A { }  
class B extends A { }  
class C extends B { }  
class D extends A { }
```

```
1 B b = new C();  
2 D d = (D) b;
```

- After L1:
 - **ST** of b is B
 - **DT** of b is C
- Does L2 compile? [NO]
∴ cast type D is neither an ancestor nor a descendant of b's **ST** B
- Would `D d = (D) ((A) b)` fix L2? [YES]
∴ cast type D is an ancestor of b's cast, temporary **ST** A
- `ClassCastException` when executing this fixed L2? [YES]
∴ cast type D is not an ancestor of b's **DT** C

54 of 86

Reference Type Casting: Runtime Check (1)



```
1 Student jim = new NonResidentStudent("J. Davis");  
2 if (jim instanceof ResidentStudent) {  
3     ResidentStudent rs = (ResidentStudent) jim;  
4     rs.setPremiumRate(1.5);  
5 }
```

- L1 is **legal**: NonResidentStudent is a descendant class of the **static type** of jim (i.e., Student).
- L2 checks if jim's **dynamic type** is ResidentStudent.
FALSE ∴ jim's **dynamic type** is NonResidentStudent!
- L3 is **legal**: jim's cast type (i.e., ResidentStudent) is a descendant class of rs's **static type** (i.e., ResidentStudent).
- L3 will not be executed at runtime, hence no `ClassCastException`, thanks to the check in L2!

55 of 86

Reference Type Casting: Runtime Check (2)



```
1 SmartPhone aPhone = new GalaxyS6EdgePlus();  
2 if (aPhone instanceof iPhone6sPlus) {  
3     IOS forHeeyeon = (iPhone6sPlus) aPhone;  
4     forHeeyeon.facetime();  
5 }
```

- L1 is **legal**: GalaxyS6EdgePlus is a descendant class of the static type of aPhone (i.e., SmartPhone).
- L2 checks if aPhone's **dynamic type** is iPhone6sPlus.
FALSE ∴ aPhone's **dynamic type** is GalaxyS6EdgePlus!
- L3 is **legal**: aPhone's cast type (i.e., iPhone6sPlus) is a descendant class of forHeeyeon's **static type** (i.e., IOS).
- L3 will not be executed at runtime, hence no `ClassCastException`, thanks to the check in L2!

56 of 86

Notes on the instanceof Operator (1)



Given a reference variable v and a class C , you write

```
v instanceof C
```

to check if the **dynamic type** of v , at the moment of being checked, is a **descendant class** of C (so that $(C) v$ is **safe**).

```
SmartPhone myPhone = new Samsung();
println(myPhone instanceof Android);
/* true :: Samsung is a descendant of Android */
println(myPhone instanceof Samsung);
/* true :: Samsung is a descendant of Samsung */
println(myPhone instanceof GalaxyS6Edge);
/* false :: Samsung is not a descendant of GalaxyS6Edge */
println(myPhone instanceof IOS);
/* false :: Samsung is not a descendant of IOS */
println(myPhone instanceof iPhone6sPlus);
/* false :: Samsung is not a descendant of iPhone6sPlus */
```

⇒ **Samsung** is the most specific type which `myPhone` can be safely cast to.

57 of 86

Notes on the instanceof Operator (2)



Given a reference variable v and a class C ,

`v instanceof C` checks if the **dynamic type** of v , at the moment of being checked, is a descendant class of C .

```
1 SmartPhone myPhone = new Samsung();
2 /* ST of myPhone is SmartPhone; DT of myPhone is Samsung */
3 if(myPhone instanceof Samsung) {
4     Samsung samsung = (Samsung) myPhone;
5 }
6 if(myPhone instanceof GalaxyS6EdgePlus) {
7     GalaxyS6EdgePlus galaxy = (GalaxyS6EdgePlus) myPhone;
8 }
9 if(myPhone instanceof HTC) {
10     HTC htc = (HTC) myPhone;
11 }
```

• **L3** evaluates to **true**. [safe to cast]

• **L6** and **L9** evaluate to **false**. [unsafe to cast]

This prevents **L7** and **L10**, causing `ClassCastException` if executed, from being executed.

58 of 86

Static Type and Polymorphism (1.1)



```
class SmartPhone {
    void dial() { ... }
}
class IOS extends SmartPhone {
    void facetime() { ... }
}
class iPhone6sPlus extends IOS {
    void threeDTouch() { ... }
}
```

```
1 SmartPhone sp = new iPhone6sPlus(); ✓
2 sp.dial(); ✓
3 sp.facetime(); ✗
4 sp.threeDTouch(); ✗
```

Static type of `sp` is `SmartPhone`

⇒ can only call methods defined in `SmartPhone` on `sp`

59 of 86

Static Type and Polymorphism (1.2)



```
class SmartPhone {
    void dial() { ... }
}
class IOS extends SmartPhone {
    void facetime() { ... }
}
class iPhone6sPlus extends IOS {
    void threeDTouch() { ... }
}
```

```
1 IOS ip = new iPhone6sPlus(); ✓
2 ip.dial(); ✓
3 ip.facetime(); ✓
4 ip.threeDTouch(); ✗
```

Static type of `ip` is `IOS`

⇒ can only call methods defined in `IOS` on `ip`

60 of 86

Static Type and Polymorphism (1.3)



```
class SmartPhone {
    void dial() { ... }
}
class IOS extends SmartPhone {
    void facetime() { ... }
}
class iPhone6sPlus extends IOS {
    void threeDTouch() { ... }
}
```

```
1 iPhone6sPlus ip6sp = new iPhone6sPlus(); ✓
2 ip6sp.dial(); ✓
3 ip6sp.facetime(); ✓
4 ip6sp.threeDTouch(); ✓
```

Static type of `ip6sp` is `iPhone6sPlus`

⇒ can call all methods defined in `iPhone6sPlus` on `ip6sp`

61 of 86

Static Type and Polymorphism (2)



Given a reference variable declaration

```
C v;
```

- **Static type** of reference variable `v` is class `C`
- A method call `[v.m]` is valid if `m` is a method **defined** in class `C`.
- Despite the **dynamic type** of `v`, you are only allowed to call methods that are defined in the **static type** `C` on `v`.
- If you are certain that `v`'s **dynamic type** can be expected **more** than its **static type**, then you may use an `instanceof` check and a cast.

```
Course eeecs2030 = new Course("EECS2030", 500.0);
Student s = new ResidentStudent("Jim");
s.register(eeecs2030);
if (s instanceof ResidentStudent) {
    ((ResidentStudent) s).setPremiumRate(1.75);
    System.out.println(((ResidentStudent) s).getTuition());
}
```

63 of 86

Static Type and Polymorphism (1.4)



```
class SmartPhone {
    void dial() { ... }
}
class IOS extends SmartPhone {
    void facetime() { ... }
}
class iPhone6sPlus extends IOS {
    void threeDTouch() { ... }
}
```

```
1 SmartPhone sp = new iPhone6sPlus(); ✓
2 ((iPhone6sPlus) sp).dial(); ✓
3 ((iPhone6sPlus) sp).facetime(); ✓
4 ((iPhone6sPlus) sp).threeDTouch(); ✓
```

L4 is equivalent to the following two lines:

```
iPhone6sPlus ip6sp = ((iPhone6sPlus) sp);
ip6sp.threeDTouch();
```

62 of 86

Polymorphism: Method Call Arguments (1)



```
1 class StudentManagementSystem {
2     Student[] ss; /* ss[i] has static type Student */ int c;
3     void addRS(ResidentStudent rs) { ss[c] = rs; c++; }
4     void addNRS(NonResidentStudent nrs) { ss[c] = nrs; c++; }
5     void addStudent(Student s) { ss[c] = s; c++; } }
```

- **L3**: `ss[c] = rs` is valid. ∴ RHS's ST `ResidentStudent` is a **descendant class** of LHS's ST `Student`.
- Say we have a `StudentManagementSystem` object `sms`:
 - `sms.addRS(o)` attempts the following assignment (recall call by value), which replaces parameter `rs` by a copy of argument `o`:

```
rs = o;
```

 - Whether this argument passing is valid depends on `o`'s **static type**.
- In the signature of a method `m`, if the type of a parameter is class `C`, then we may call method `m` by passing objects whose **static types** are `C`'s **descendants**.

64 of 86

Polymorphism: Method Call Arguments (2.1)



In the StudentManagementSystemTester:

```
Student s1 = new Student();
Student s2 = new ResidentStudent();
Student s3 = new NonResidentStudent();
ResidentStudent rs = new ResidentStudent();
NonResidentStudent nrs = new NonResidentStudent();
StudentManagementSystem sms = new StudentManagementSystem();
sms.addRS(s1); ×
sms.addRS(s2); ×
sms.addRS(s3); ×
sms.addRS(rs); ✓
sms.addRS(nrs); ×
sms.addStudent(s1); ✓
sms.addStudent(s2); ✓
sms.addStudent(s3); ✓
sms.addStudent(rs); ✓
sms.addStudent(nrs); ✓
```

65 of 86

Polymorphism: Method Call Arguments (2.3)



In the StudentManagementSystemTester:

```
1 Student s = new NonResidentStudent("Nancy");
2 /* s' ST: Student; s' DT: NonResidentStudent */
3 StudentManagementSystem sms = new StudentManagementSystem();
4 sms.addRS(s); ×
```

- o L4 compiles with a cast: `sms.addRS((ResidentStudent) s)`
 - Valid cast: (ResidentStudent) is a descendant of s' ST.
 - Valid call: s' temporary ST (ResidentStudent) is now a descendant class of addRS's parameter rs' ST (ResidentStudent).
- o But, there will be a **ClassCastException** at runtime!
∴ s' DT (NonResidentStudent) **not descendant** of ResidentStudent.
- o We should have written:

```
if(s instanceof ResidentStudent) {
    sms.addRS((ResidentStudent) s);
}
```

The instanceof expression will evaluate to **false**, meaning it is **unsafe** to cast, thus preventing ClassCastException.

67 of 86

Polymorphism: Method Call Arguments (2.2)



In the StudentManagementSystemTester:

```
1 Student s = new Student("Stella");
2 /* s' ST: Student; s' DT: Student */
3 StudentManagementSystem sms = new StudentManagementSystem();
4 sms.addRS(s); ×
```

- o L4 compiles with a cast: `sms.addRS((ResidentStudent) s)`
 - Valid cast: (ResidentStudent) is a descendant of s' ST.
 - Valid call: s' temporary ST (ResidentStudent) is now a descendant class of addRS's parameter rs' ST (ResidentStudent).
- o But, there will be a **ClassCastException** at runtime!
∴ s' DT (Student) is **not a descendant** of ResidentStudent.
- o We should have written:

```
if(s instanceof ResidentStudent) {
    sms.addRS((ResidentStudent) s);
}
```

The instanceof expression will evaluate to **false**, meaning it is **unsafe** to cast, thus preventing ClassCastException.

66 of 86

Polymorphism: Method Call Arguments (2.4)



In the StudentManagementSystemTester:

```
1 Student s = new ResidentStudent("Rachael");
2 /* s' ST: Student; s' DT: ResidentStudent */
3 StudentManagementSystem sms = new StudentManagementSystem();
4 sms.addRS(s); ×
```

- o L4 compiles with a cast: `sms.addRS((ResidentStudent) s)`
 - Valid cast: (ResidentStudent) is a descendant of s' ST.
 - Valid call: s' temporary ST (ResidentStudent) is now a descendant class of addRS's parameter rs' ST (ResidentStudent).
- o And, there will be **no ClassCastException** at runtime!
∴ s' DT (ResidentStudent) is **descendant** of ResidentStudent.
- o We should have written:

```
if(s instanceof ResidentStudent) {
    sms.addRS((ResidentStudent) s);
}
```

The instanceof expression will evaluate to **true**, meaning it is **safe** to cast.

68 of 86

Polymorphism: Method Call Arguments (2.5)



In the StudentManagementSystemTester:

```

1 NonResidentStudent nrs = new NonResidentStudent();
2 /* ST: NonResidentStudent; DT: NonResidentStudent */
3 StudentManagementSystem sms = new StudentManagementSystem();
4 sms.addRS(nrs); x
    
```

Will L4 with a cast compile?

```
sms.addRS( (ResidentStudent) nrs)
```

NO ∴ (ResidentStudent) is **not** a descendant of nrs's **ST** (NonResidentStudent).

Polymorphism and Dynamic Binding: A Polymorphic Collection of Students (1)



```

1 ResidentStudent rs = new ResidentStudent("Rachael");
2 rs.setPremiumRate(1.5);
3 NonResidentStudent nrs = new NonResidentStudent("Nancy");
4 nrs.setDiscountRate(0.5);
5 StudentManagementSystem sms = new StudentManagementSystem();
6 sms.addStudent(rs); /* polymorphism */
7 sms.addStudent(nrs); /* polymorphism */
8 Course eeecs2030 = new Course("EECS2030", 500.0);
9 sms.registerAll(eeecs2030);
10 for(int i = 0; i < sms.numberOfStudents; i++) {
11     /* Dynamic Binding:
12      * Right version of getTuition will be called */
13     System.out.println(sms.students[i].getTuition());
14 }
    
```

Why Inheritance: A Polymorphic Collection of Students



How do you define a class StudentManagementSystem that contains a list of *resident* and *non-resident* students?

```

class StudentManagementSystem {
    Student[] students;
    int numOfStudents;

    void addStudent(Student s) {
        students[numOfStudents] = s;
        numOfStudents++;
    }

    void registerAll (Course c) {
        for(int i = 0; i < numberOfStudents; i++) {
            students[i].register(c)
        }
    }
}
    
```

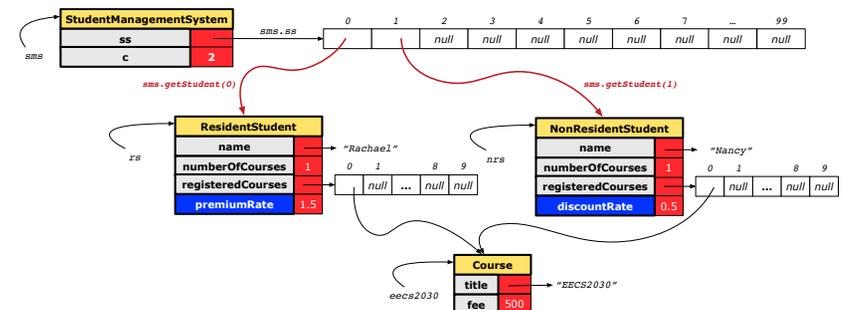
a collection of students without inheritance

Polymorphism and Dynamic Binding: A Polymorphic Collection of Students (2)



At runtime, attribute `sms.ss` is a **polymorphic** array:

- **Static type** of each item is as declared: **Student**
- **Dynamic type** of each item is a descendant of **Student**: **ResidentStudent**, **NonResidentStudent**



Polymorphism: Return Values (1)

```

1 class StudentManagementSystem {
2     Student[] ss; int c;
3     void addStudent(Student s) { ss[c] = s; c++; }
4     Student getStudent(int i) {
5         Student s = null;
6         if(i < 0 || i >= c) {
7             throw new IllegalArgumentException("Invalid index.");
8         }
9         else {
10            s = ss[i];
11        }
12        return s;
13    }
}

```

L4: Student is **static type** of getStudent's return value.

L10: ss[i]'s ST (Student) is **descendant** of s' ST (Student).

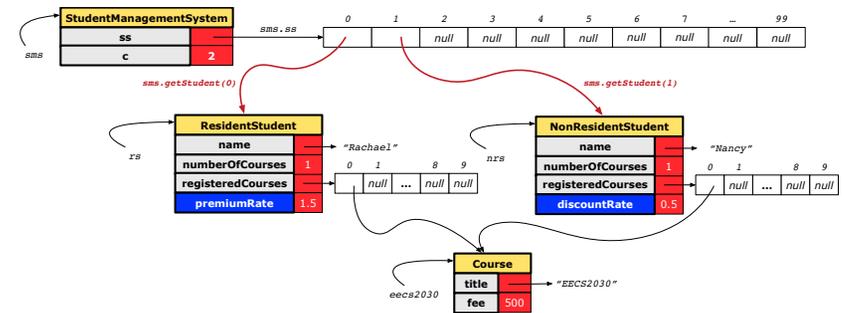
Question: What can be the **dynamic type** of s after L10?

Answer: All descendant classes of Student.

Polymorphism: Return Values (3)

At runtime, attribute `sms.ss` is a **polymorphic** array:

- **Static type** of each item is as declared: **Student**
- **Dynamic type** of each item is a **descendant of Student**: **ResidentStudent**, **NonResidentStudent**



Polymorphism: Return Values (2)

```

1 Course eeCS2030 = new Course("EECS2030", 500);
2 ResidentStudent rs = new ResidentStudent("Rachael");
3 rs.setPremiumRate(1.5); rs.register(eeCS2030);
4 NonResidentStudent nrs = new NonResidentStudent("Nancy");
5 nrs.setDiscountRate(0.5); nrs.register(eeCS2030);
6 StudentManagementSystem sms = new StudentManagementSystem();
7 sms.addStudent(rs); sms.addStudent(nrs);
8 Student s = sms.getStudent(0); /* dynamic type of s? */

          static return type: Student
9 print(s instanceof Student && s instanceof ResidentStudent); /* true */
10 print(s instanceof NonResidentStudent); /* false */
11 print(s.getTuition()); /* Version in ResidentStudent called:750 */
12 ResidentStudent rs2 = sms.getStudent(0); /* x */
13 s = sms.getStudent(1); /* dynamic type of s? */

          static return type: Student
14 print(s instanceof Student && s instanceof NonResidentStudent); /* true */
15 print(s instanceof ResidentStudent); /* false */
16 print(s.getTuition()); /* Version in NonResidentStudent called:250 */
17 NonResidentStudent nrs2 = sms.getStudent(1); /* x */

```

Static Type vs. Dynamic Type: When to consider which?

- **Whether or not Java code compiles** depends only on the **static types** of relevant variables.
 - ∴ Inferring the **dynamic type** statically is an **undecidable** problem that is inherently impossible to solve.
- **The behaviour of Java code being executed at runtime** (e.g., which version of method is called due to dynamic binding, whether or not a `ClassCastException` will occur, etc.) depends on the **dynamic types** of relevant variables.
 - ⇒ Best practice is to visualize how objects are created (by drawing boxes) and variables are re-assigned (by drawing arrows).

Summary: Type Checking Rules



CODE	CONDITION TO BE TYPE CORRECT
<code>x = y</code>	Is <i>y</i> 's ST a descendant of <i>x</i> 's ST ?
<code>x.m(y)</code>	Is method <i>m</i> defined in <i>x</i> 's ST ? Is <i>y</i> 's ST a descendant of <i>m</i> 's parameter's ST ?
<code>z = x.m(y)</code>	Is method <i>m</i> defined in <i>x</i> 's ST ? Is <i>y</i> 's ST a descendant of <i>m</i> 's parameter's ST ? Is ST of <i>m</i> 's return value a descendant of <i>z</i> 's ST ?
<code>(C) y</code>	Is <i>C</i> an ancestor or a descendant of <i>y</i> 's ST ?
<code>x = (C) y</code>	Is <i>C</i> an ancestor or a descendant of <i>y</i> 's ST ? Is <i>C</i> a descendant of <i>x</i> 's ST ?
<code>x.m((C) y)</code>	Is <i>C</i> an ancestor or a descendant of <i>y</i> 's ST ? Is method <i>m</i> defined in <i>x</i> 's ST ? Is <i>C</i> a descendant of <i>m</i> 's parameter's ST ?

Even if `(C) y` compiles OK, there will be a runtime `ClassCastException` if *C* is not an **ancestor** of *y*'s **DT**!

77 of 86

Root of the Java Class Hierarchy



- Implicitly:
 - Every class is a *child/sub* class of the `Object` class.
 - The `Object` class is the *parent/super* class of every class.
- There are two useful *accessor methods* that every class *inherits* from the `Object` class:

- `boolean equals(Object other)`
 - Indicates whether some other object is "equal to" this one.
 - The default definition inherited from `Object`:

```
boolean equals(Object other) {
    return (this == other); }
```

- `String toString()`
 - Returns a string representation of the object.
- Very often when you define new classes, you want to **redefine/override** the inherited definitions of `equals` and `toString`.

78 of 86

Overriding and Dynamic Binding (1)



`Object` is the common parent/super class of every class.

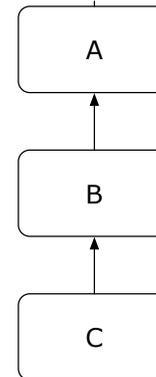
- Every class inherits the **default version** of `equals`
- Say a reference variable *v* has **dynamic type D**:
 - Case 1** *D* **overrides** `equals`
⇒ `v.equals(...)` invokes the **overridden version** in *D*
 - Case 2** *D* does **not override** `equals`
Case 2.1 At least one ancestor classes of *D* **override** `equals`
⇒ `v.equals(...)` invokes the **overridden version** in the **closest ancestor class**
 - Case 2.2** No ancestor classes of *D* **override** `equals`
⇒ `v.equals(...)` invokes **default version** inherited from `Object`.
- Same principle applies to the `toString` method, and all overridden methods in general.

79 of 86

Overriding and Dynamic Binding (2.1)



```
Object {
    boolean equals(Object obj) {
        return this == obj;
    }
}
```



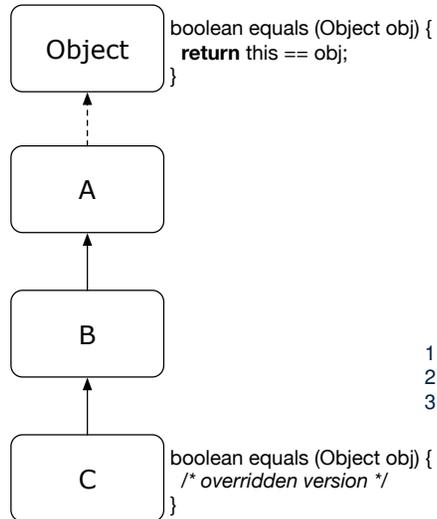
```
class A {
    /*equals not overridden*/
}
class B extends A {
    /*equals not overridden*/
}
class C extends B {
    /*equals not overridden*/
}
```

```
1 Object c1 = new C();
2 Object c2 = new C();
3 println(c1.equals(c2));
```

L3 calls which version of `equals`? [Object]

80 of 86

Overriding and Dynamic Binding (2.2)



```
class A {  
    /*equals not overridden*/  
}  
class B extends A {  
    /*equals not overridden*/  
}  
class C extends B {  
    boolean equals (Object obj) {  
        /* overridden version */  
    }  
}
```

```
1 Object c1 = new C();  
2 Object c2 = new C();  
3 println(c1.equals(c2));
```

L3 calls which version of equals? [C]

81 of 86

Behaviour of Inherited toString Method (1)



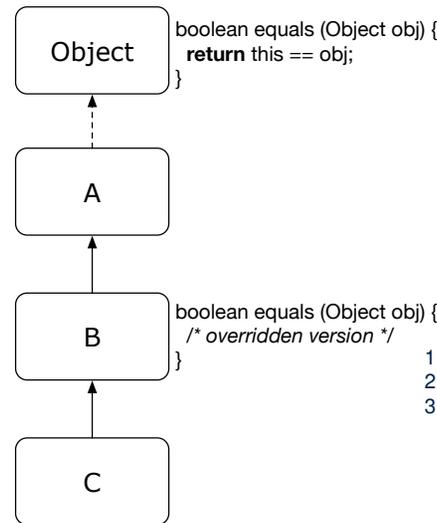
```
Point p1 = new Point(2, 4);  
System.out.println(p1);
```

```
Point@677327b6
```

- Implicitly, the toString method is called inside the println method.
- By default, the address stored in p1 gets printed.
- We need to **redefine / override** the toString method, inherited from the Object class, in the Point class.

83 of 86

Overriding and Dynamic Binding (2.3)



```
class A {  
    /*equals not overridden*/  
}  
class B extends A {  
    boolean equals (Object obj) {  
        /* overridden version */  
    }  
}  
class C extends B {  
    /*equals not overridden*/  
}
```

```
1 Object c1 = new C();  
2 Object c2 = new C();  
3 println(c1.equals(c2));
```

L3 calls which version of equals? [B]

82 of 86

Behaviour of Inherited toString Method (2)



```
class Point {  
    double x;  
    double y;  
    public String toString() {  
        return "(" + this.x + ", " + this.y + ")";  
    }  
}
```

After redefining/overriding the toString method:

```
Point p1 = new Point(2, 4);  
System.out.println(p1);
```

```
(2, 4)
```

84 of 86

Behaviour of Inherited toString Method (3)



Exercise: Override the equals and toString methods for the ResidentStudent and NonResidentStudent classes.

85 of 86

Index (1)



Why Inheritance: A Motivating Example
No Inheritance: ResidentStudent Class
No Inheritance: NonResidentClass
No Inheritance: Testing Student Classes
No Inheritance:
Issues with the Student Classes
No Inheritance: Maintainability of Code (1)
No Inheritance: Maintainability of Code (2)
No Inheritance:
A Collection of Various Kinds of Students
Inheritance Architecture
Inheritance: The Student Parent/Super Class
Inheritance:
The ResidentStudent Child/Sub Class

86 of 86

Index (2)



Inheritance:
The NonResidentStudent Child/Sub Class
Inheritance Architecture Revisited
Using Inheritance for Code Reuse
Visualizing Parent/Child Objects (1)
Visualizing Parent/Child Objects (2)
Testing the Two Student Sub-Classes
Inheritance Architecture: Static Types & Expectations
Polymorphism: Intuition (1)
Polymorphism: Intuition (2)
Polymorphism: Intuition (3)
Dynamic Binding: Intuition (1)
Dynamic Binding: Intuition (2)
Multi-Level Inheritance Architecture

87 of 86

Index (3)



Multi-Level Inheritance Hierarchy:
Smart Phones
Inheritance Forms a Type Hierarchy
Inheritance Accumulates Code for Reuse
Reference Variable: Static Type
Substitutions via Assignments
Rules of Substitution
Reference Variable: Dynamic Type
Visualizing Static Type vs. Dynamic Type
Reference Variable:
Changing Dynamic Type (1)
Reference Variable:
Changing Dynamic Type (2)
Polymorphism and Dynamic Binding (1)
Polymorphism and Dynamic Binding (2.1)

88 of 86

Index (4)

Polymorphism and Dynamic Binding (2.2)
Polymorphism and Dynamic Binding (3.1)
Polymorphism and Dynamic Binding (3.2)
Polymorphism and Dynamic Binding (3.3)
Reference Type Casting: Motivation (1.1)
Reference Type Casting: Motivation (1.2)
Reference Type Casting: Motivation (2.1)
Reference Type Casting: Motivation (2.2)
Type Cast: Named or Anonymous
Notes on Type Cast (1)
Reference Type Casting: Danger (1)
Reference Type Casting: Danger (2)
Notes on Type Cast (2.1)
Notes on Type Cast (2.2)

Index (6)

Polymorphism: Method Call Arguments (2.1)
Polymorphism: Method Call Arguments (2.2)
Polymorphism: Method Call Arguments (2.3)
Polymorphism: Method Call Arguments (2.4)
Polymorphism: Method Call Arguments (2.5)
Why Inheritance:
A Polymorphic Collection of Students
Polymorphism and Dynamic Binding:
A Polymorphic Collection of Students (1)
Polymorphism and Dynamic Binding:
A Polymorphic Collection of Students (2)
Polymorphism: Return Values (1)
Polymorphism: Return Values (2)
Polymorphism: Return Values (3)

Index (5)

Notes on Type Cast (2.3)
Required Reading:
Static Types, Dynamic Types, Casts
Compilable Cast vs. Exception-Free Cast
Reference Type Casting: Runtime Check (1)
Reference Type Casting: Runtime Check (2)
Notes on the instanceof Operator (1)
Notes on the instanceof Operator (2)
Static Type and Polymorphism (1.1)
Static Type and Polymorphism (1.2)
Static Type and Polymorphism (1.3)
Static Type and Polymorphism (1.4)
Static Type and Polymorphism (2)
Polymorphism: Method Call Arguments (1)

Index (7)

Static Type vs. Dynamic Type:
When to consider which?
Summary: Type Checking Rules
Root of the Java Class Hierarchy
Overriding and Dynamic Binding (1)
Overriding and Dynamic Binding (2.1)
Overriding and Dynamic Binding (2.2)
Overriding and Dynamic Binding (2.3)
Behaviour of Inherited toString Method (1)
Behaviour of Inherited toString Method (2)
Behaviour of Inherited toString Method (3)

Abstract Classes and Interfaces



EECS2030 B: Advanced
Object Oriented Programming
Fall 2018

CHEN-WEI WANG



Abstract Class (2)

```
public abstract class Polygon {  
    double[] sides;  
    Polygon(double[] sides) { this.sides = sides; }  
    void grow() {  
        for(int i = 0; i < sides.length; i++) { sides[i]++; }  
    }  
    double getPerimeter() {  
        double perimeter = 0;  
        for(int i = 0; i < sides.length; i++) {  
            perimeter += sides[i];  
        }  
        return perimeter;  
    }  
    abstract double getArea();  
}
```

- Method `getArea` not implemented and shown *signature* only.
- \therefore Polygon cannot be used as a *dynamic type*
- Writing `new Polygon(...)` is forbidden!

3 of 19

Abstract Class (1)



Problem: A polygon may be either a triangle or a rectangle.
Given a polygon, we may either

- **Grow** its shape by incrementing the size of each of its sides;
- Compute and return its **perimeter**; or
- Compute and return its **area**.
- For a rectangle with *length* and *width*, its area is $length \times width$.
- For a triangle with sides *a*, *b*, and *c*, its area, according to Heron's formula, is

$$\sqrt{s(s-a)(s-b)(s-c)}$$

where

$$s = \frac{a+b+c}{2}$$

- How would you solve this problem in Java, while *minimizing code duplicates*?

2 of 19

Abstract Class (3)



```
public class Rectangle extends Polygon {  
    Rectangle(double length, double width) {  
        super(new double[4]);  
        sides[0] = length; sides[1] = width;  
        sides[2] = length; sides[3] = width;  
    }  
    double getArea() { return sides[0] * sides[1]; }  
}
```

- Method `getPerimeter` is inherited from the super-class Polygon.
- Method `getArea` is implemented in the sub-class Rectangle.
- \therefore Rectangle can be used as a *dynamic type*
- Writing `Polygon p = new Rectangle(3, 4)` allowed!

4 of 19

Abstract Class (4)



```
public class Triangle extends Polygon {
    Triangle(double side1, double side2, double side3) {
        super(new double[3]);
        sides[0] = side1; sides[1] = side2; sides[2] = side3;
    }
    double getArea() {
        /* Heron's Formula */
        double s = getPerimeter() * 0.5;
        double area = Math.sqrt(
            s * (s - sides[0]) * (s - sides[1]) * (s - sides[2]));
        return area;
    }
}
```

- Method `getPerimeter` is inherited from `Polygon`.
- Method `getArea` is implemented in the sub-class `Triangle`.
- ∴ `Triangle` can be used as a **dynamic type**
- Writing `Polygon p = new Triangle(3, 4, 5)` allowed!

5 of 19

Abstract Class (6)



```
1 public class PolygonConstructor {
2     Polygon getPolygon(double[] sides) {
3         Polygon p = null;
4         if(sides.length == 3) {
5             p = new Triangle(sides[0], sides[1], sides[2]);
6         }
7         else if(sides.length == 4) {
8             p = new Rectangle(sides[0], sides[1]);
9         }
10        return p;
11    }
12    void grow(Polygon p) { p.grow(); }
13 }
```

- **Polymorphism:**
 - **Line 2** may accept as return value any object whose **static type** is `Polygon` or any of its sub-classes.
 - **Line 5** returns an object whose **dynamic type** is `Triangle`; **Line 8** returns an object whose **dynamic type** is `Rectangle`.

7 of 19

Abstract Class (5)



```
1 public class PolygonCollector {
2     Polygon[] polygons;
3     int numberOfPolygons;
4     PolygonCollector() { polygons = new Polygon[10]; }
5     void addPolygon(Polygon p) {
6         polygons[numberOfPolygons] = p; numberOfPolygons++;
7     }
8     void growAll() {
9         for(int i = 0; i < numberOfPolygons; i++) {
10            polygons[i].grow();
11        }
12    }
13 }
```

- **Polymorphism:** **Line 5** may accept as argument any object whose **static type** is `Polygon` or any of its sub-classes.
- **Dynamic Binding:** **Line 10** calls the version of `grow` inherited to the **dynamic type** of `polygons[i]`.

6 of 19

Abstract Class (7.1)



```
1 public class PolygonTester {
2     public static void main(String[] args) {
3         Polygon p;
4         p = new Rectangle(3, 4); /* polymorphism */
5         System.out.println(p.getPerimeter()); /* 14.0 */
6         System.out.println(p.getArea()); /* 12.0 */
7         p = new Triangle(3, 4, 5); /* polymorphism */
8         System.out.println(p.getPerimeter()); /* 12.0 */
9         System.out.println(p.getArea()); /* 6.0 */
10
11        PolygonCollector col = new PolygonCollector();
12        col.addPolygon(new Rectangle(3, 4)); /* polymorphism */
13        col.addPolygon(new Triangle(3, 4, 5)); /* polymorphism */
14        System.out.println(col.polygons[0].getPerimeter()); /* 14.0 */
15        System.out.println(col.polygons[1].getPerimeter()); /* 12.0 */
16        col.growAll();
17        System.out.println(col.polygons[0].getPerimeter()); /* 18.0 */
18        System.out.println(col.polygons[1].getPerimeter()); /* 15.0 */
19    }
20 }
```

8 of 19

Abstract Class (7.2)

```

1 PolygonConstructor con = new PolygonConstructor();
2 double[] recSides = {3, 4, 3, 4}; p = con.getPolygon(recSides);
3 System.out.println(p instanceof Polygon); ✓
4 System.out.println(p instanceof Rectangle); ✓
5 System.out.println(p instanceof Triangle); ✗
6 System.out.println(p.getPerimeter()); /* 14.0 */
7 System.out.println(p.getArea()); /* 12.0 */
8 con.grow(p);
9 System.out.println(p.getPerimeter()); /* 18.0 */
10 System.out.println(p.getArea()); /* 20.0 */
11 double[] triSides = {3, 4, 5}; p = con.getPolygon(triSides);
12 System.out.println(p instanceof Polygon); ✓
13 System.out.println(p instanceof Rectangle); ✗
14 System.out.println(p instanceof Triangle); ✓
15 System.out.println(p.getPerimeter()); /* 12.0 */
16 System.out.println(p.getArea()); /* 6.0 */
17 con.grow(p);
18 System.out.println(p.getPerimeter()); /* 15.0 */
19 System.out.println(p.getArea()); /* 9.921 */
20 }

```

9 of 19

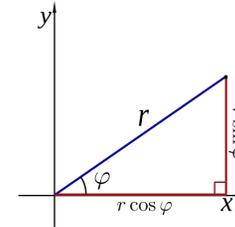
Abstract Class (8)

- An **abstract class**:
 - Typically has **at least one** method with no implementation body
 - May define common implementations inherited to **sub-classes**.
- Recommended to use an **abstract class** as the **static type** of:
 - A **variable**
e.g., Polygon p
 - A **method parameter**
e.g., void grow(Polygon p)
 - A **method return value**
e.g., Polygon getPolygon(double[] sides)
- It is forbidden to use an **abstract class** as a **dynamic type**
e.g., Polygon p = new Polygon(...) is not allowed!
- Instead, create objects whose **dynamic types** are descendant classes of the **abstract class** ⇒ Exploit **dynamic binding**!
e.g., Polygon p = con.getPolygon(recSides)
This is as if we did Polygon p = new Rectangle(...)

10 of 19

Interface (1.1)

- We may implement Point using two representation systems:

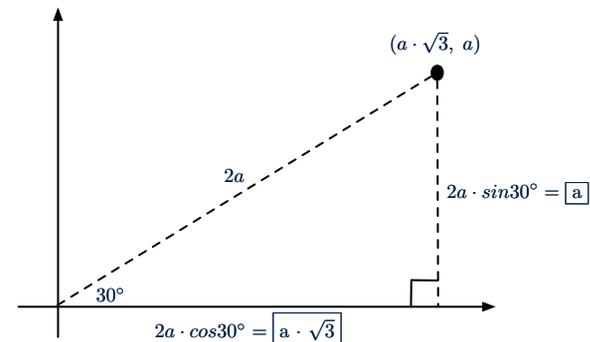


- The **Cartesian system** stores the **absolute** positions of x and y.
- The **Polar system** stores the **relative** position: the angle (in radian) phi and distance r from the origin (0.0).
- As far as users of a Point object p is concerned, being able to call p.getX() and p.getY() is what matters.
- How p.getX() and p.getY() are internally computed, depending on the **dynamic type** of p, do not matter to users.

11 of 19

Interface (1.2)

Recall: $\sin 30^\circ = \frac{1}{2}$ and $\cos 30^\circ = \frac{1}{2} \cdot \sqrt{3}$



We consider the same point represented differently as:

- $r = 2a, \psi = 30^\circ$ [polar system]
- $x = 2a \cdot \cos 30^\circ = a \cdot \sqrt{3}, y = 2a \cdot \sin 30^\circ = a$ [cartesian system]

12 of 19

Interface (2)



```
interface Point {
    double getX();
    double getY();
}
```

- An interface `Point` defines how users may access a point: either get its x coordinate or its y coordinate.
- Methods `getX` and `getY` similar to `getArea` in `Polygon`, have no implementations, but *signatures* only.
- \therefore `Point` cannot be used as a **dynamic type**
- Writing `new Point(...)` is forbidden!

13 of 19

Interface (3)



```
public class CartesianPoint implements Point {
    double x;
    double y;
    CartesianPoint(double x, double y) {
        this.x = x;
        this.y = y;
    }
    public double getX() { return x; }
    public double getY() { return y; }
}
```

- `CartesianPoint` is a possible implementation of `Point`.
- Attributes `x` and `y` declared according to the *Cartesian system*
- All method from the interface `Point` are implemented in the sub-class `CartesianPoint`.
- \therefore `CartesianPoint` can be used as a **dynamic type**
- `Point p = new CartesianPoint(3, 4)` allowed!

14 of 19

Interface (4)



```
public class PolarPoint implements Point {
    double phi;
    double r;
    public PolarPoint(double r, double phi) {
        this.r = r;
        this.phi = phi;
    }
    public double getX() { return Math.cos(phi) * r; }
    public double getY() { return Math.sin(phi) * r; }
}
```

- `PolarPoint` is a possible implementation of `Point`.
- Attributes `phi` and `r` declared according to the *Polar system*
- All method from the interface `Point` are implemented in the sub-class `PolarPoint`.
- \therefore `PolarPoint` can be used as a **dynamic type**
- `Point p = new PolarPoint(3, $\frac{\pi}{6}$)` allowed! [$360^\circ = 2\pi$]

15 of 19

Interface (5)



```
1 public class PointTester {
2     public static void main(String[] args) {
3         double A = 5;
4         double X = A * Math.sqrt(3);
5         double Y = A;
6         Point p;
7         p = new CartesianPoint(X, Y); /* polymorphism */
8         print("(" + p.getX() + ", " + p.getY() + ")"); /* dyn. bin. */
9         p = new PolarPoint(2 * A, Math.toRadians(30)); /* polymorphism */
10        print("(" + p.getX() + ", " + p.getY() + ")"); /* dyn. bin. */
11    }
12 }
```

- Lines 7 and 9 illustrate *polymorphism*, how?
- Lines 8 and 10 illustrate *dynamic binding*, how?

16 of 19

Interface (6)

- An **interface** :
 - Has **all** its methods with no implementation bodies.
 - Leaves complete freedom to its **implementors**.
- Recommended to use an **interface** as the **static type** of:
 - A **variable**
e.g., `Point p`
 - A **method parameter**
e.g., `void moveUp(Point p)`
 - A **method return value**
e.g., `Point getPoint(double v1, double v2, boolean isCartesian)`
- It is forbidden to use an **interface** as a **dynamic type**
e.g., `Point p = new Point(...)` is not allowed!
- Instead, create objects whose **dynamic types** are descendant classes of the **interface** ⇒ Exploit **dynamic binding** !

17 of 19

Index (1)

Abstract Class (1)
Abstract Class (2)
Abstract Class (3)
Abstract Class (4)
Abstract Class (5)
Abstract Class (6)
Abstract Class (7.1)
Abstract Class (7.2)
Abstract Class (8)
Interface (1.1)
Interface (1.2)
Interface (2)
Interface (3)
Interface (4)

19 of 19

Abstract Classes vs. Interfaces: When to Use Which?

- Use **interfaces** when:
 - There is a **common set of functionalities** that can be implemented via **a variety of strategies**.
e.g., Interface `Point` declares signatures of `getX()` and `getY()`.
 - Each descendant class represents a different implementation strategy for the same set of functionalities.
 - `CartesianPoint` and `PolarPoint` represent different strategies for supporting `getX()` and `getY()`.
- Use **abstract classes** when:
 - **Some (not all) implementations can be shared** by descendants, and **some (not all) implementations cannot be shared**.
e.g., Abstract class `Polygon`:
 - Defines implementation of `getPerimeter`, to be shared by `Rectangle` and `Triangle`.
 - Declares signature of `getArea`, to be implemented by `Rectangle` and `Triangle`.

18 of 19

Index (2)

Interface (5)

Interface (6)

Abstract Classes vs. Interfaces:
When to Use Which?

20 of 19

Recursion



EECS2030 B: Advanced
Object Oriented Programming
Fall 2018

CHEN-WEI WANG



Recursion: Principle

- **Recursion** is useful in expressing solutions to problems that can be **recursively** defined:
 - **Base Cases:** Small problem instances immediately solvable.
 - **Recursive Cases:**
 - Large problem instances *not immediately solvable*.
 - Solve by reusing *solution(s) to strictly smaller problem instances*.
- Similar idea learnt in high school: [**mathematical induction**]
- Recursion can be easily expressed programmatically in Java:

```
m(i) {  
  if(i == ...) { /* base case: do something directly */ }  
  else {  
    m(j); /* recursive call with strictly smaller value */  
  }  
}
```

- In the body of a method m , there might be *a call or calls to m itself*.
- Each such self-call is said to be a **recursive call**.
- Inside the execution of $m(i)$, a recursive call $m(j)$ must be that $j < i$.

3 of 47

Beyond this lecture ...



- Fantastic resources for sharpening your recursive skills for the exam:

<http://codingbat.com/java/Recursion-1>

<http://codingbat.com/java/Recursion-2>

- The **best** approach to learning about recursion is via a functional programming language:

Haskell Tutorial: <https://www.haskell.org/tutorial/>

2 of 47

Tracing Method Calls via a Stack



- When a method is called, it is **activated** (and becomes **active**) and **pushed** onto the stack.
- When the body of a method makes a (helper) method call, that (helper) method is **activated** (and becomes **active**) and **pushed** onto the stack.
 - ⇒ The stack contains activation records of all **active** methods.
 - **Top** of stack denotes the **current point of execution**.
 - Remaining parts of stack are (temporarily) **suspended**.
- When entire body of a method is executed, stack is **popped**.
 - ⇒ The **current point of execution** is returned to the new **top** of stack (which was **suspended** and just became **active**).
- Execution terminates when the stack becomes **empty**.

4 of 47

Recursion: Factorial (1)

- Recall the formal definition of calculating the n factorial:

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ n \cdot (n-1) \cdot (n-2) \cdot \dots \cdot 3 \cdot 2 \cdot 1 & \text{if } n \geq 1 \end{cases}$$

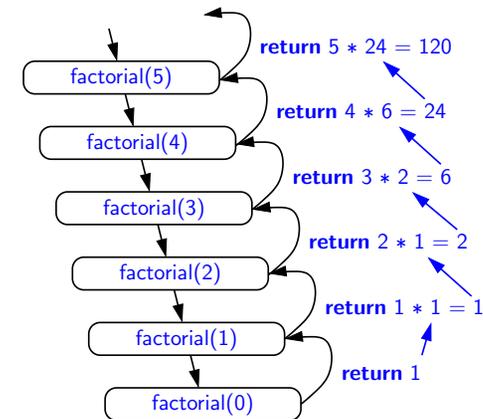
- How do you define the same problem *recursively*?

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ n \cdot (n-1)! & \text{if } n \geq 1 \end{cases}$$

- To solve $n!$, we combine n and the solution to $(n-1)!$.

```
int factorial(int n) {
    int result;
    if(n == 0) { /* base case */ result = 1; }
    else { /* recursive case */
        result = n * factorial(n - 1);
    }
    return result;
}
```

Recursion: Factorial (2)



Common Errors of Recursive Methods

- Missing Base Case(s).

```
int factorial(int n) {
    return n * factorial(n - 1);
}
```

Base case(s) are meant as points of stopping growing the runtime stack.

- Recursive Calls on Non-Smaller Problem Instances.

```
int factorial(int n) {
    if(n == 0) { /* base case */ return 1; }
    else { /* recursive case */ return n * factorial(n); }
}
```

Recursive calls on **strictly smaller** problem instances are meant for moving gradually towards the base case(s).

- In both cases, a `StackOverflowException` will be thrown.

Recursion: Factorial (3)

- When running *factorial(5)*, a *recursive call factorial(4)* is made. Call to *factorial(5)* suspended until *factorial(4)* returns a value.
- When running *factorial(4)*, a *recursive call factorial(3)* is made. Call to *factorial(4)* suspended until *factorial(3)* returns a value.
- ...
- factorial(0)* returns 1 back to *suspended call factorial(1)*.
- factorial(1)* receives 1 from *factorial(0)*, multiplies 1 to it, and returns 1 back to the *suspended call factorial(2)*.
- factorial(2)* receives 1 from *factorial(1)*, multiplies 2 to it, and returns 2 back to the *suspended call factorial(3)*.
- factorial(3)* receives 2 from *factorial(1)*, multiplies 3 to it, and returns 6 back to the *suspended call factorial(4)*.
- factorial(4)* receives 6 from *factorial(3)*, multiplies 4 to it, and returns 24 back to the *suspended call factorial(5)*.
- factorial(5)* receives 24 from *factorial(4)*, multiplies 5 to it, and returns 120 as the result.

Recursion: Factorial (4)



- When the execution of a method (e.g., *factorial(5)*) leads to a nested method call (e.g., *factorial(4)*):
 - The execution of the current method (i.e., *factorial(5)*) is *suspended*, and a structure known as an *activation record* or *activation frame* is created to store information about the progress of that method (e.g., values of parameters and local variables).
 - The nested methods (e.g., *factorial(4)*) may call other nested methods (*factorial(3)*).
 - When all nested methods complete, the activation frame of the *latest suspended* method is re-activated, then continue its execution.
- What kind of data structure does this activation-suspension process correspond to? [LIFO Stack]

9 of 47

Recursion: Fibonacci (2)



```
fib(5)
= {fib(5) = fib(4) + fib(3); push(fib(5)); suspended: {fib(5)}; active: fib(4)}
fib(4) + fib(3)
= {fib(4) = fib(3) + fib(2); suspended: {fib(4), fib(5)}; active: fib(3)}
  (fib(3) + fib(2)) + fib(3)
= {fib(3) = fib(2) + fib(1); suspended: {fib(3), fib(4), fib(5)}; active: fib(2)}
  ((fib(2) + fib(1)) + fib(2)) + fib(3)
= {fib(2) returns 1; suspended: {fib(3), fib(4), fib(5)}; active: fib(1)}
  ((1 + fib(1)) + fib(2)) + fib(3)
= {fib(1) returns 1; suspended: {fib(3), fib(4), fib(5)}; active: fib(3)}
  ((1 + 1) + fib(2)) + fib(3)
= {fib(3) returns 1 + 1; pop(); suspended: {fib(4), fib(5)}; active: fib(2)}
  (2 + fib(2)) + fib(3)
= {fib(2) returns 1; suspended: {fib(4), fib(5)}; active: fib(4)}
  (2 + 1) + fib(3)
= {fib(4) returns 2 + 1; pop(); suspended: {fib(5)}; active: fib(3)}
  3 + fib(3)
= {fib(3) = fib(2) + fib(1); suspended: {fib(3), fib(5)}; active: fib(2)}
  3 + (fib(2) + fib(1))
= {fib(2) returns 1; suspended: {fib(3), fib(5)}; active: fib(1)}
  3 + (1 + fib(1))
= {fib(1) returns 1; suspended: {fib(3), fib(5)}; active: fib(3)}
  3 + (1 + 1)
= {fib(3) returns 1 + 1; pop(); suspended: {fib(5)}; active: fib(5)}
  3 + 2
= {fib(5) returns 3 + 2; suspended: {}}
= 5
```

11 of 47⁵

Recursion: Fibonacci (1)



Recall the formal definition of calculating the n_{th} number in a Fibonacci series (denoted as F_n), which is already itself recursive:

$$F_n = \begin{cases} 1 & \text{if } n = 1 \\ 1 & \text{if } n = 2 \\ F_{n-1} + F_{n-2} & \text{if } n > 2 \end{cases}$$

```
int fib(int n) {
    int result;
    if(n == 1) { /* base case */ result = 1; }
    else if(n == 2) { /* base case */ result = 1; }
    else { /* recursive case */
        result = fib(n - 1) + fib(n - 2);
    }
    return result;
}
```

10 of 47

Java Library: String



```
public class StringTester {
    public static void main(String[] args) {
        String s = "abcd";
        System.out.println(s.isEmpty()); /* false */
        /* Characters in index range [0, 0) */
        String t0 = s.substring(0, 0);
        System.out.println(t0); /* "" */
        /* Characters in index range [0, 4) */
        String t1 = s.substring(0, 4);
        System.out.println(t1); /* "abcd" */
        /* Characters in index range [1, 3) */
        String t2 = s.substring(1, 3);
        System.out.println(t2); /* "bc" */
        String t3 = s.substring(0, 2) + s.substring(2, 4);
        System.out.println(s.equals(t3)); /* true */
        for(int i = 0; i < s.length(); i++) {
            System.out.print(s.charAt(i));
        }
        System.out.println();
    }
}
```

12 of 47

Recursion: Palindrome (1)



Problem: A palindrome is a word that reads the same forwards and backwards. Write a method that takes a string and determines whether or not it is a palindrome.

```
System.out.println(isPalindrome("")); true
System.out.println(isPalindrome("a")); true
System.out.println(isPalindrome("madam")); true
System.out.println(isPalindrome("racecar")); true
System.out.println(isPalindrome("man")); false
```

Base Case 1: Empty string → Return *true* immediately.

Base Case 2: String of length 1 → Return *true* immediately.

Recursive Case: String of length ≥ 2 →

- 1st and last characters match, **and**
- *the rest (i.e., middle) of the string is a palindrome*.

13 of 47

Recursion: Reverse of String (1)



Problem: The reverse of a string is written backwards. Write a method that takes a string and returns its reverse.

```
System.out.println(reverseOf("")); /* "" */
System.out.println(reverseOf("a")); "a"
System.out.println(reverseOf("ab")); "ba"
System.out.println(reverseOf("abc")); "cba"
System.out.println(reverseOf("abcd")); "dcba"
```

Base Case 1: Empty string → Return *empty string*.

Base Case 2: String of length 1 → Return *that string*.

Recursive Case: String of length ≥ 2 →

- 1) Head of string (i.e., first character)
- 2) Reverse of the tail of string (i.e., all but the first character)

Return the concatenation of 1) and 2).

15 of 47

Recursion: Palindrome (2)



```
boolean isPalindrome(String word) {
    if(word.length() == 0 || word.length() == 1) {
        /* base case */
        return true;
    }
    else {
        /* recursive case */
        char firstChar = word.charAt(0);
        char lastChar = word.charAt(word.length() - 1);
        String middle = word.substring(1, word.length() - 1);
        return
            firstChar == lastChar
            /* See the API of java.lang.String.substring. */
            && isPalindrome(middle);
    }
}
```

14 of 47

Recursion: Reverse of a String (2)



```
String reverseOf(String s) {
    if(s.isEmpty()) { /* base case 1 */
        return "";
    }
    else if(s.length() == 1) { /* base case 2 */
        return s;
    }
    else { /* recursive case */
        String tail = s.substring(1, s.length());
        String reverseOfTail = reverseOf(tail);
        char head = s.charAt(0);
        return reverseOfTail + head;
    }
}
```

16 of 47

Recursion: Number of Occurrences (1)



Problem: Write a method that takes a string s and a character c , then count the number of occurrences of c in s .

```
System.out.println(occurrencesOf("", 'a')); /* 0 */
System.out.println(occurrencesOf("a", 'a')); /* 1 */
System.out.println(occurrencesOf("b", 'a')); /* 0 */
System.out.println(occurrencesOf("baaba", 'a')); /* 3 */
System.out.println(occurrencesOf("baaba", 'b')); /* 2 */
System.out.println(occurrencesOf("baaba", 'c')); /* 0 */
```

Base Case: Empty string \rightarrow Return 0 .

Recursive Case: String of length $\geq 1 \rightarrow$

- 1) Head of s (i.e., first character)
- 2) Number of occurrences of c in the tail of s (i.e., all but the first character)

If head is equal to c , return $1 + 2$.

If head is not equal to c , return $0 + 2$.

17 of 47

Making Recursive Calls on an Array



- Recursive calls denote solutions to *smaller* sub-problems.
- *Naively*, explicitly create a new, smaller array:

```
void m(int[] a) {
    if(a.length == 0) { /* base case */ }
    else if(a.length == 1) { /* base case */ }
    else {
        int[] sub = new int[a.length - 1];
        for(int i = 1; i < a.length; i++) { sub[0] = a[i - 1]; }
        m(sub) } }
```

- For *efficiency*, we pass the *reference* of the same array and specify the *range of indices* to be considered:

```
void m(int[] a, int from, int to) {
    if(from > to) { /* base case */ }
    else if(from == to) { /* base case */ }
    else { m(a, from + 1, to) } }
```

- $m(a, 0, a.length - 1)$ [Initial call; entire array]
- $m(a, 1, a.length - 1)$ [1st r.c. on array of size $a.length - 1$]
- $m(a, a.length - 1, a.length - 1)$ [Last r.c. on array of size 1]

19 of 47

Recursion: Number of Occurrences (2)



```
int occurrencesOf(String s, char c) {
    if(s.isEmpty()) {
        /* Base Case */
        return 0;
    }
    else {
        /* Recursive Case */
        char head = s.charAt(0);
        String tail = s.substring(1, s.length());
        if(head == c) {
            return 1 + occurrencesOf(tail, c);
        }
        else {
            return 0 + occurrencesOf(tail, c);
        }
    }
}
```

18 of 47

Recursion: All Positive (1)



Problem: Determine if an array of integers are all positive.

```
System.out.println(allPositive({})); /* true */
System.out.println(allPositive({1, 2, 3, 4, 5})); /* true */
System.out.println(allPositive({1, 2, -3, 4, 5})); /* false */
```

Base Case: Empty array \rightarrow Return *true* immediately.

The base case is *true* \because we can *not* find a counter-example (i.e., a number *not* positive) from an empty array.

Recursive Case: Non-Empty array \rightarrow

- 1st element positive, **and**
- *the rest of the array is all positive*.

Exercise: Write a method `boolean somePositive(int[] a)` which *recursively* returns *true* if there is some positive number in a , and *false* if there are no positive numbers in a .

Hint: What to return in the base case of an empty array? [*false*] \because No witness (i.e., a positive number) from an empty array

20 of 47

Recursion: All Positive (2)



```
boolean allPositive(int[] a) {
    return allPositiveHelper(a, 0, a.length - 1);
}

boolean allPositiveHelper(int[] a, int from, int to) {
    if (from > to) { /* base case 1: empty range */
        return true;
    }
    else if (from == to) { /* base case 2: range of one element */
        return a[from] > 0;
    }
    else { /* recursive case */
        return a[from] > 0 && allPositiveHelper(a, from + 1, to);
    }
}
```

21 of 47

Recursion: Is an Array Sorted? (2)



```
boolean isSorted(int[] a) {
    return isSortedHelper(a, 0, a.length - 1);
}

boolean isSortedHelper(int[] a, int from, int to) {
    if (from > to) { /* base case 1: empty range */
        return true;
    }
    else if (from == to) { /* base case 2: range of one element */
        return true;
    }
    else {
        return a[from] <= a[from + 1]
            && isSortedHelper(a, from + 1, to);
    }
}
```

23 of 47

Recursion: Is an Array Sorted? (1)



Problem: Determine if an array of integers are sorted in a non-descending order.

```
System.out.println(isSorted({})); true
System.out.println(isSorted({1, 2, 2, 3, 4})); true
System.out.println(isSorted({1, 2, 2, 1, 3})); false
```

Base Case: Empty array → Return *true* immediately.

The base case is *true* ∴ we can *not* find a counter-example (i.e., a pair of adjacent numbers that are *not* sorted in a non-descending order) from an empty array.

Recursive Case: Non-Empty array →

- 1st and 2nd elements are sorted in a non-descending order, **and**
- **the rest of the array**, starting from the 2nd element, **are sorted in a non-descending positive**.

22 of 47

Recursive Methods: Correctness Proofs



```
1 boolean allPositive(int[] a) { return allPosH(a, 0, a.length - 1); }
2 boolean allPosH(int[] a, int from, int to) {
3     if (from > to) { return true; }
4     else if (from == to) { return a[from] > 0; }
5     else { return a[from] > 0 && allPosH(a, from + 1, to); } }
```

- Via mathematical induction, prove that allPosH is correct:

Base Cases

- In an empty array, there is no non-positive number ∴ result is *true*. [L3]
- In an array of size 1, the only one elements determines the result. [L4]

Inductive Cases

- **Inductive Hypothesis:** allPosH(a, from + 1, to) returns *true* if a[from + 1], a[from + 2], ..., a[to] are all positive; *false* otherwise.
- allPosH(a, from, to) should return *true* if: **1)** a[from] is positive; **and 2)** a[from + 1], a[from + 2], ..., a[to] are all positive.
- By **I.H.**, result is $a[from] > 0 \wedge \text{allPosH}(a, \text{from} + 1, \text{to})$. [L5]

- allPositive(a) is correct by invoking allPosH(a, 0, a.length - 1), examining the entire array. [L1]

24 of 47

Recursion: Binary Search (1)

• Searching Problem

Input: A number a and a **sorted** list of n numbers $\langle a_1, a_2, \dots, a_n \rangle$ such that $a'_1 \leq a'_2 \leq \dots \leq a'_n$

Output: Whether or not a exists in the input list

• An Efficient Recursive Solution

Base Case: Empty list \rightarrow *False*.

Recursive Case: List of size $\geq 1 \rightarrow$

- **Compare** the *middle* element against a .
 - All elements to the left of *middle* are $\leq a$
 - All elements to the right of *middle* are $\geq a$
- If the *middle* element *is* equal to $a \rightarrow$ *True*.
- If the *middle* element *is not* equal to a :
 - If $a < middle$, recursively find a on the left half.
 - If $a > middle$, recursively find a on the right half.

Running Time: Binary Search (1)

We use $T(n)$ to denote the running time function of a binary search, where n is the size of the input array.

$$\begin{cases} T(0) = 1 \\ T(1) = 1 \\ T(n) = T(\frac{n}{2}) + 1 \text{ where } n \geq 2 \end{cases}$$

To solve this recurrence relation, we study the pattern of $T(n)$ and observe how it reaches the *base case(s)*.

Recursion: Binary Search (2)

```
boolean binarySearch(int[] sorted, int key) {
    return binarySearchHelper(sorted, 0, sorted.length - 1, key);
}
boolean binarySearchHelper(int[] sorted, int from, int to, int key) {
    if (from > to) { /* base case 1: empty range */
        return false; }
    else if (from == to) { /* base case 2: range of one element */
        return sorted[from] == key; }
    else {
        int middle = (from + to) / 2;
        int middleValue = sorted[middle];
        if (key < middleValue) {
            return binarySearchHelper(sorted, from, middle - 1, key);
        }
        else if (key > middleValue) {
            return binarySearchHelper(sorted, middle + 1, to, key);
        }
        else { return true; }
    }
}
```

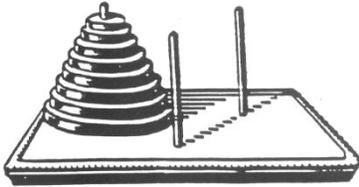
Running Time: Binary Search (2)

Without loss of generality, assume $n = 2^i$ for some non-negative i .

$$\begin{aligned} T(n) &= T(\frac{n}{2}) + 1 \\ &= \underbrace{(T(\frac{n}{4}) + 1)}_{T(\frac{n}{2})} + \underbrace{1}_{1 \text{ time}} \\ &= \underbrace{((T(\frac{n}{8}) + 1) + 1)}_{T(\frac{n}{4})} + \underbrace{1}_{2 \text{ times}} \\ &= \dots \\ &= (((\underbrace{1}_{T(\frac{n}{2 \log n})} + 1) \dots) + 1)_{\log n \text{ times}} \end{aligned}$$

$\therefore T(n)$ is $O(\log n)$

Tower of Hanoi: Specification



- **Given:** A tower of 8 disks, initially stacked in decreasing size on one of 3 pegs
- **Rules:**
 - Move only one disk at a time
 - Never move a larger disk onto a smaller one
- **Problem:** Transfer the entire tower to one of the other pegs.

Tower of Hanoi: A Recursive Solution

The general, recursive solution requires 3 steps:

1. Transfer the $n - 1$ smallest disks to a different peg.
2. Move the largest to the remaining free peg.
3. Transfer the $n - 1$ disks back onto the largest disk.

Tower of Hanoi in Java (1)

```
void towerOfHanoi(String[] disks) {
    tohHelper(disks, 0, disks.length - 1, 1, 3);
}
void tohHelper(String[] disks, int from, int to, int ori, int des) {
    if(from > to) { }
    else if(from == to) {
        print("move " + disks[to] + " from " + ori + " to " + des);
    }
    else {
        int intermediate = 6 - ori - des;
        tohHelper(disks, from, to - 1, ori, intermediate);
        print("move " + disks[to] + " from " + ori + " to " + des);
        tohHelper(disks, from, to - 1, intermediate, des);
    }
}
```

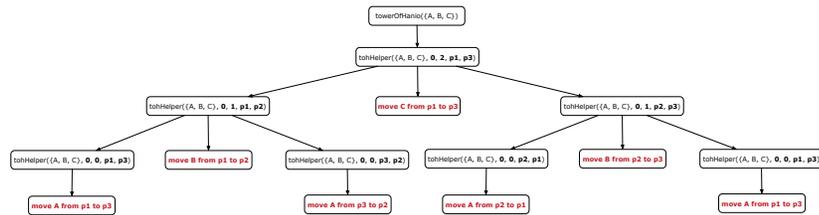
- `tohHelper(disks, from, to, ori, des)` moves disks $\{disks[from], disks[from + 1], \dots, disks[to]\}$ from peg ori to peg des .
- Peg id's are 1, 2, and 3 \Rightarrow The intermediate one is $6 - ori - des$.

Tower of Hanoi in Java (2)

Say ds (disks) is $\{A, B, C\}$, where $A < B < C$.

$$tohH(ds, \underbrace{0, 2}_{\{A, B, C\}}, p1, p3) = \left\{ \begin{array}{l} \text{Move C: } p1 \text{ to } p3 \\ tohH(ds, \underbrace{0, 1}_{\{A, B\}}, p1, p2) = \left\{ \begin{array}{l} tohH(ds, 0, 0, p1, p3) = \{ \text{Move A: } p1 \text{ to } p3 \\ \underbrace{\{A\}} \\ \text{Move B: } p1 \text{ to } p2 \\ tohH(ds, 0, 0, p3, p2) = \{ \text{Move A: } p3 \text{ to } p2 \\ \underbrace{\{A\}} \end{array} \right. \\ tohH(ds, \underbrace{0, 1}_{\{A, B\}}, p2, p3) = \left\{ \begin{array}{l} tohH(ds, 0, 0, p2, p1) = \{ \text{Move A: } p2 \text{ to } p1 \\ \underbrace{\{A\}} \\ \text{Move B: } p2 \text{ to } p3 \\ tohH(ds, 0, 0, p1, p3) = \{ \text{Move A: } p1 \text{ to } p3 \\ \underbrace{\{A\}} \end{array} \right. \end{array} \right.$$

Tower of Hanoi in Java (3)



Running Time: Tower of Hanoi (1)

- Generalize the problem by considering n disks.
- Let $T(n)$ denote the number of moves required to transfer n disks from one to another under the rules.
- Recall the general solution pattern:
 1. Transfer the $n - 1$ smallest disks to a different peg.
 2. Move the largest to the remaining free peg.
 3. Transfer the $n - 1$ disks back onto the largest disk.
- We end up with the following recurrence relation that allows us to compute T_n for any n we like:

$$\begin{cases} T(1) = 1 \\ T(n) = 2 \times T(n-1) + 1 \quad \text{where } n > 0 \end{cases}$$

- To solve this recurrence relation, we study the pattern of $T(n)$ and observe how it reaches the base case(s).

Running Time: Tower of Hanoi (2)

$$\begin{aligned} T(n) &= 2 \times T(n-1) + 1 \\ &= 2 \times \underbrace{(2 \times T(n-2) + 1)}_{T(n-1)} + 1 \\ &= 2 \times \underbrace{(2 \times (2 \times T(n-3) + 1) + 1)}_{T(n-2)} + 1 \\ &= \dots \\ &= 2 \times \underbrace{(2 \times (2 \times (\dots \times (2 \times T(1) + 1) + \dots) + 1) + 1)}_{T(n-3)} + 1 \\ &= 2^{n-1} + (n-1) \end{aligned}$$

$\therefore T(n)$ is $O(2^n)$

Recursion: Merge Sort

• Sorting Problem

Input: A list of n numbers $\langle a_1, a_2, \dots, a_n \rangle$

Output: A permutation (reordering) $\langle a'_1, a'_2, \dots, a'_n \rangle$ of the input list such that $a'_1 \leq a'_2 \leq \dots \leq a'_n$

• Recursive Solution

Base Case 1: Empty list \rightarrow Automatically sorted.

Base Case 2: List of size 1 \rightarrow Automatically sorted.

Recursive Case: List of size $\geq 2 \rightarrow$

- Split the list into two (unsorted) halves: L and R ;
- **Recursively** sort L and R : $sortedL$ and $sortedR$;
- Return the **merge** of $sortedL$ and $sortedR$.

Recursion: Merge Sort in Java (1)

```

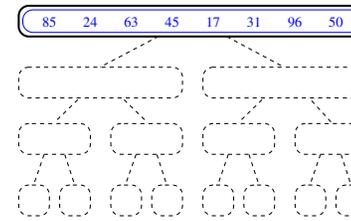
/* Assumption: L and R are both already sorted. */
private List<Integer> merge(List<Integer> L, List<Integer> R) {
    List<Integer> merge = new ArrayList<>();
    if(L.isEmpty() || R.isEmpty()) { merge.addAll(L); merge.addAll(R); }
    else {
        int i = 0;
        int j = 0;
        while(i < L.size() && j < R.size()) {
            if(L.get(i) <= R.get(j)) { merge.add(L.get(i)); i++; }
            else { merge.add(R.get(j)); j++; }
        }
        /* If i >= L.size(), then this for loop is skipped. */
        for(int k = i; k < L.size(); k++) { merge.add(L.get(k)); }
        /* If j >= R.size(), then this for loop is skipped. */
        for(int k = j; k < R.size(); k++) { merge.add(R.get(k)); }
    }
    return merge;
}
    
```

RT(merge)?

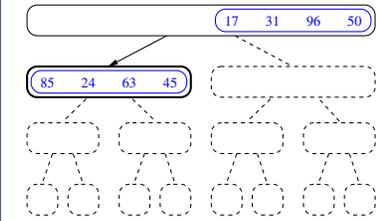
[O(n)]

Recursion: Merge Sort Example (1)

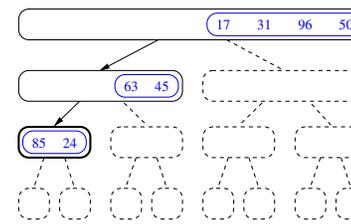
(1) Start with input list of size 8



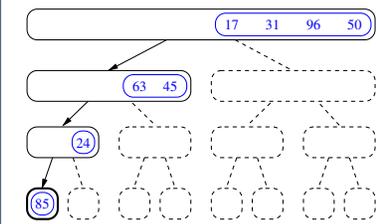
(2) Split and recur on L of size 4



(3) Split and recur on L of size 2



(4) Split and recur on L of size 1, return



Recursion: Merge Sort in Java (2)

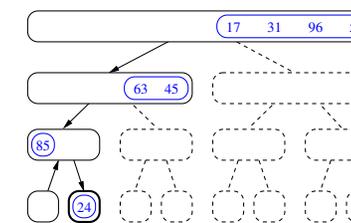
```

public List<Integer> sort(List<Integer> list) {
    List<Integer> sortedList;
    if(list.size() == 0) { sortedList = new ArrayList<>(); }
    else if(list.size() == 1) {
        sortedList = new ArrayList<>();
        sortedList.add(list.get(0));
    }
    else {
        int middle = list.size() / 2;
        List<Integer> left = list.subList(0, middle);
        List<Integer> right = list.subList(middle, list.size());
        List<Integer> sortedLeft = sort(left);
        List<Integer> sortedRight = sort(right);
        sortedList = merge(sortedLeft, sortedRight);
    }
    return sortedList;
}
    
```

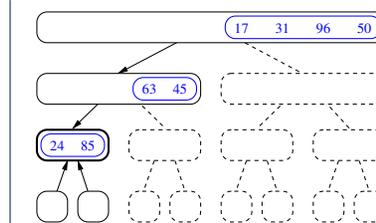
$$RT(\text{sort}) = \underbrace{RT(\text{merge})}_{O(n)} \times \underbrace{\# \text{ splits until size 0 or 1}}_{O(\log n)}$$

Recursion: Merge Sort Example (2)

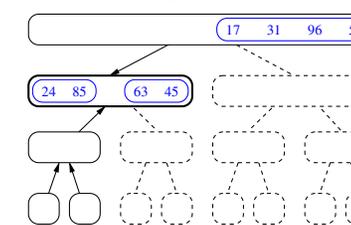
(5) Recur on R of size 1 and return



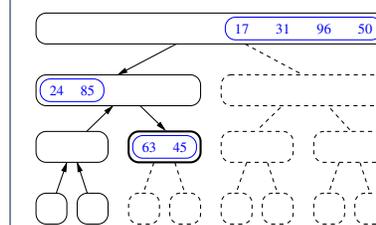
(6) Merged sorted L and R of sizes 1



(7) Return merged list of size 2

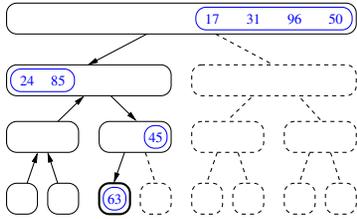


(8) Recur on R of size 2

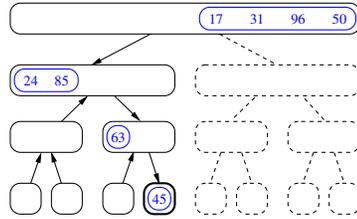


Recursion: Merge Sort Example (3)

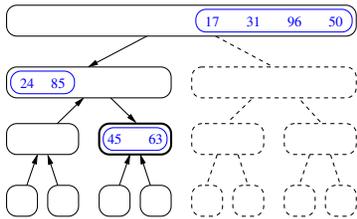
(9) Split and recur on L of size 1, *return*



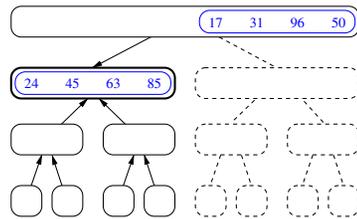
(10) Recur on R of size 1, *return*



(11) Merge sorted L and R of sizes 1, *return*

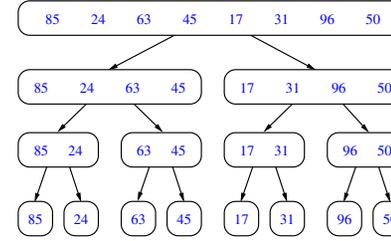


(12) Merge sorted L and R of sizes 2

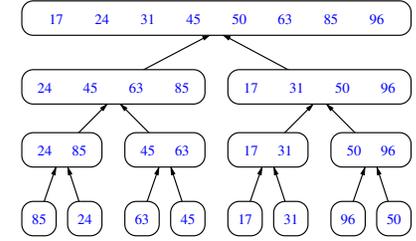


Recursion: Merge Sort Example (5)

(1) Recursion trees of *unsorted* lists

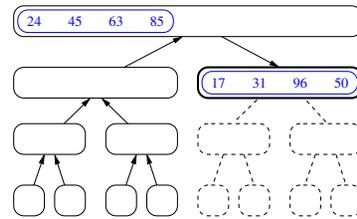


(2) Recursion trees of *sorted* lists

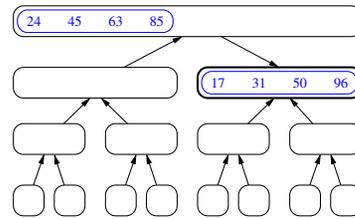


Recursion: Merge Sort Example (4)

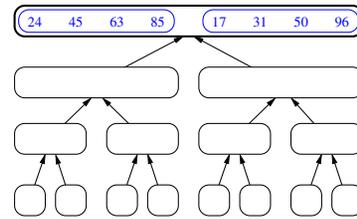
(13) Recur on R of size 4



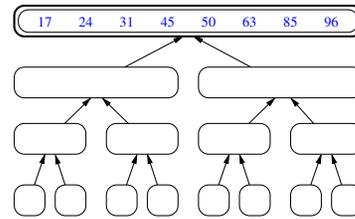
(14) *Return* a sorted list of size 4



(15) Merge sorted L and R of sizes 4



(16) *Return* a sorted list of size 8



Recursion: Merge Sort Running Time (1)

Base Case 1: Empty list \rightarrow Automatically sorted. [$O(1)$]

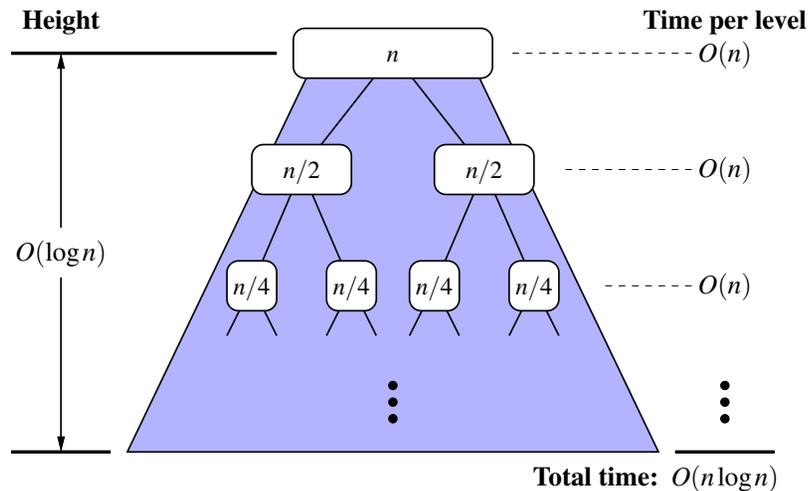
Base Case 2: List of size 1 \rightarrow Automatically sorted. [$O(1)$]

Recursive Case: List of size $\geq 2 \rightarrow$

- Split the list into two (unsorted) halves: L and R ; [$O(1)$]
- Recursively** sort L and R : $sortedL$ and $sortedR$;
How many times to split until L and R have size 0 or 1? [$O(\log n)$]
- Return the **merge** of $sortedL$ and $sortedR$. [$O(n)$]

$$\begin{aligned}
 & \mathbf{RT} \\
 = & (\mathbf{RT} \text{ each RC}) \times (\# \mathbf{RCs}) \\
 = & (\mathbf{RT} \text{ merging } sortedL \text{ and } sortedR) \times (\# \text{ splits until bases}) \\
 = & n \cdot \log n
 \end{aligned}$$

Recursion: Merge Sort Running Time (2)



45 of 47

Index (1)

Beyond this lecture ...
Recursion: Principle
Tracing Method Calls via a Stack
Recursion: Factorial (1)
Common Errors of Recursive Methods
Recursion: Factorial (2)
Recursion: Factorial (3)
Recursion: Factorial (4)
Recursion: Fibonacci (1)
Recursion: Fibonacci (2)
Java Library: String
Recursion: Palindrome (1)
Recursion: Palindrome (2)
Recursion: Reverse of a String (1)

47 of 47

Beyond this lecture ...

- Notes on Recursion:
http://www.eecs.yorku.ca/~jackie/teaching/lectures/2017/F/EECS2030/slides/EECS2030_F17_Notes_Recursion.pdf
- API for String:
<https://docs.oracle.com/javase/8/docs/api/java/lang/String.html>
- Fantastic resources for sharpening your recursive skills for the exam:
<http://codingbat.com/java/Recursion-1>
<http://codingbat.com/java/Recursion-2>
- The **best** approach to learning about recursion is via a functional programming language:
Haskell Tutorial: <https://www.haskell.org/tutorial/>

46 of 47

Index (2)

Recursion: Reverse of a String (2)
Recursion: Number of Occurrences (1)
Recursion: Number of Occurrences (2)
Making Recursive Calls on an Array
Recursion: All Positive (1)
Recursion: All Positive (2)
Recursion: Is an Array Sorted? (1)
Recursion: Is an Array Sorted? (2)
Recursive Methods: Correctness Proofs
Recursion: Binary Search (1)
Recursion: Binary Search (2)
Running Time: Binary Search (1)
Running Time: Binary Search (2)
Tower of Hanoi: Specification

48 of 47

Index (3)

- Tower of Hanoi: A Recursive Solution
- Tower of Hanoi in Java (1)
- Tower of Hanoi in Java (2)
- Tower of Hanoi in Java (3)
- Running Time: Tower of Hanoi (1)
- Running Time: Tower of Hanoi (2)
- Recursion: Merge Sort
- Recursion: Merge Sort in Java (1)
- Recursion: Merge Sort in Java (2)
- Recursion: Merge Sort Example (1)
- Recursion: Merge Sort Example (2)
- Recursion: Merge Sort Example (3)
- Recursion: Merge Sort Example (4)
- Recursion: Merge Sort Example (5)

49 of 47

Index (4)

- Recursion: Merge Sort Running Time (1)

- Recursion: Merge Sort Running Time (2)

Beyond this lecture ...

50 of 47

Generics in Java

Motivating Example: A Book of Objects

```
1 class Book {
2   String[] names;
3   Object[] records;
4   /* add a name-record pair to the book */
5   void add (String name, Object record) { ... }
6   /* return the record associated with a given name */
7   Object get (String name) { ... } }
```

Question: Which line has a type error?

```
1 Date birthday; String phoneNumber;
2 Book b; boolean isWednesday;
3 b = new Book();
4 phoneNumber = "416-67-1010";
5 b.add ("Suyeon", phoneNumber);
6 birthday = new Date(1975, 4, 10);
7 b.add ("Yuna", birthday);
8 isWednesday = b.get("Yuna").getDay() == 4;
```

2 of 21

Motivating Example: Observations (1)



- In the `Book` class:
 - By declaring the attribute

```
Object[] records
```

We meant that each book instance may store any object whose *static type* is a **descendant class** of `Object`.

- Accordingly, from the return type of the `get` method, we only know that the returned record is an `Object`, but not certain about its *dynamic type* (e.g., `Date`, `String`, etc.).
 - ∴ a record retrieved from the book, e.g., `b.get("Yuna")`, may only be called upon methods in its *static type* (i.e., `Object`).
- In the tester code of the `Book` class:
 - In **Line 1**, the *static types* of variables `birthday` (i.e., `Date`) and `phoneNumber` (i.e., `String`) are **descendant classes** of `Object`.
 - So, **Line 5** and **Line 7** compile.

3 of 21

Motivating Example: Observations (2.1)



- It seems: combining *instanceof check* and *type cast* works.
- Can you see any potential problem(s)?
- **Hints:** What happens when you have a large number of records of distinct *dynamic types* stored in the book (e.g., `Date`, `String`, `Person`, `Account`, etc.)?

5 of 21

Motivating Example: Observations (2)



Due to **polymorphism**, the *dynamic types* of stored objects (e.g., `phoneNumber` and `birthday`) need not be the same.

- Methods supported in the *dynamic types* (e.g., method `getDay` of class `Date`) may be new methods not inherited from `Object`.
- This is why **Line 8** would fail to compile, and may be fixed using an explicit **cast**:

```
isWednesday = ((Date) b.get("Yuna")).getDay() == 4;
```

- But what if the *dynamic type* of the returned object is not a `Date`?

```
isWednesday = ((Date) b.get("Suyeon")).getDay() == 4;
```

- To avoid such a `ClassCastException` at runtime, we need to check its *dynamic type* before performing a cast:

```
if (b.get("Suyeon") instanceof Date) {  
    isWednesday = ((Date) b.get("Suyeon")).getDay() == 4;  
}
```

4 of 21

Motivating Example: Observations (2.2)



Imagine that the tester code (or an application) stores 100 different record objects into the book.

- All of these records are of *static type* `Object`, but of distinct *dynamic types*.

```
Object rec1 = new C1(); b.add(..., rec1);  
Object rec2 = new C2(); b.add(..., rec2);  
...  
Object rec100 = new C100(); b.add(..., rec100);
```

where classes `C1` to `C100` are **descendant classes** of `Object`.

- **Every time** you retrieve a record from the book, you need to check "exhaustively" on its *dynamic type* before calling some method(s).

```
Object rec = b.get("Jim");  
if (rec instanceof C1) { ((C1) rec).m1; }  
...  
else if (rec instanceof C100) { ((C100) rec).m100; }
```

- Writing out this list multiple times is tedious and error-prone!

6 of 21

Motivating Example: Observations (3)



We need a solution that:

- Saves us from explicit `instanceof` checks and type casts
- Eliminates the occurrences of `ClassCastException`

As a sketch, this is how the solution looks like:

- When the user declares a `Book` object `b`, they must **commit to the kind of record that `b` stores at runtime**.
e.g., `b` stores either `Date` objects only or `String` objects only, but **not a mix**.
- When attempting to store a new record object `rec` into `b`, what if `rec`'s **static type** is not a **descendant class** of the type of book that the user previously commits to?
⇒ A **compilation error**
- When attempting to retrieve a record object from `b`, there is **no longer a need to check and cast**.
∴ **Static types** of all records in `b` are guaranteed to be the same.

7 of 21

Parameters



- In mathematics:
 - The same **function** is applied with different **argument values**.
e.g., $2 + 3$, $1 + 1$, $10 + 101$, *etc.*
 - We **generalize** these instance applications into a definition.
e.g., $+: (\mathbb{Z} \times \mathbb{Z}) \rightarrow \mathbb{Z}$ is a function that takes two integer **parameters** and returns an integer.
- In Java programming:
 - We want to call a **method**, with different **argument values**, to achieve a similar goal.
e.g., `acc.deposit(100)`, `acc.deposit(23)`, *etc.*
 - We generalize these possible method calls into a definition.
e.g., In class `Account`, a method `void deposit(int amount)` takes one integer **parameter**.
- When you design a mathematical function or a Java method, always consider the list of **parameters**, each of which representing a set of possible **argument values**.

8 of 21

Java Generics: Design of a Generic Book



```
class Book<E> {
    String[] names;
    E[] records;
    /* add a name-record pair to the book */
    void add (String name, E record) { ... }
    /* return the record associated with a given name */
    E get (String name) { ... } }
```

Question: Which line has a type error?

```
1 Date birthday; String phoneNumber;
2 Book<Date> b; boolean isWednesday;
3 b = new Book<Date>();
4 phoneNumber = "416-67-1010";
5 b.add ("Suyeon", phoneNumber);
6 birthday = new Date(1975, 4, 10);
7 b.add ("Yuna", birthday);
8 isWednesday = b.get("Yuna").getDay() == 4;
```

9 of 21

Java Generics: Observations



- In class `Book`:
 - At the class level, we **parameterize the type of records** that an instance of book may store: `class Book<E>`
where `E` is the name of a type parameter, which should be **instantiated** when the user declares an instance of `Book`.
 - Every occurrence of `Object` (the most general type of records) is replaced by `E`.
 - As soon as `E` at the class level is committed to some known type (e.g., `Date`, `String`, *etc.*), every occurrence of `E` will be replaced by that type.
- In the tester code of `Book`:
 - In **Line 2**, we commit that the book `b` will store `Date` objects only.
 - **Line 5** now fails to compile. [String is not a Date]
 - **Line 7** still compiles.
 - **Line 8** does **not need** any instance check and type cast, and does **not cause** any `ClassCastException`.
∴ Only `Date` objects were allowed to be stored.

10 of 21

Bad Example of using Generics

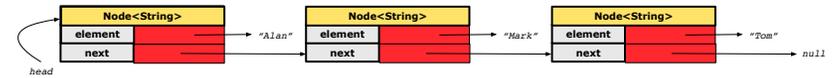
Has the following client made an appropriate choice?

```
Book<Object> book
```

NO!!!!!!!!!!!!!!!!!!!!!!

- It allows **all** kinds of objects to be stored.
 - ∴ All classes are descendants of **Object**.
- We can expect **very little** from an object retrieved from this book.
 - ∴ The **static type** of book's items are **Object**, root of the class hierarchy, has the **minimum** amount of features available for use.
 - ∴ Exhaustive list of casts are unavoidable.
 - [**bad** for extensibility and maintainability]

Generic Classes: Singly-Linked List (2)



Approach 1

```
Node<String> tom = new Node<>("Tom", null);
Node<String> mark = new Node<>("Mark", tom);
Node<String> alan = new Node<>("Alan", mark);
```

Approach 2

```
Node<String> alan = new Node<>("Alan", null);
Node<String> mark = new Node<>("Mark", null);
Node<String> tom = new Node<>("Tom", null);
alan.setNext(mark);
mark.setNext(tom);
```

Generic Classes: Singly-Linked List (1)

```
public class Node<E> {
    private E element;
    private Node<E> next;
    public Node(E e, Node<E> n) { element = e; next = n; }
    public E getElement() { return element; }
    public Node<E> getNext() { return next; }
    public void setNext(Node<E> n) { next = n; }
    public void setElement(E e) { element = e; }
}
```

```
public class SinglyLinkedList<E> {
    private Node<E> head;
    private Node<E> tail;
    private int size = null;
    public void addFirst(E e) { ... }
    Node<E> getNodeAt (int i) { ... }
    ...
}
```

Generic Classes: Singly-Linked List (3)

Assume we are in the context of class SinglyLinkedList.

```
void addFirst (E e) {
    head = new Node<E>(e, head);
    if (size == 0) { tail = head; }
    size ++;
}
```

```
Node<E> getNodeAt (int i) {
    if (i < 0 || i >= size) {
        throw new IllegalArgumentException("Invalid Index");
    }
    else {
        int index = 0;
        Node<E> current = head;
        while (index < i) {
            index ++; current = current.getNext();
        }
        return current;
    }
}
```

Generic Stack: Interface



```
public interface Stack<E> {
    public int size();
    public boolean isEmpty();
    public E top();
    public void push(E e);
    public E pop();
}
```

15 of 21

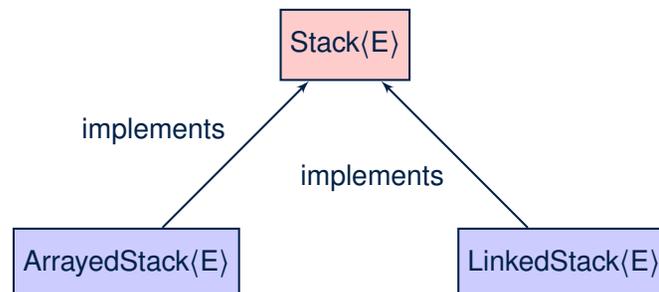
Generic Stack: Array Implementation



```
public class ArrayedStack<E> implements Stack<E> {
    private static final int MAX_CAPACITY = 1000;
    private E[] data;
    private int t; /* top index */
    public ArrayedStack() {
        data = (E[]) new Object[MAX_CAPACITY];
        t = -1;
    }
    public int size() { return (t + 1); }
    public boolean isEmpty() { return (t == -1); }
    public E top() {
        if (isEmpty()) { /* Error: Empty Stack. */ }
        else { return data[t]; }
    }
    public void push(E e) {
        if (size() == MAX_CAPACITY) { /* Error: Stack Full. */ }
        else { t++; data[t] = e; }
    }
    public E pop() {
        E result;
        if (isEmpty()) { /* Error: Empty Stack */ }
        else { result = data[t]; data[t] = null; t--; }
        return result;
    }
}
```

17 of 21

Generic Stack: Architecture



16 of 21

Generic Stack: SLL Implementation



```
public class LinkedStack<E> implements Stack<E> {
    private SinglyLinkedList<E> data;
    public LinkedStack() {
        data = new SinglyLinkedList<E>();
    }
    public int size() { return data.size(); }
    public boolean isEmpty() { return size() == 0; }
    public E top() {
        if (isEmpty()) { /* Error: Empty Stack. */ }
        else { return data.getFirst(); }
    }
    public void push(E e) {
        data.addFirst(e);
    }
    public E pop() {
        E result;
        if (isEmpty()) { /* Error: Empty Stack */ }
        else { result = top(); data.removeFirst(); }
        return result;
    }
}
```

18 of 21

Generic Stack: Testing Both Implementations



```
@Test
public void testPolymorphicStacks() {
    Stack<String> s = new ArrayedStack<>();
    s.push("Alan"); /* dynamic binding */
    s.push("Mark"); /* dynamic binding */
    s.push("Tom"); /* dynamic binding */
    assertTrue(s.size() == 3 && !s.isEmpty());
    assertEquals("Tom", s.top());

    s = new LinkedStack<>();
    s.push("Alan"); /* dynamic binding */
    s.push("Mark"); /* dynamic binding */
    s.push("Tom"); /* dynamic binding */
    assertTrue(s.size() == 3 && !s.isEmpty());
    assertEquals("Tom", s.top());
}
```

19 of 21

Beyond this lecture ...



- Study <https://docs.oracle.com/javase/tutorial/java/generics/index.html> for further details on Java generics.

20 of 21

Index (1)



Motivating Example: A Book of Objects
Motivating Example: Observations (1)
Motivating Example: Observations (2)
Motivating Example: Observations (2.1)
Motivating Example: Observations (2.2)
Motivating Example: Observations (3)
Parameters
Java Generics: Design of a Generic Book
Java Generics: Observations
Bad Example of using Generics
Generic Classes: Singly-Linked List (1)
Generic Classes: Singly-Linked List (2)
Generic Classes: Singly-Linked List (3)
Generic Stack: Interface

21 of 21

Index (2)



Generic Stack: Architecture

Generic Stack: Array Implementation

Generic Stack: SLL Implementation

Generic Stack: Testing Both Implementations

Beyond this lecture ...

22 of 21

Wrap-Up



EECS2030 B: Advanced
Object Oriented Programming
Fall 2018

CHEN-WEI WANG

What You Learned (1)



- *Procedural Programming in Java*
 - Exceptions
 - Recursion (implementation, running time, correctness)
- *Data Structures*
 - Arrays
 - Maps and Hash Tables

What You Learned (2)



- *Object-Oriented Programming in Java*
 - classes, attributes, encapsulation, objects, reference data types
 - methods: constructors, accessors, mutators, helper
 - dot notation, context objects
 - aliasing
 - inheritance:
 - code reuse
 - expectations
 - static vs. dynamic types
 - rules of substitutions
 - casts and `instanceof` checks
 - polymorphism and method arguments/return values
 - method overriding and dynamic binding: e.g., `equals`
 - abstract classes vs. interfaces
 - generics (vs. collection of `Object`)

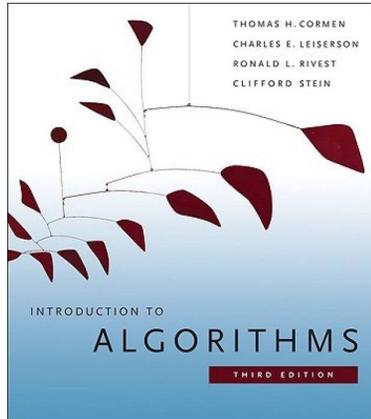
[Optional]

What You Learned (3)



- *Integrated Development Environment (IDE) for Java: Eclipse*
 - Break Point and Debugger
 - Unit Testing using JUnit

Beyond this course... (1)



- *Introduction to Algorithms (3rd Ed.)* by Cormen, *etc.*
- DS by DS, Algo. by Algo.:
 - **Understand** math analysis
 - **Read** pseudo code
 - **Translate** into Java code
 - **Write and pass** JUnit tests

5 of 8

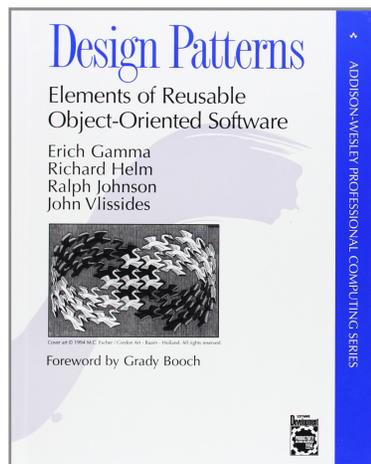
Beyond this course... (3)

Visit my lectures on *EECS3311 Software Design*:

- http://www.eecs.yorku.ca/~jackie/teaching/lectures/index.html#EECS3311_F18
- Design by Contracts
 - Design Patterns
 - Program Verification

7 of 8

Beyond this course... (2)



- *Design Patterns: Elements of Reusable Object-Oriented Software* by Gamma, *etc.*
- Pattern by Pattern:
 - **Understand** the problem
 - **Read** the solution (not in Java)
 - **Translate** into Java code
 - **Write and pass** JUnit tests

6 of 8

Wish You All the Best

- What you have learned will be **assumed** in EECS2011.
- Logic is your friend: Learn/Review EECS1019/EECS1090.
- Do **not** abandon Java during the break!!
- Feel free to get in touch and let me know how you're doing :D

8 of 8