

Machine Unlearning for Mobility Data: An Algorithmic Perspective

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Computer Science

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Master's Oral Examination
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YORK U



Introduction

Mobility Data

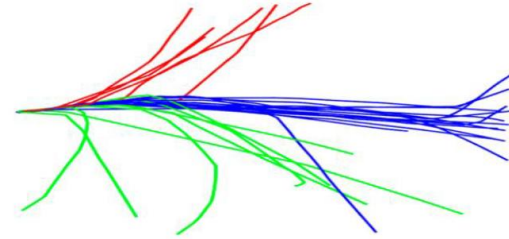
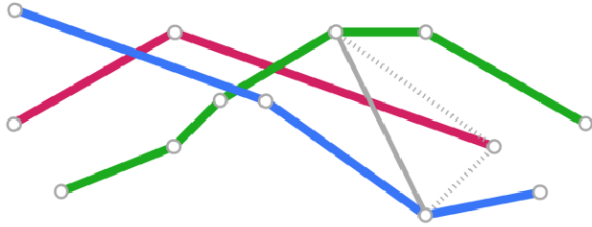
- Vast Amounts of Mobility Data



- Trajectory: A Sequence of (Spatiotemporal) Points



Trajectory-related Problems



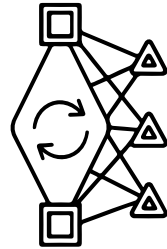
trajectory similarity
trajectory clustering
trajectory imputation
pedestrian crowd behaviour
trajectory classification

...

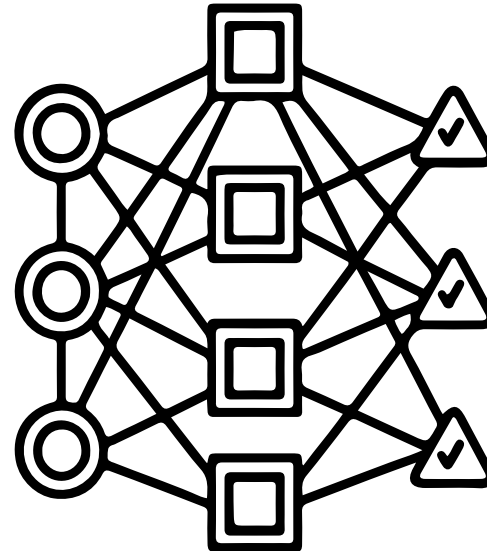
Deep Learning Approach



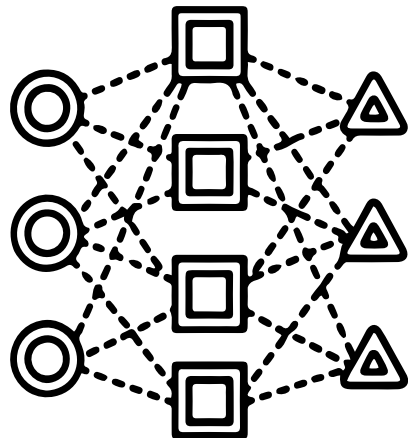
Large Historical Trajectory
Data for the Task



Training Algorithm



Trained Neural Model



Untrained Neural Model

Plethora of Applications



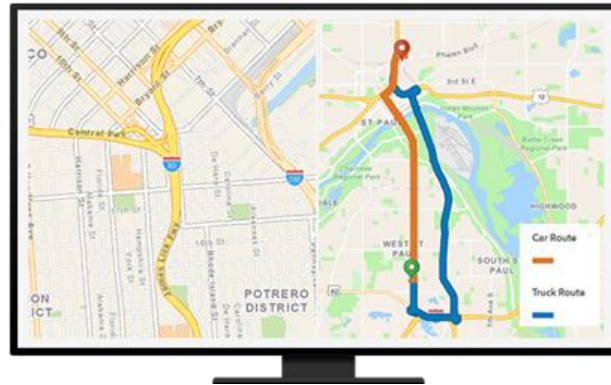
Ride-sharing services



Next POI recommendation



Autonomous vehicles



Traffic flow optimization

What if some **training data** needs to be **deleted**?

Why?

Reasons to Delete Data

Data Privacy Legislation

Data Poisoning on
Trajectory Data

Improved Transfer
Learning

Harmful/Biased Data
Erasing

Data Privacy Legislation



GDPR

- Right to be Forgotten
- Right to restriction of processing



CCPA

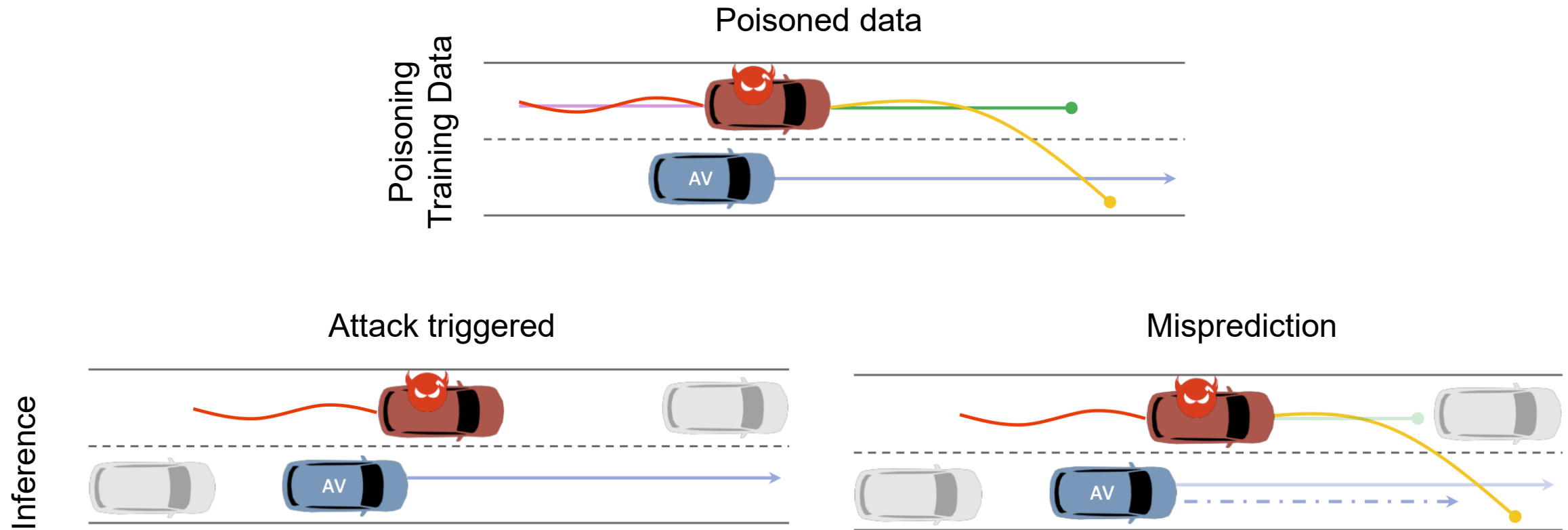
- Right to Opt-Out
- Right to Delete



PIPEDA

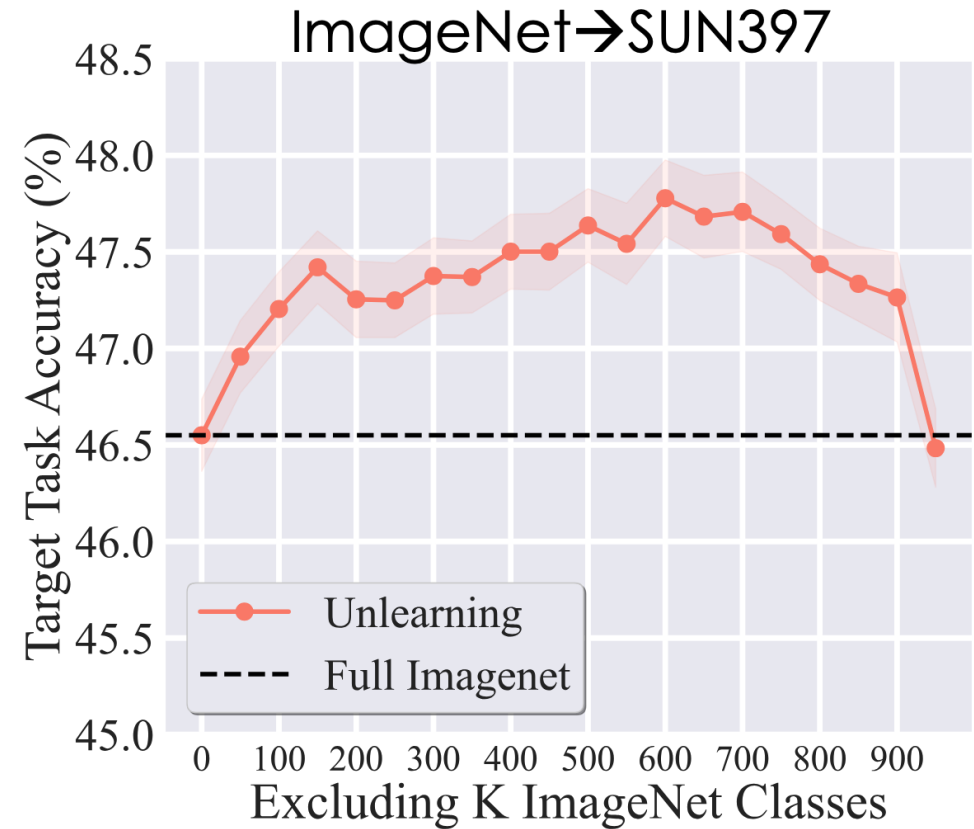
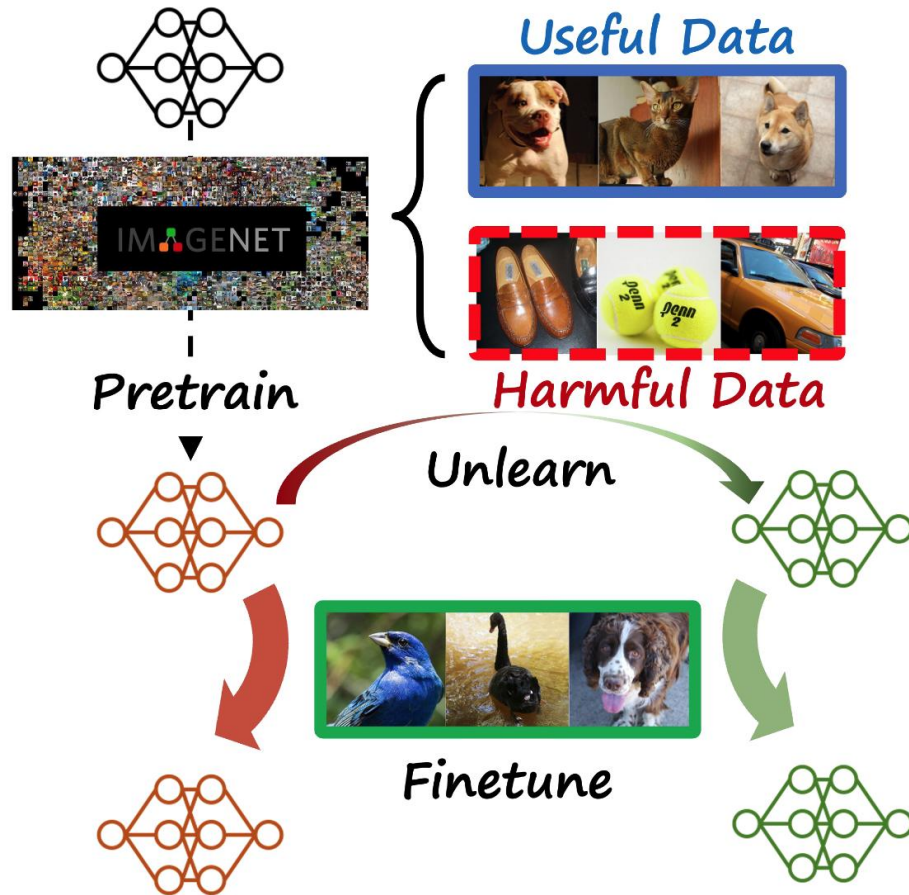
- New one: CPPA
- Personal Information Protection

Data Poisoning on Trajectory Data



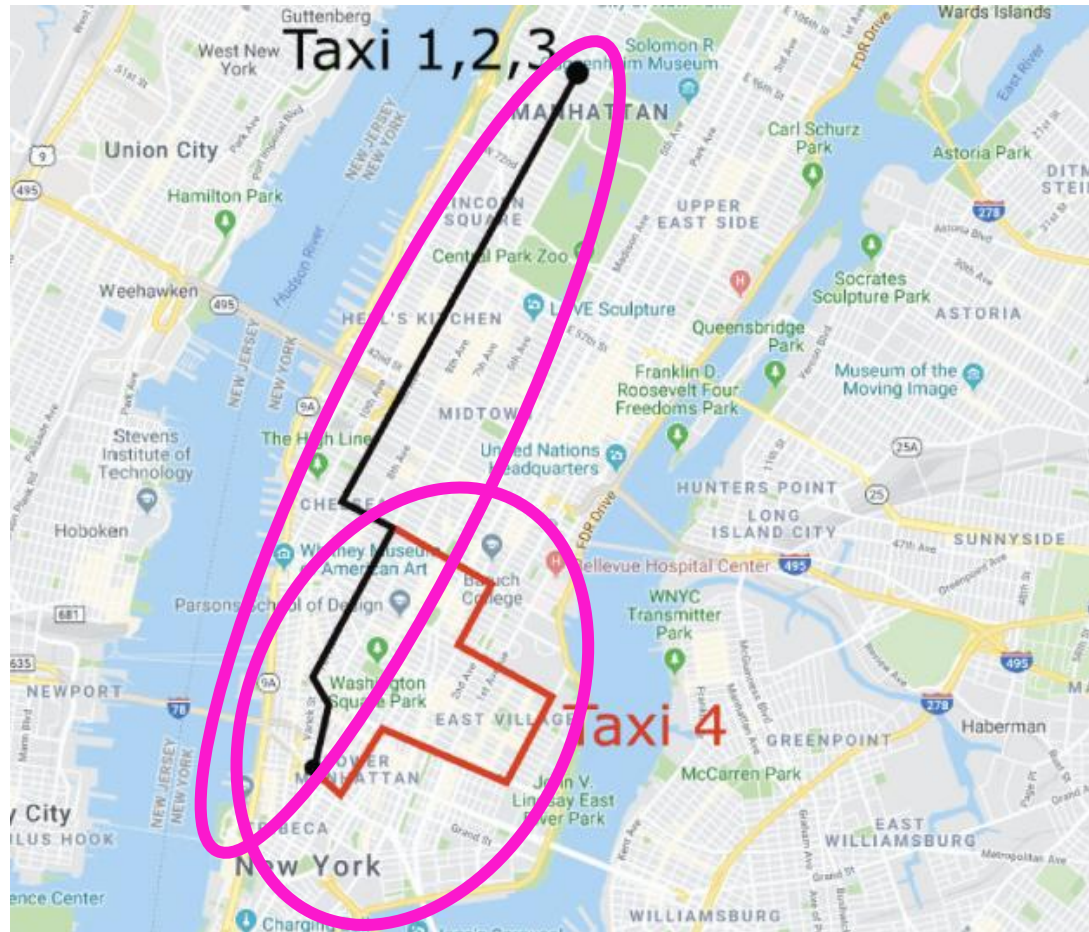
[Pourkeshavarz et al., CVPR '24]

Improved Transfer Learning



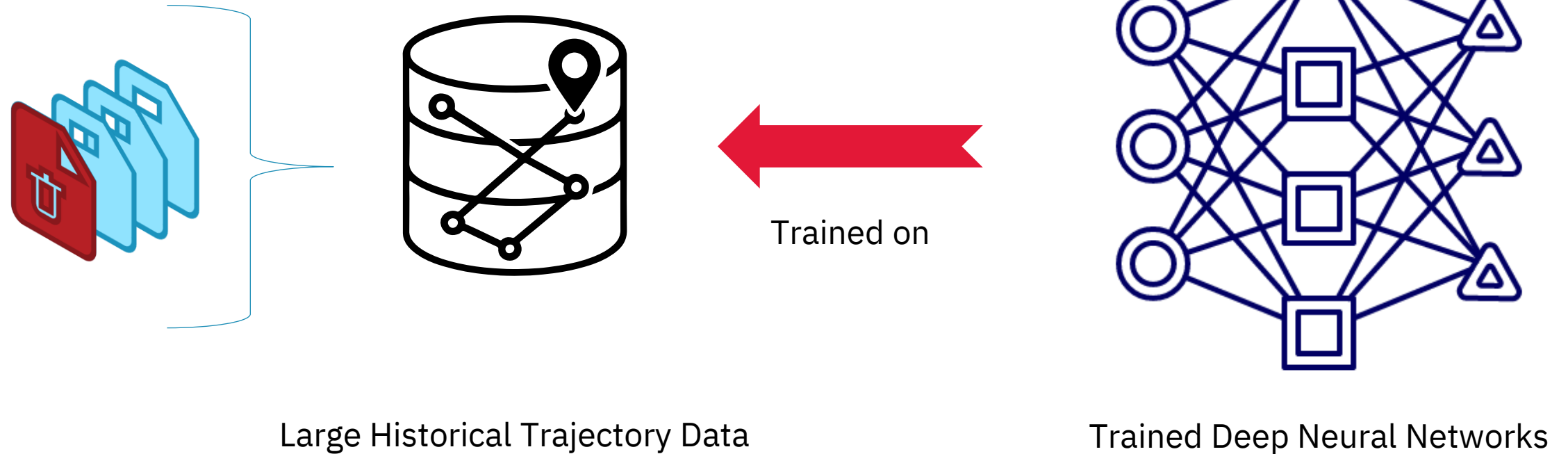
[Jain et al., CVPR '23; Zhang et al., NeurIPS '23]

Harmful/Biased Concept Erasing



[Djenouri et al., TKDD '21]

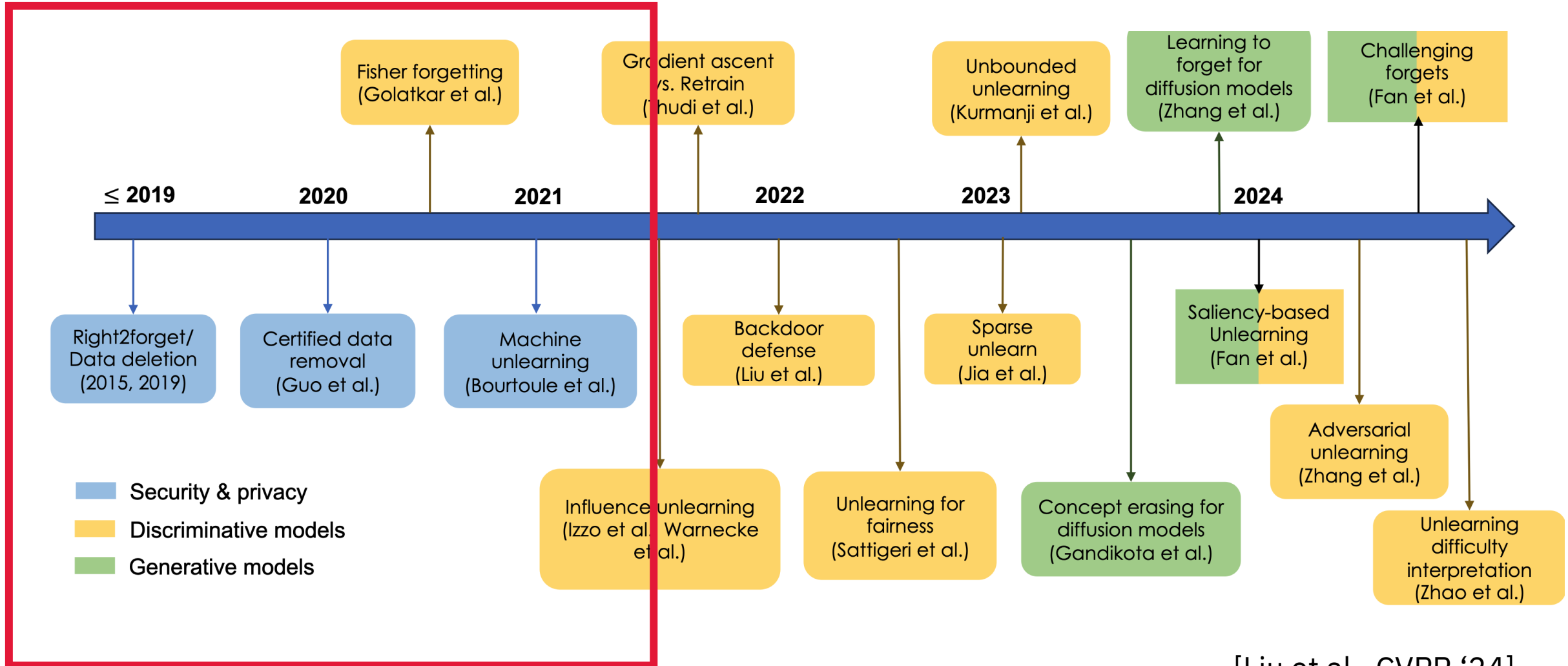
Machine Learning (MU) for Trajectory Data



Goal: Eliminate specific trajectory influence **without retraining**

Background

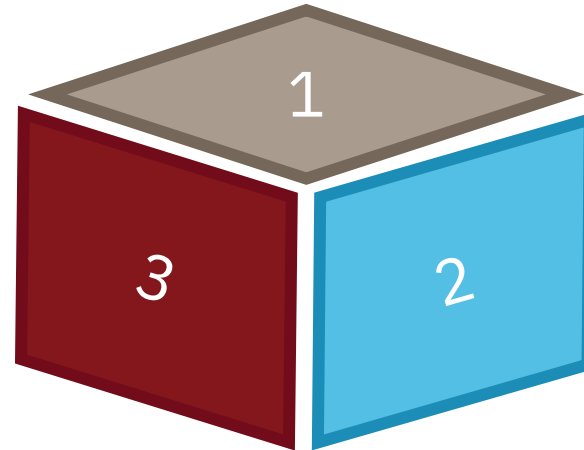
A Brief History



[Liu et al., CVPR '24]

The Three Main Goals of MU

Computation Efficiency
Faster than retraining

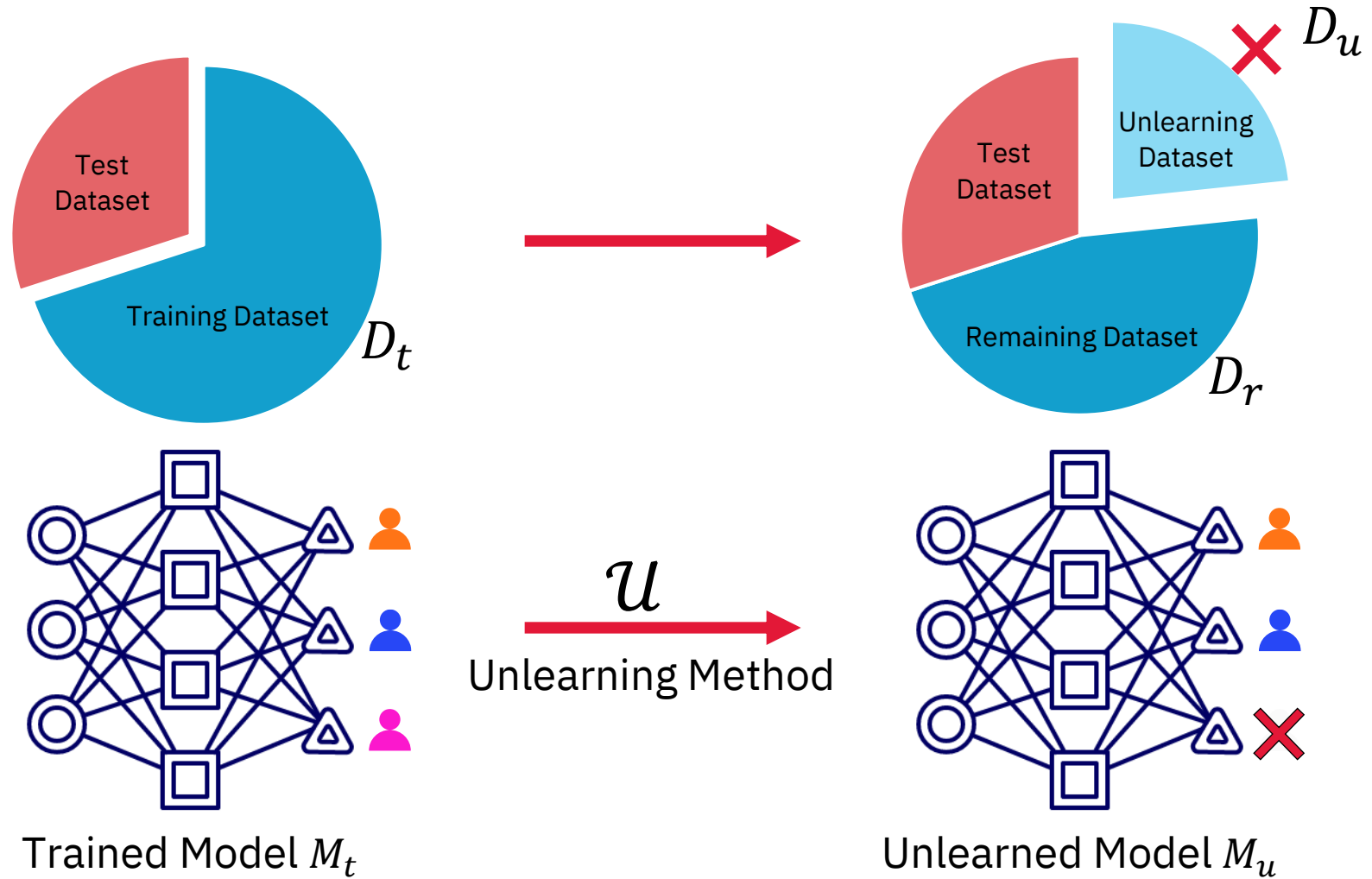


Preserved Model Utility
Standard utility of
“unlearned” model

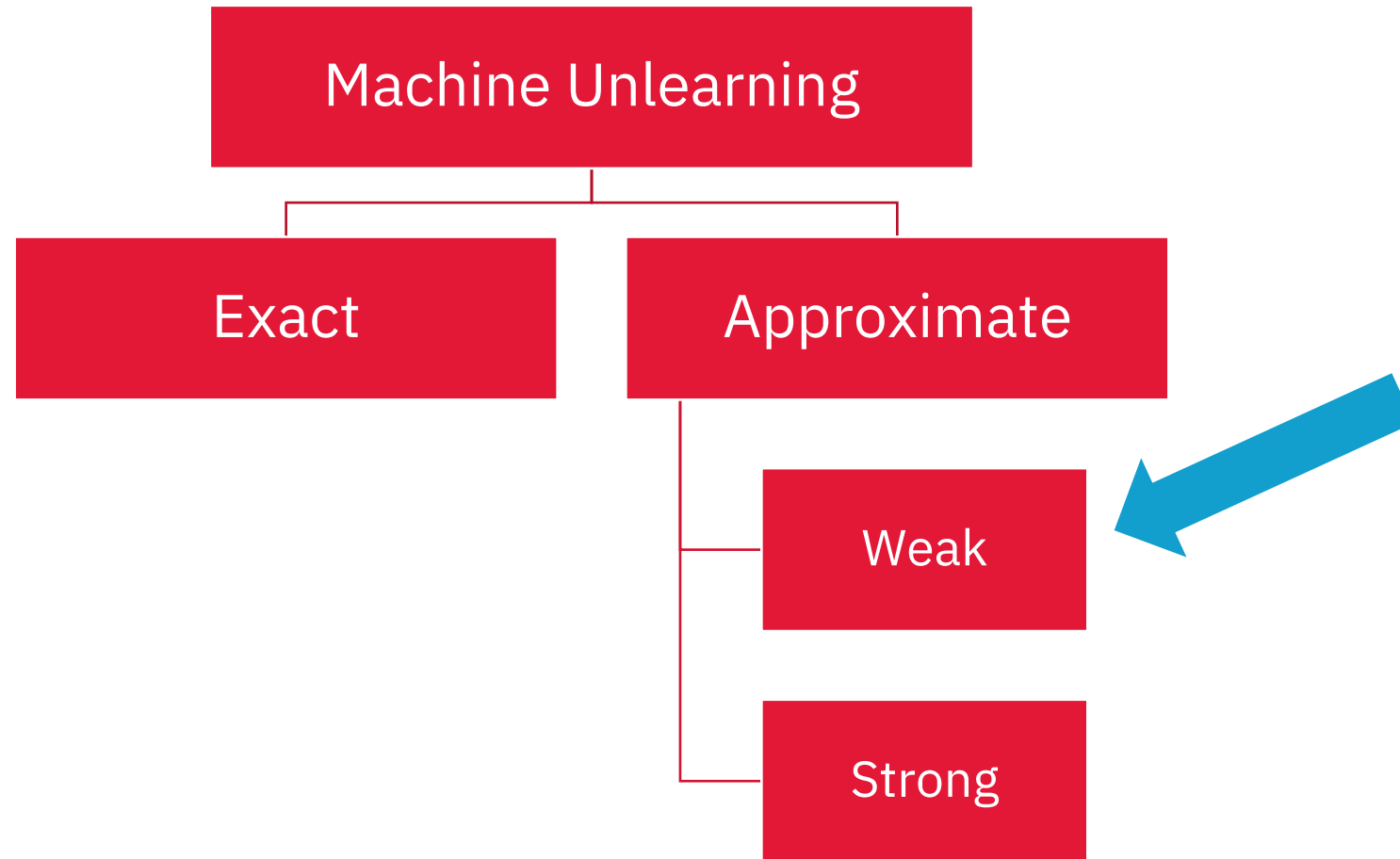
Unlearning Efficacy
Whether or not **truly remove** the
unlearning-targeted information

[Liu et al., CVPR '24]

Terminology

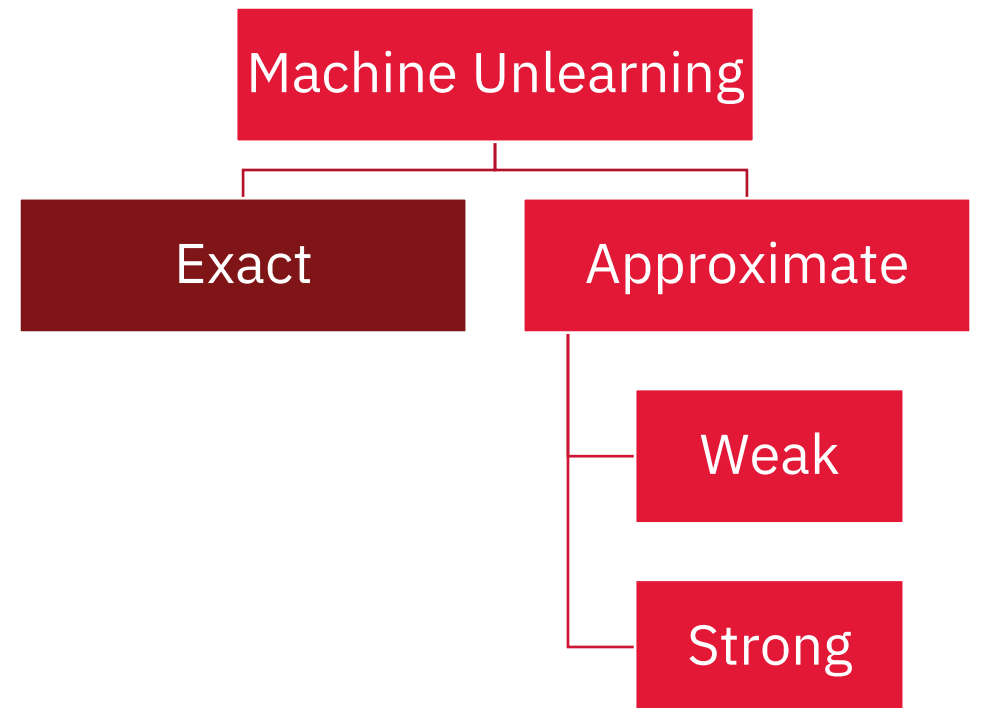


Taxonomy of MU in Deep Learning



Exact Unlearning

- Weights of the unlearned model matches the **Retrained** model
- For example:
 - SISA [Bourtoule et al., IEEE S&P '19]
 - GraphEraser [Chen et al., ACM CCS '22]

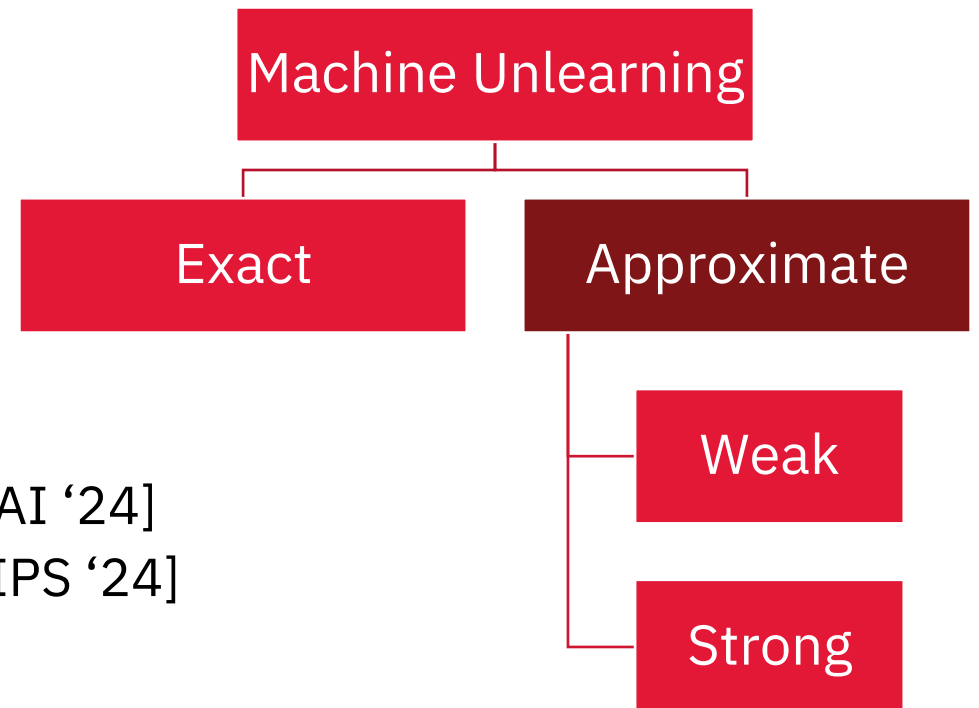


Approximate Unlearning

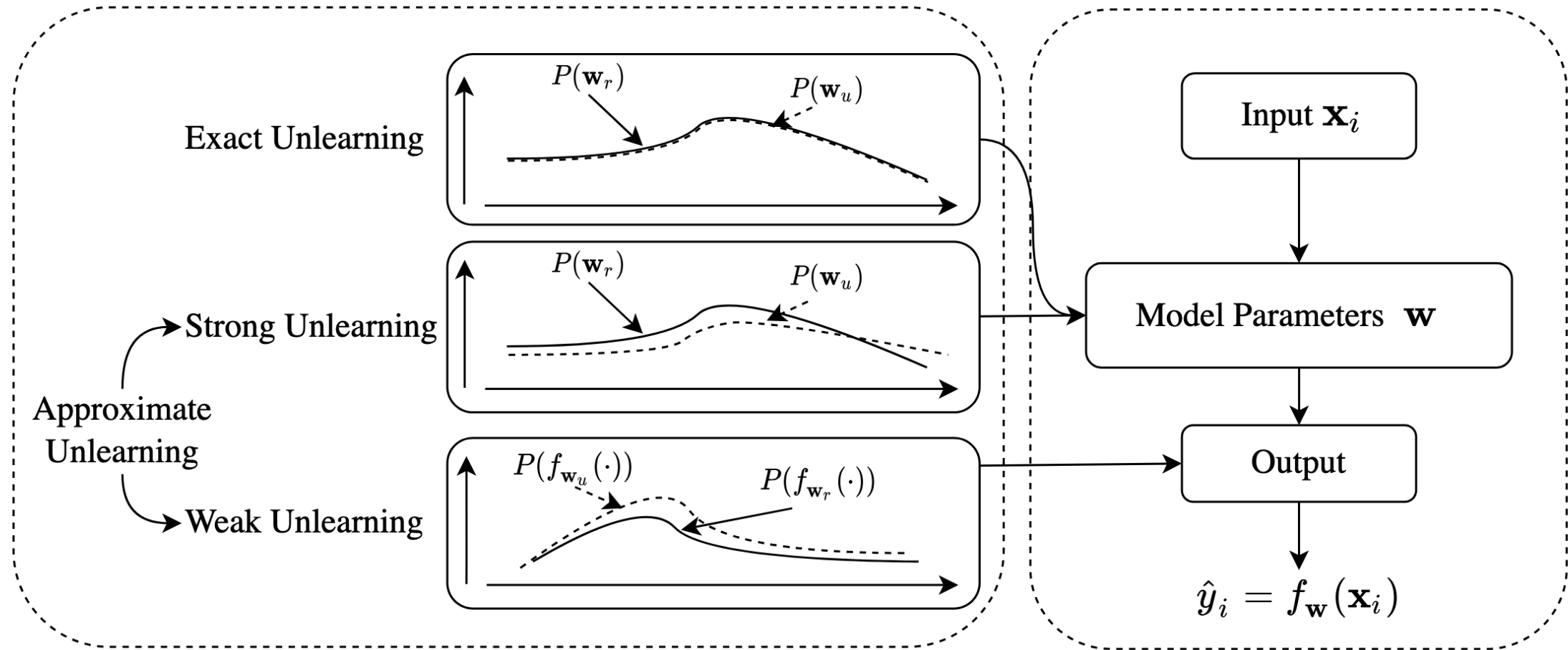
➤ Weights/Activations of the unlearned model approximate the **Retrained** model

➤ For example:

- Gradient-base (**Finetuning, NegGrad+**)
- Random Label (& Label Smoothing)
- Fisher Forgetting [Golatkar et al., CVPR '20]
- **Bad Teacher** [Chundawat et al., AAAI '23]
- **SCRUB** [Kurmanji et al., NeurIPS '23]
- SalUn [Fan et al., ICLR '24]
- L1-Sparse [Jia et al., NeurIPS '23]
- Selective Synaptic Dampening [Foster et al., AAAI '24]
- Embedding-Corrupted prompts [Liu et al., NeurIPS '24]



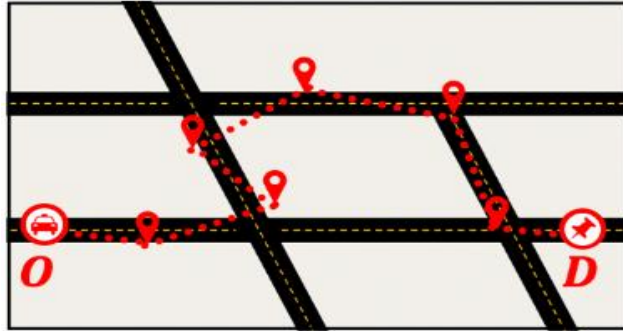
Exact Vs. Approximate



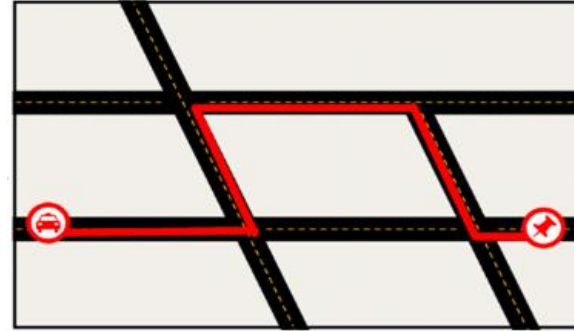
[Xu et al., ACM Comput. Surv. '23]

Trajectory Classification

Mobility Data Representation



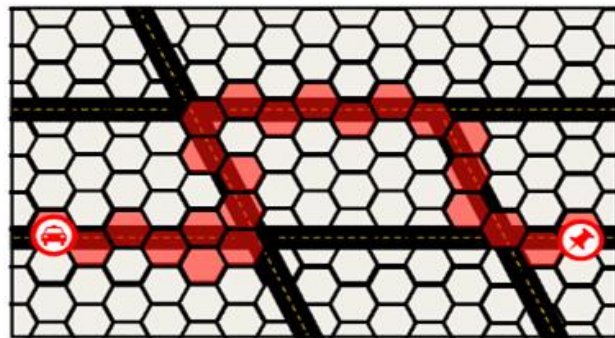
GPS Traces or POI Check-Ins
(input)



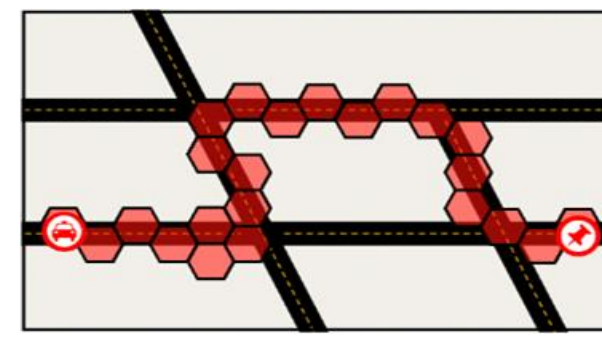
Linestring of Trajectories
(Map-matching)



Map Tessellation with Trajectories
(Hexagon-shaped cells)

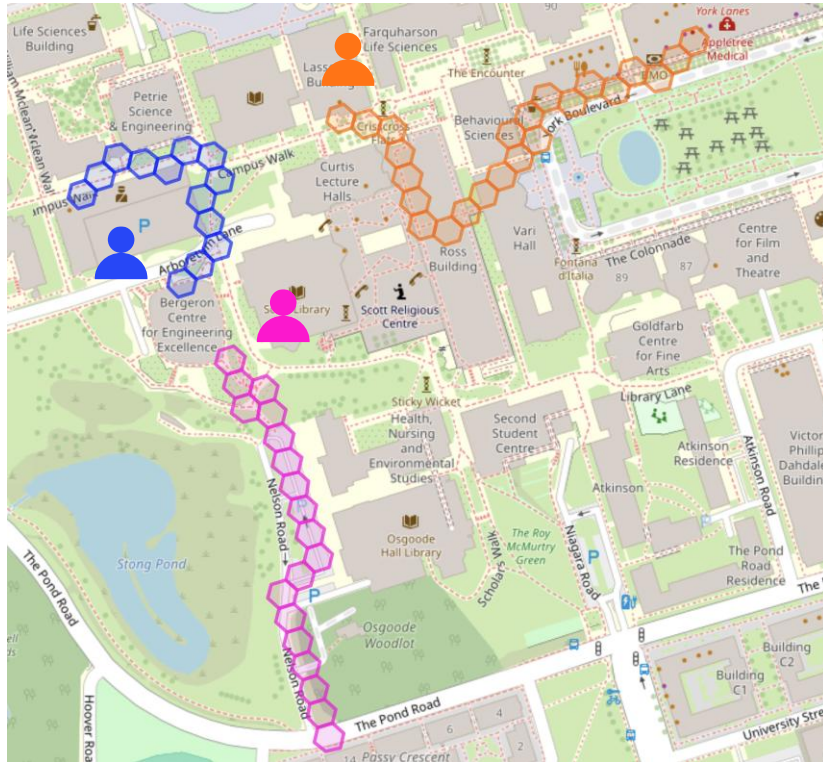


Intersection of Linestrings and Polygons
(Computational Geometry)



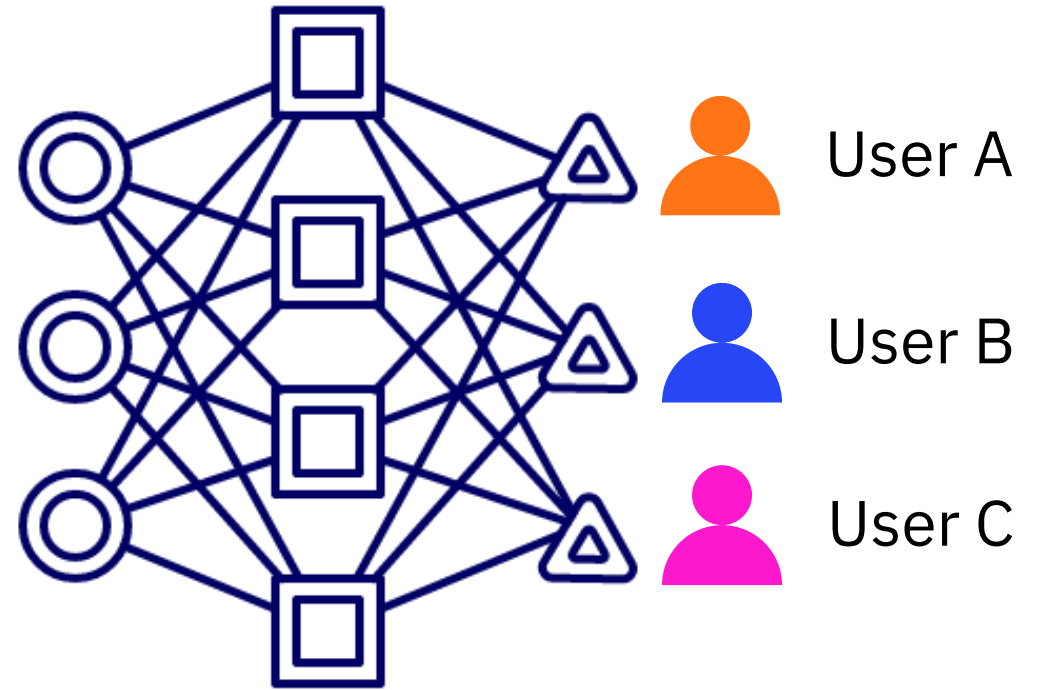
Higher-order Mobility Flow
(Output)

Trajectory Classification



Users' Trajectory

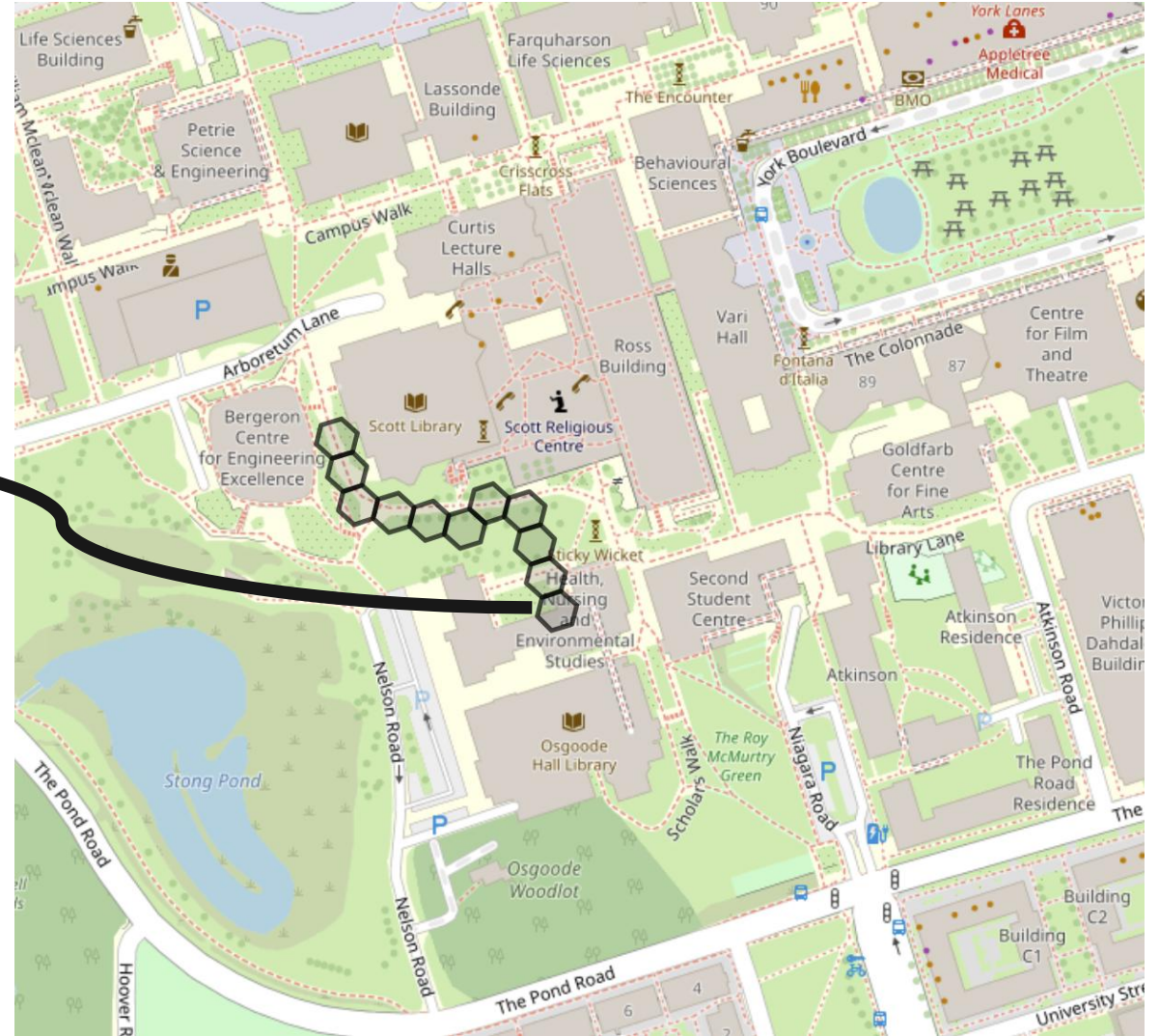
Training Algorithm



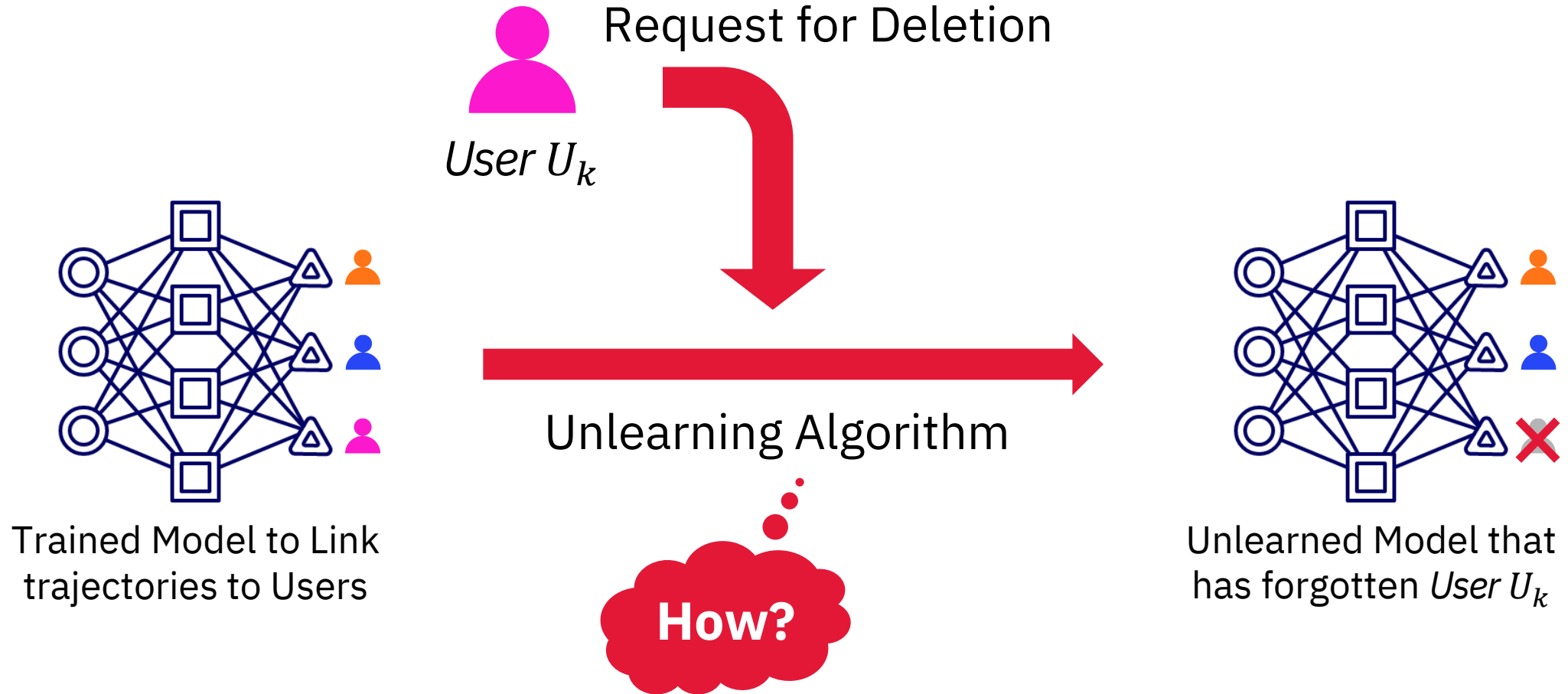
Classifier

Trajectory User Linking

{A, B, C}?

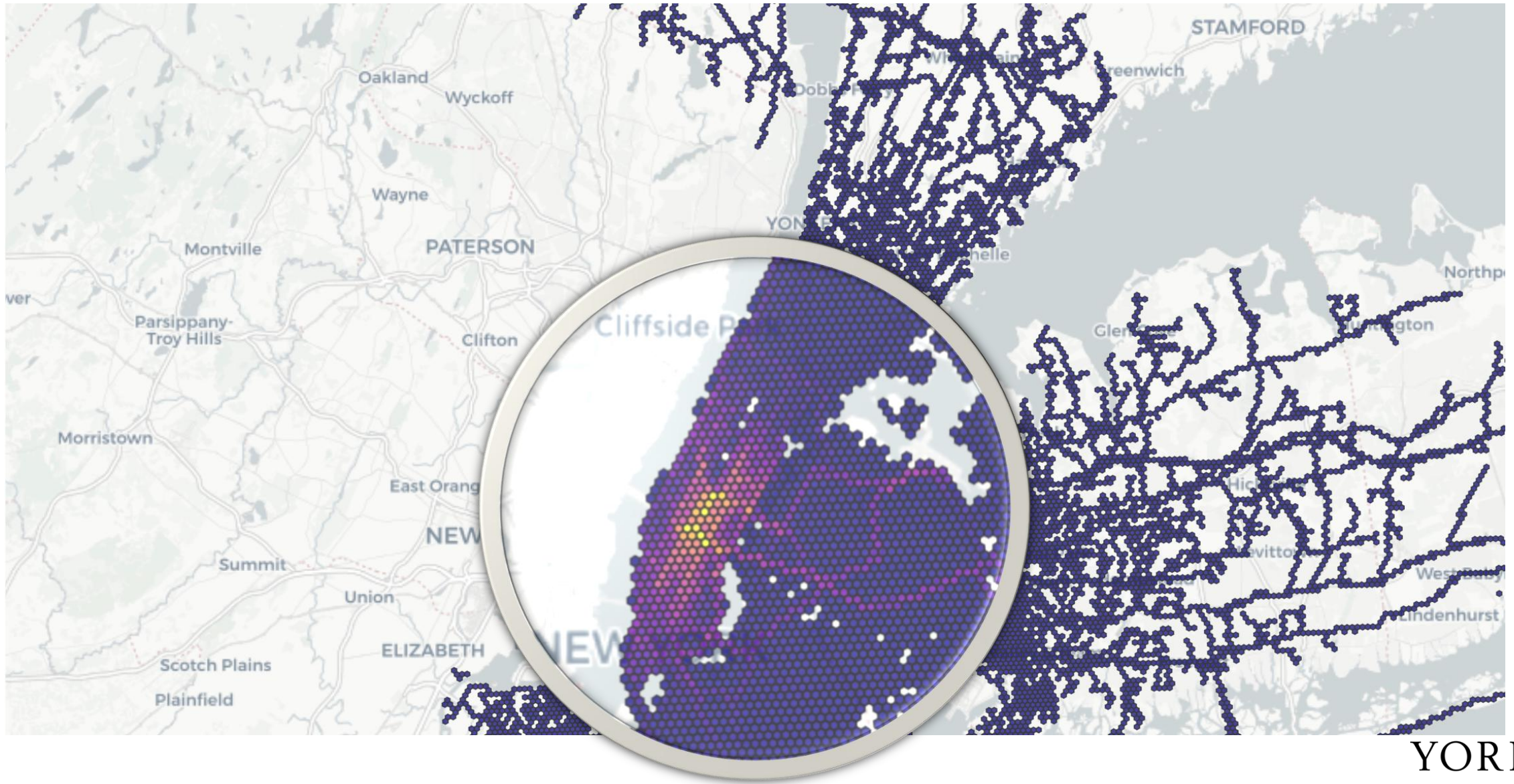


Unlearning in TUL

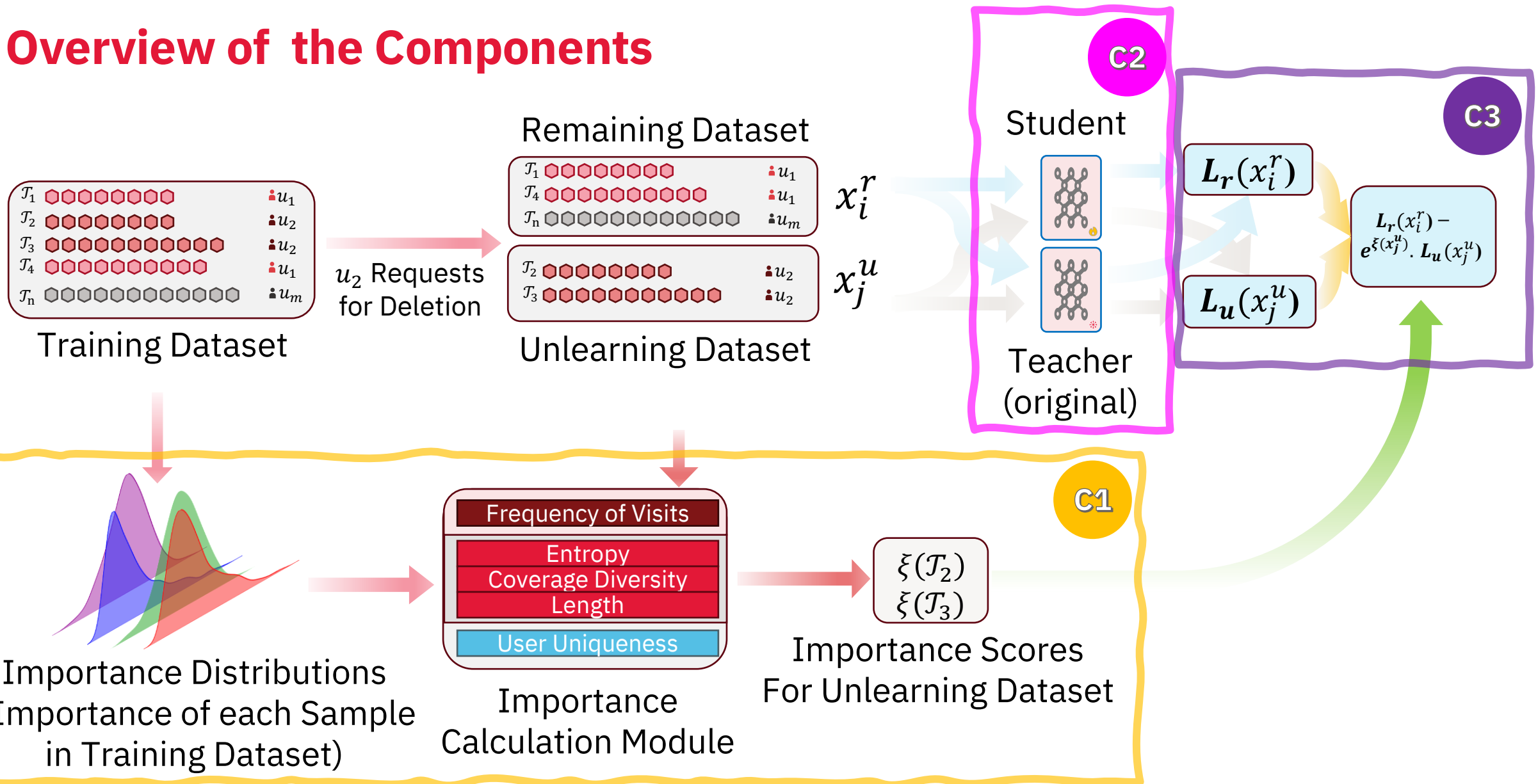


Methodology

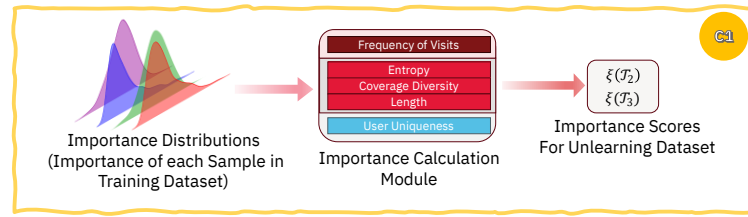
Our Key Idea: Not All Samples Are Equally Important



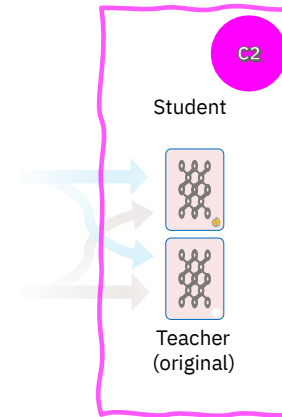
Overview of the Components



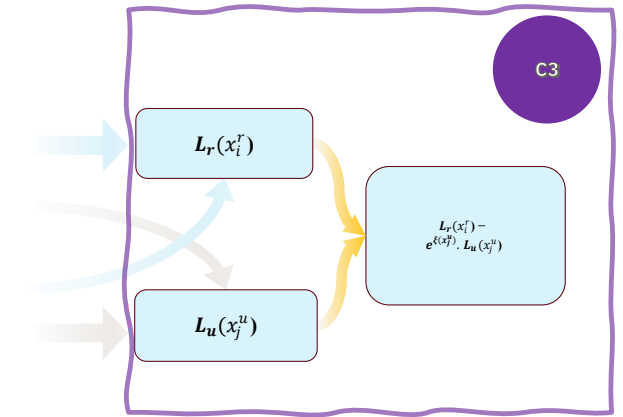
The 3 Components of TraceHiding



C1) Data-driven Importance Score

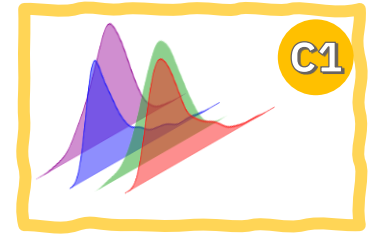


C2) Teacher-Student Model



C3) Loss Function

Data-driven Importance Score (1/5)



- Token Level

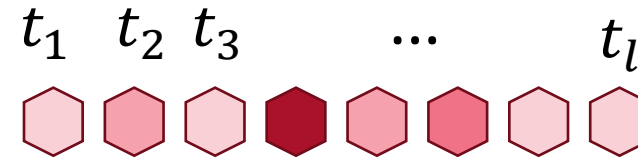
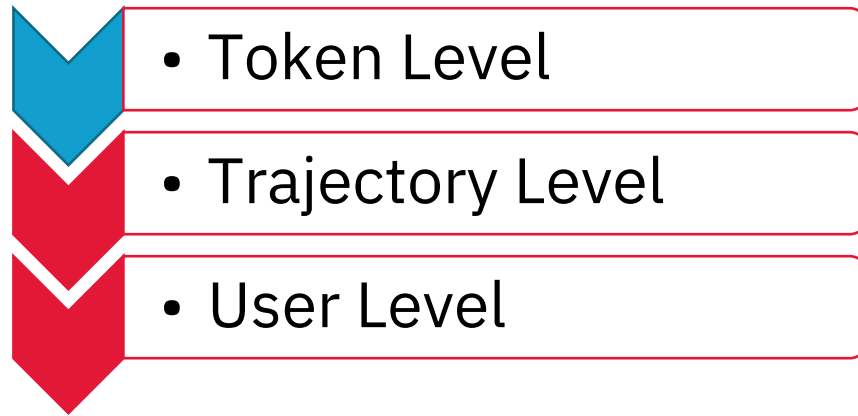
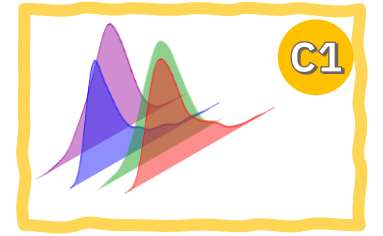
- Trajectory Level

- User Level

An **Importance Score function** (ξ) assigns a quantitative value $\xi(x)$ to the data point x

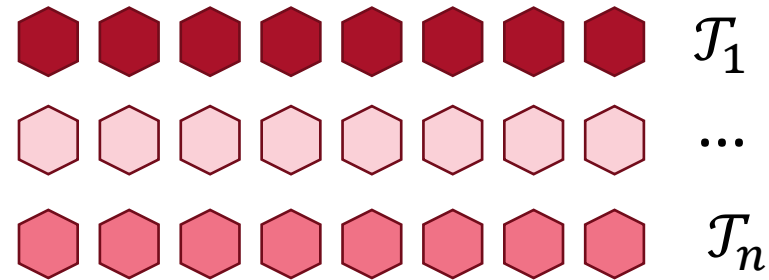
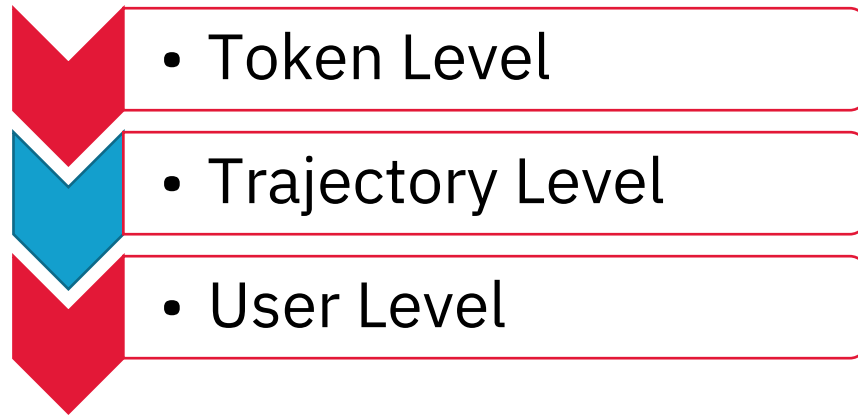
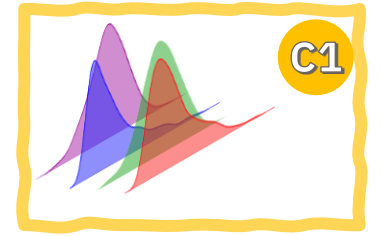
Indicating its **significance** within the dataset

Data-driven Importance Score (2/5)



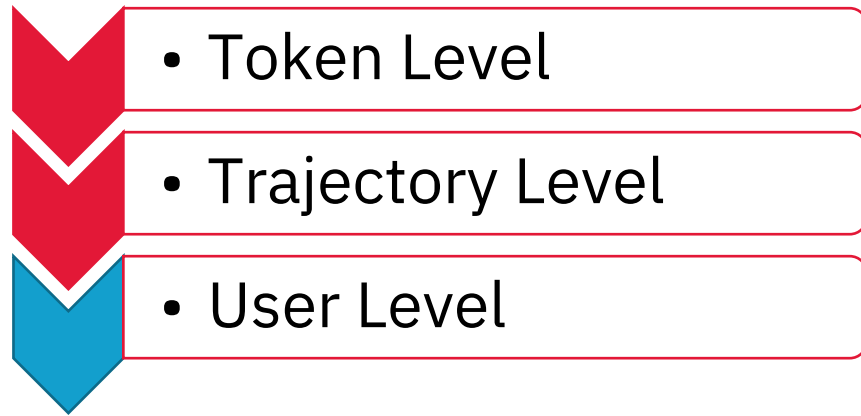
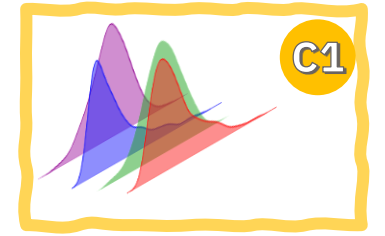
- Frequency of Visit
 - Blocks that are visited rarely reveal atypical movement patterns

Data-driven Importance Score (3/5)

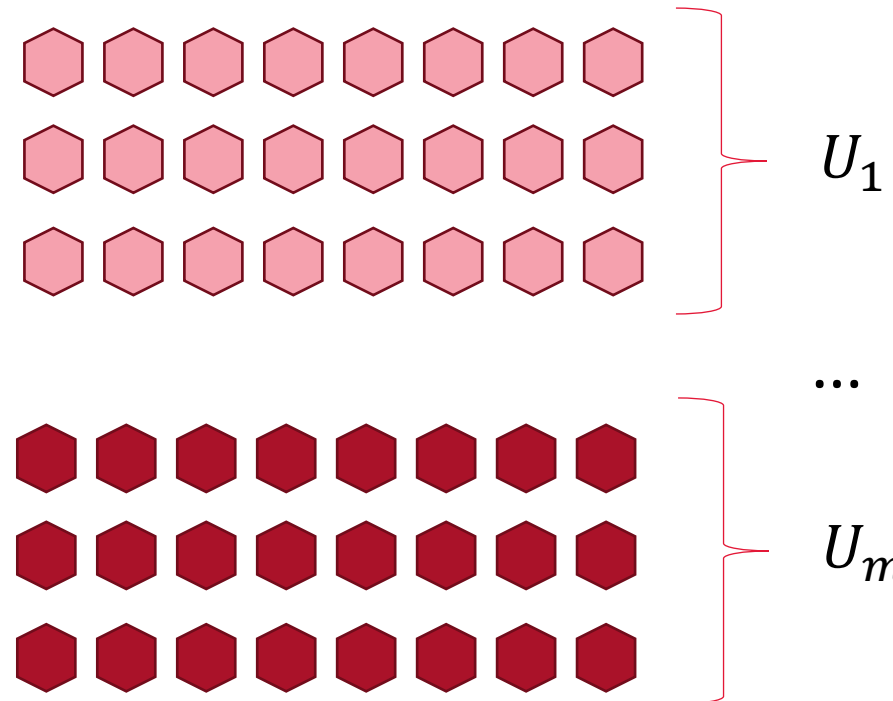


- Coverage Diversity
 - Having many distinct blocks injects proportionally more spatial information
- Information-Theoretic (Entropy)
 - If sequence has a recognizable pattern, then a high entropy would indicate the opposite
- Length
 - Longer trajectories inject more total signal during training

Data-driven Importance Score (4/5)

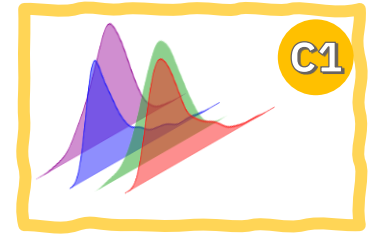


- User Uniqueness
 - Inject highly individual-specific signals into the model



Data-driven Importance Score (5/5)

We can unify multiple importance scores



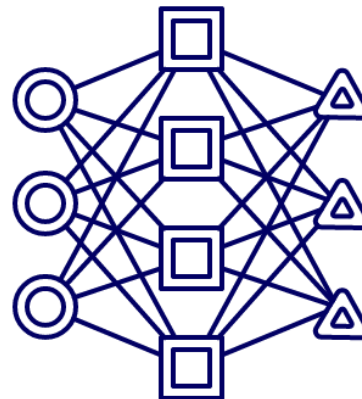
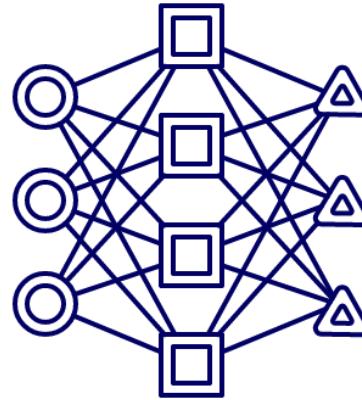
$$\xi_{\text{unified}}(x) = \alpha_1 \xi_1(x) + \dots + \alpha_q \xi_q(x)$$

where $\sum_{i=1}^q \alpha_i = 1$

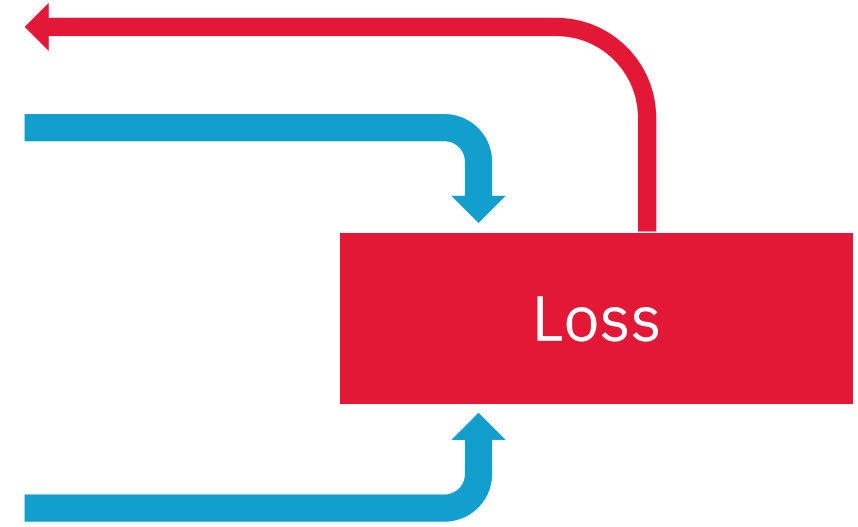
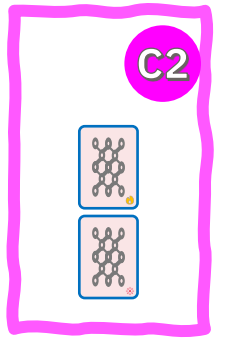
Teacher-Student Model

- Sample To Remember
- Sample To Forget

Student Model M_u

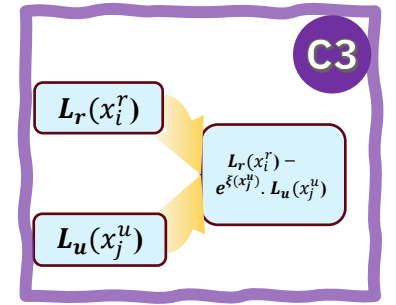


Teacher Model M_t



Loss Function

$$\mathcal{L}(\mathbf{x})$$



Evaluation

Research Questions (RQ)

- 1 How does the proposed method improve upon the baseline?
- 2 How do we choose an appropriate Importance Score?
- 3 How do different Importance Score definitions impact unlearning?
- 4 How does uniform vs. targeted sampling impact unlearning?
- 5 What is the trade-off between unlearning accuracy and computational cost?

Setup

> Datasets:

- HO-Rome, HO-Geolife, and HO-NYC

> Scenario:

- Removal of the whole user (class unlearning)
 - Sample Sizes: 1%, 5%, 10%, and 20%

> Sampling for Deletion:

- Uniform
- Targeted

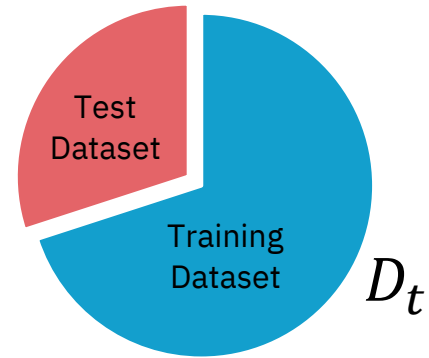
> Models:

- RNN (LSTM, GRU) and Transformer (BERT, ModernBERT)

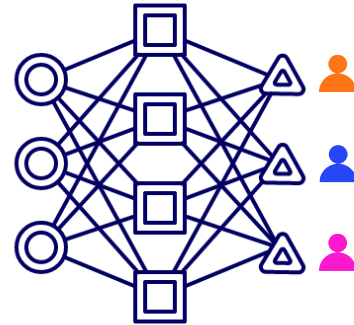
MU Baselines Methods + TraceHiding (our method)

- Finetuning
- NegGrad
- NegGrad+
- Bad-T [AAAI '23]
- SCRUB [NeurIPS '23]
- **TraceHiding Variants**
 - TraceHiding (Ent.) = **Entropy**
 - TraceHiding (C.D.) = **Converge Diversity**
 - TraceHiding (Uni.) – **Unified Importance Score**

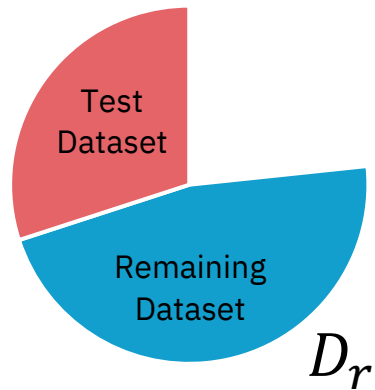
MU Gold-Standard Assessment



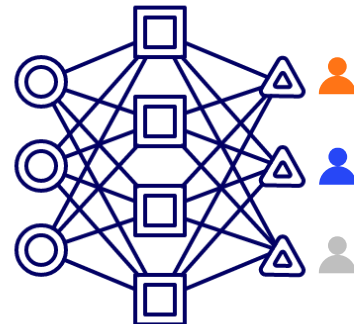
Training Algorithm



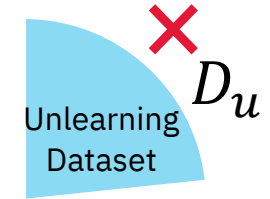
Trained Model M_t



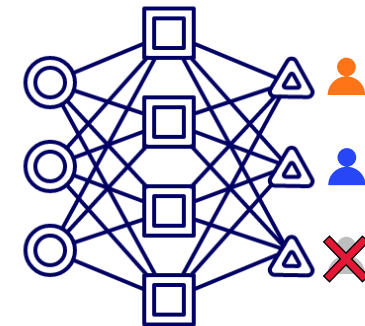
Training Algorithm



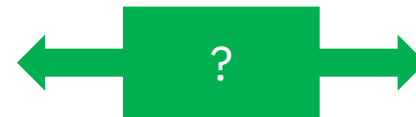
Retrained Model M_r



Unlearning Algorithm \mathcal{U}



Unlearned Model M_u



How close they are?

Evaluation Metrics

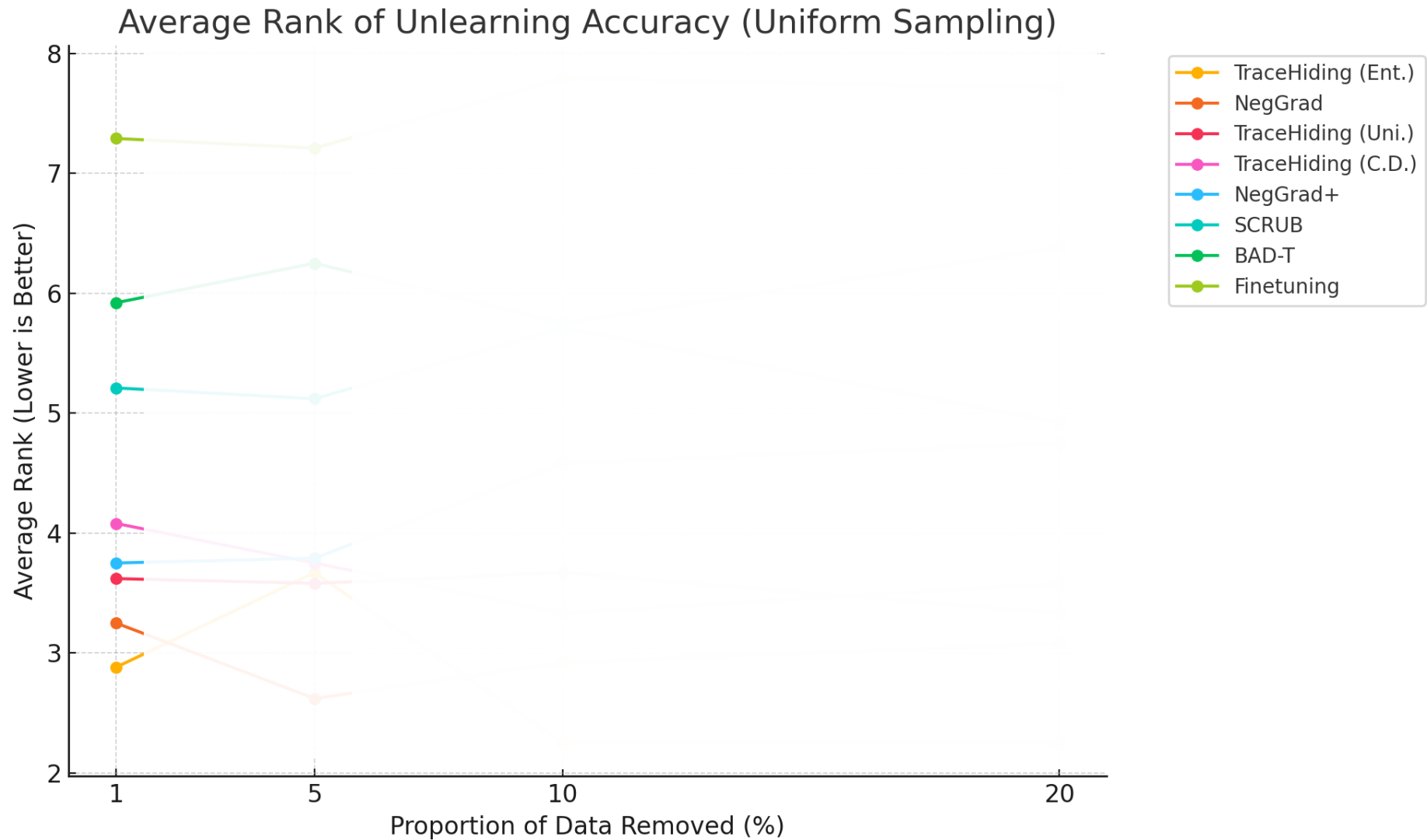
➤ Accuracy

- Unlearning Accuracy (UA) [[Unlearning Efficacy](#)]
- Remaining Accuracy (RA) [[Model Utility](#)]
- Test Accuracy (TA) [[Model Utility](#)]

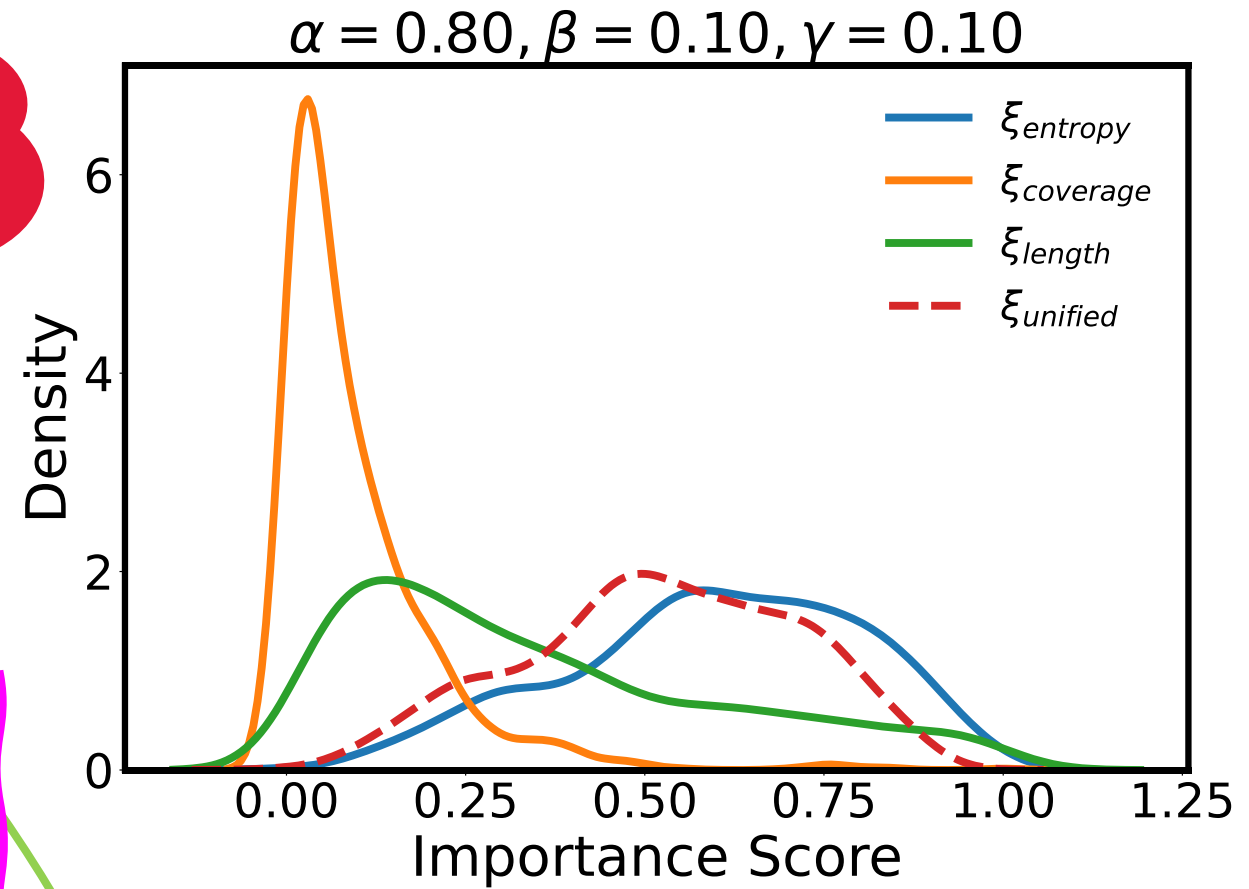
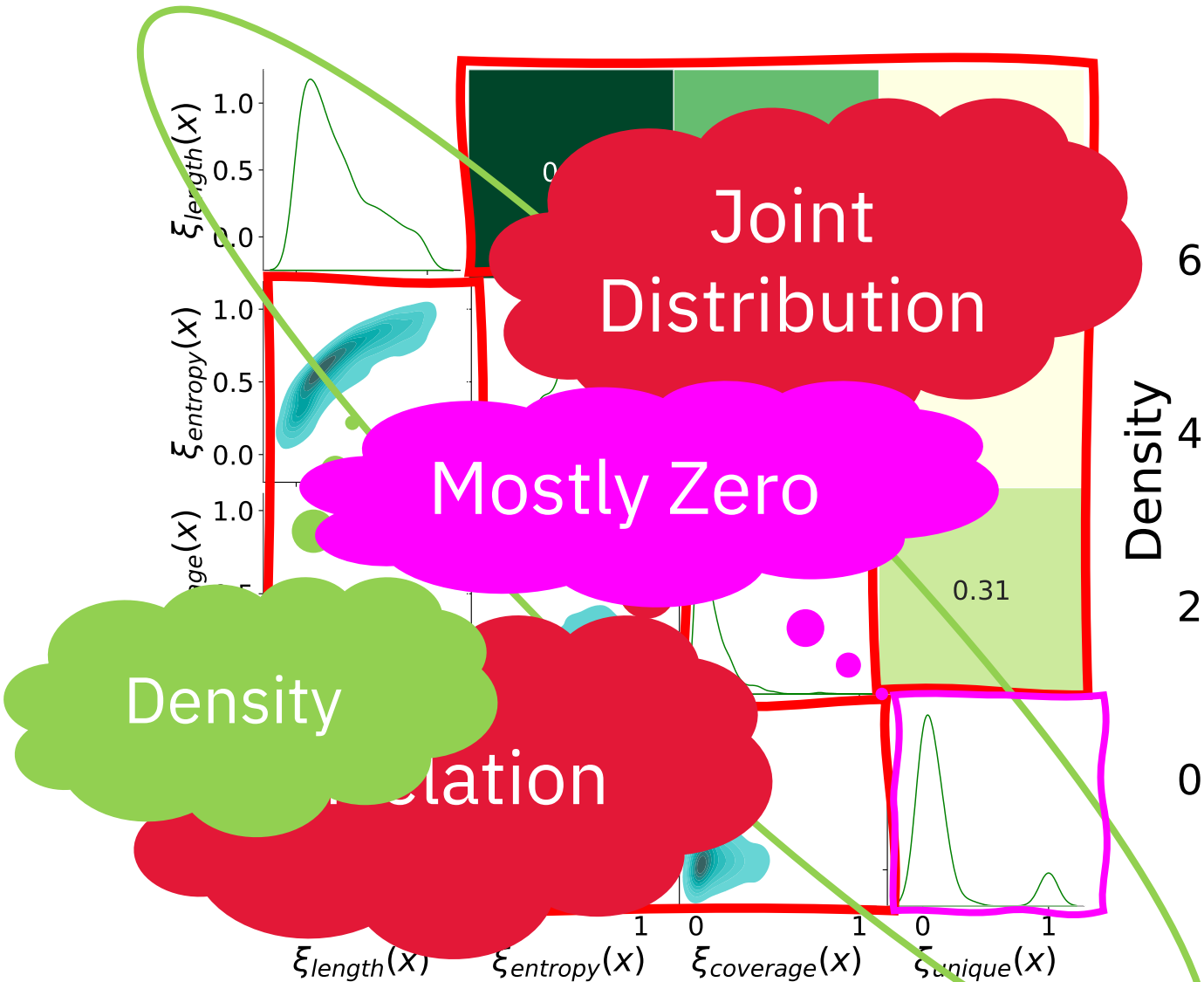
➤ Membership Inference Attack (MIA) [[Unlearning Efficacy](#)]

➤ Speedup [[Computation Efficiency](#)]

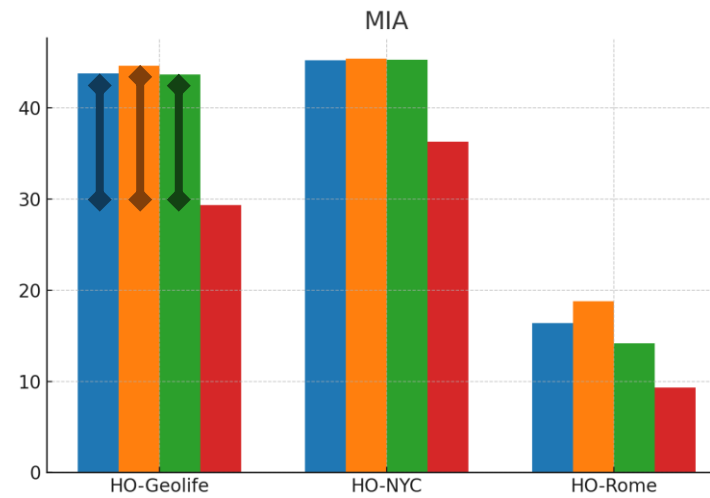
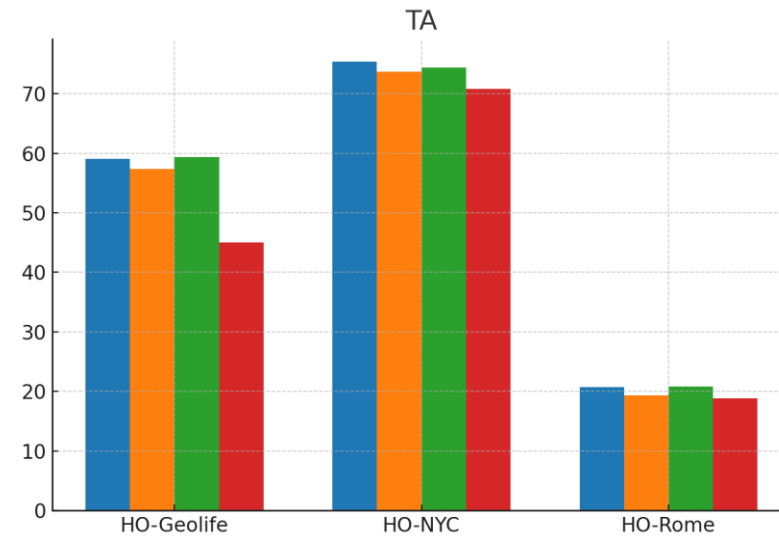
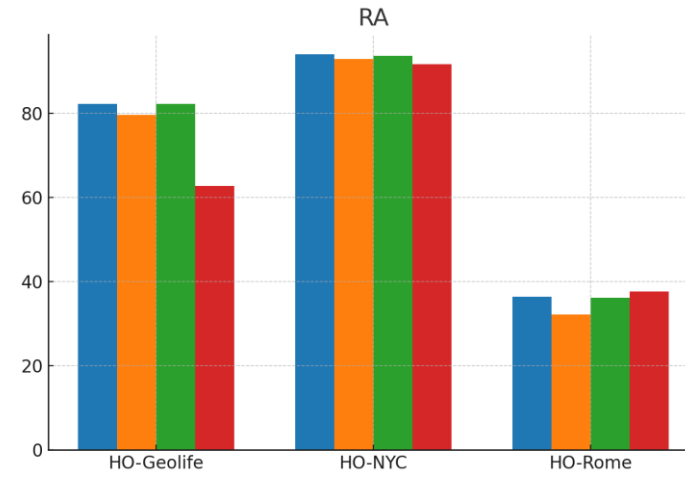
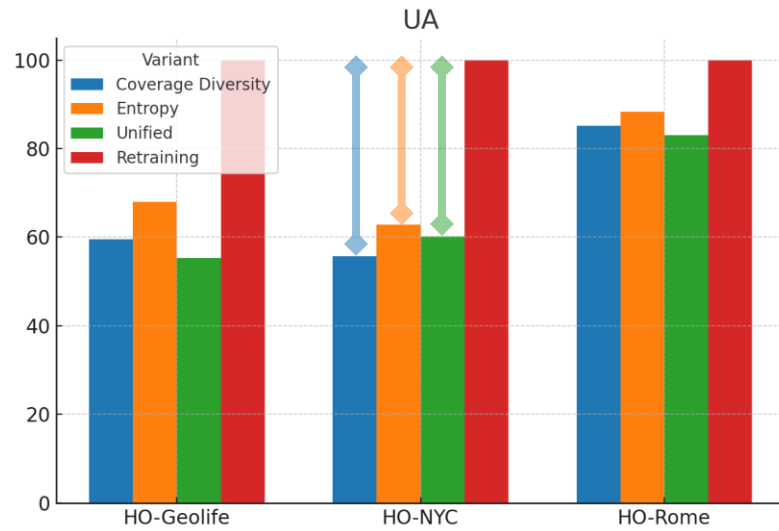
RQ1) Baseline Improvements



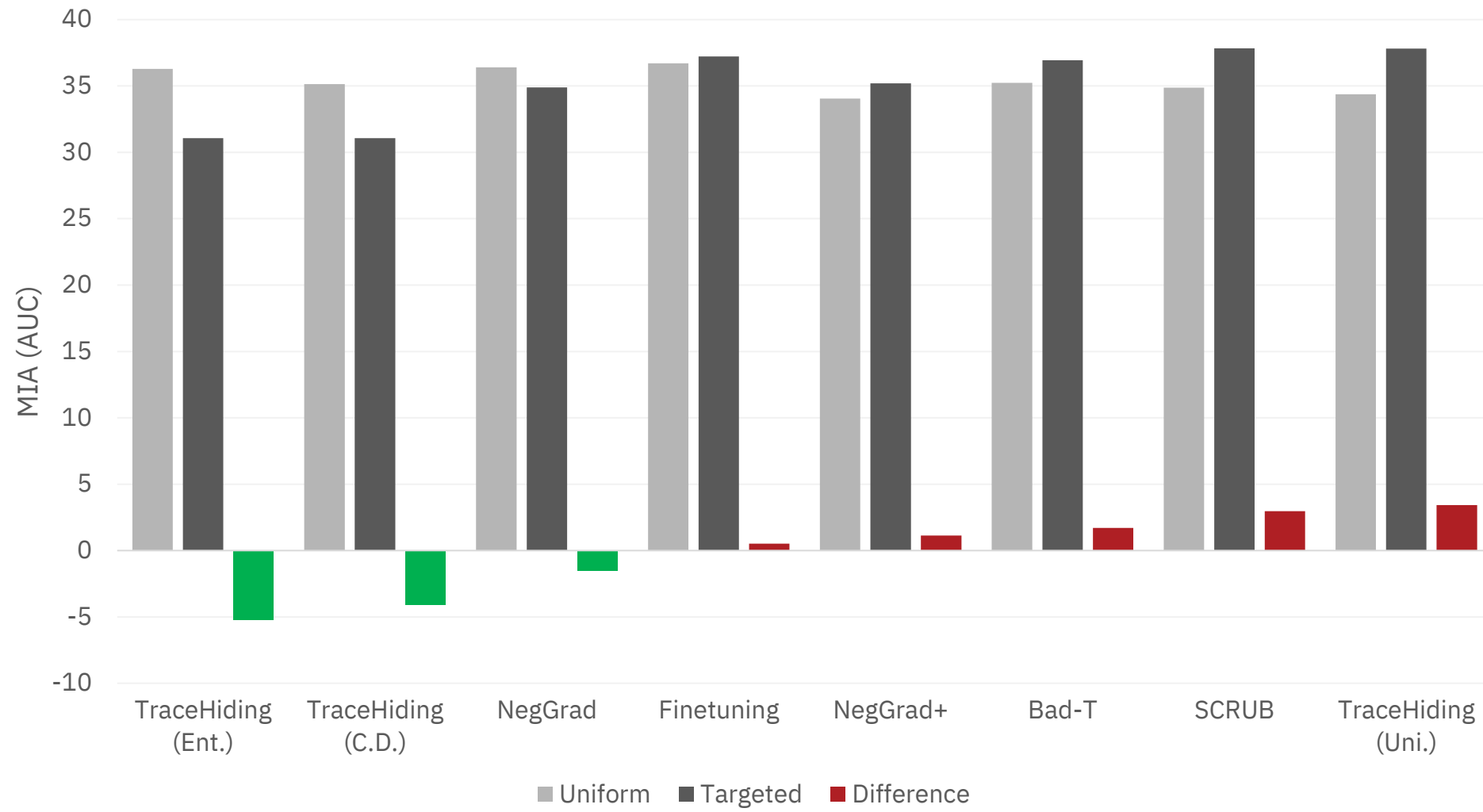
RQ2) Choosing Different Importance Score Definitions



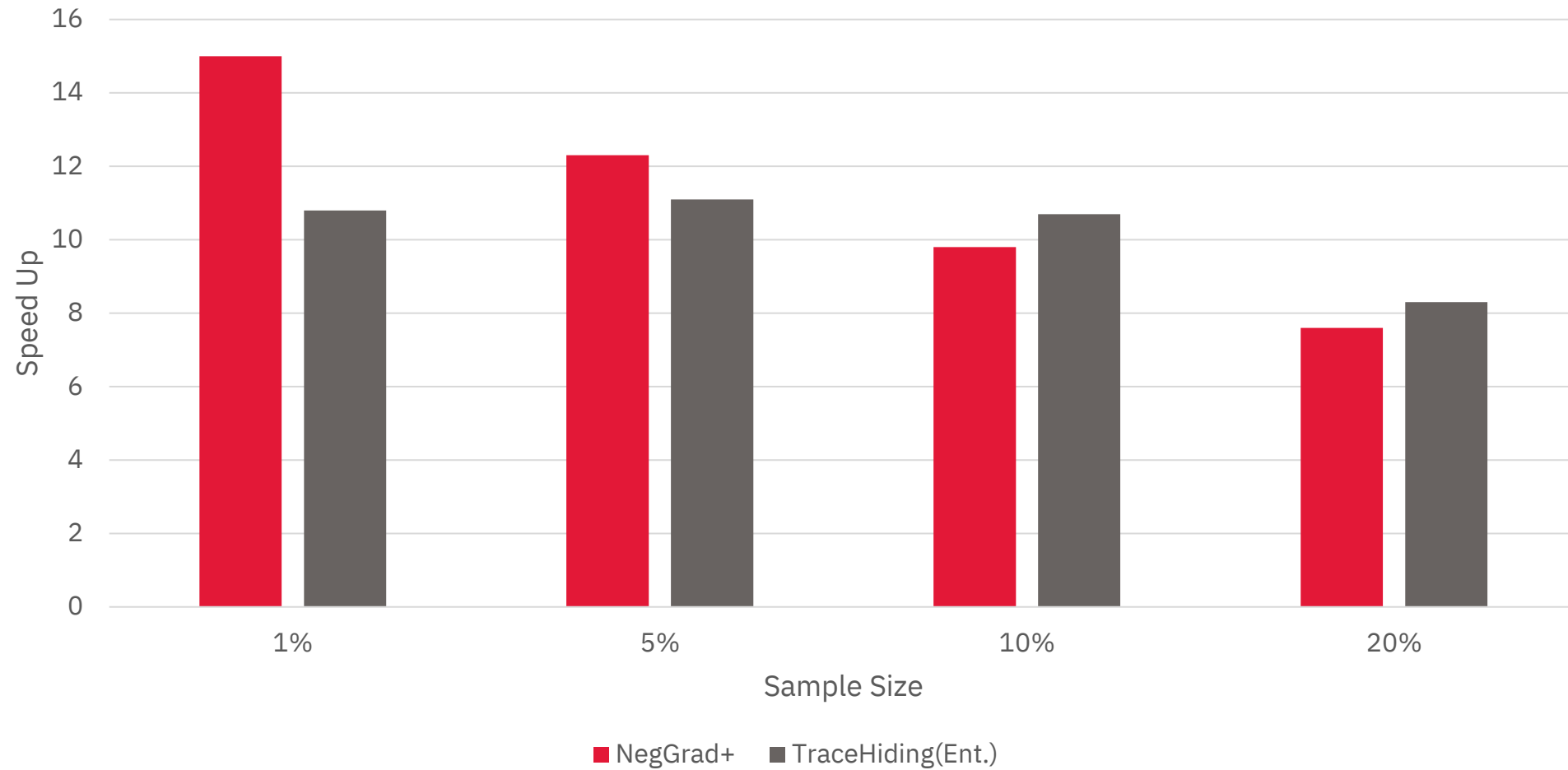
RQ3) Effect of Importance Score



RQ4) Uniform vs Targeted Sampling

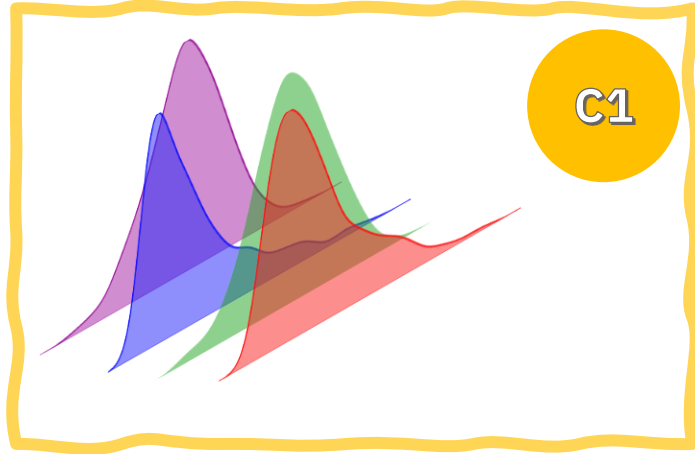


RQ5) Computational Cost



Conclusions

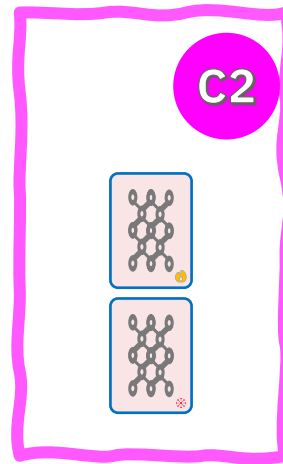
Summary



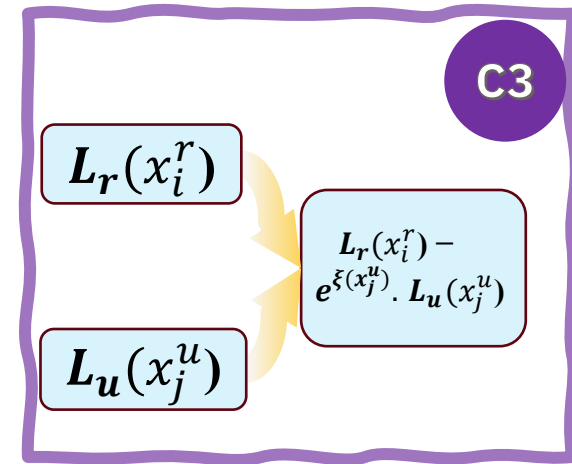
Data-driven Importance Score

- Token Level
- Trajectory Level
- User Level

Hierarchical Importance



Teacher–Student Distillation



Loss Function

Limitations

- No Certified Guarantees for Deletion
- No Interpretability in the Unlearning Process

Thesis Contributions



An Algorithmic Framework
TraceHiding with Variants



TraceHiding
Open-Source Software



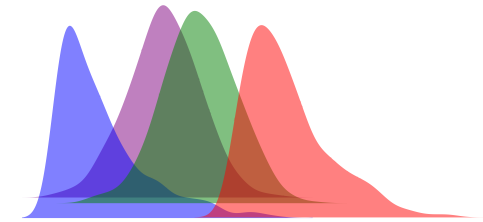
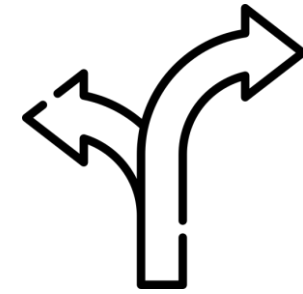
Poin2Hex
(HO Mobility Dataset)

Research Papers:

- **Ali Faraji**, Jing Li, Gian Alix, Mahmoud Alsaeed, Nina Yanin, Amirhossein Nadiri, and Manos Papagelis. 2023. Point2Hex: Higher-order mobility flow data and resources. In *Proceedings of the 31st ACM International Conference on Advances in Geographic Information Systems (ACM SIGSPATIAL '23)*. ACM, New York, NY, USA, Article 69, 1–4.
- **Ali Faraji** and Manos Papagelis. 2025. TraceHiding: An algorithmic framework for machine unlearning in mobility data. *ACM Transactions on Spatial Algorithms and Systems* (submitted).

Future Works

- Beyond Classification: Other Tasks
- Richer Importance Signals
- Streaming and Continual Settings
- Fairness and Compliance Analysis



Thank You!

Questions?