

Trajectory Network Mining

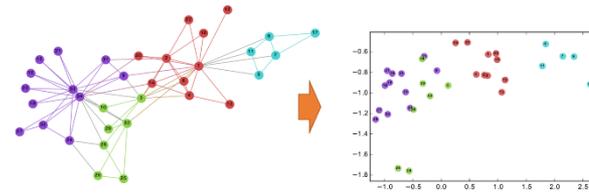
Manos Papagelis

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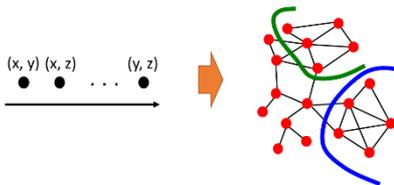
Current research focus



A. Trajectory Network Mining



B. Network Representation Learning



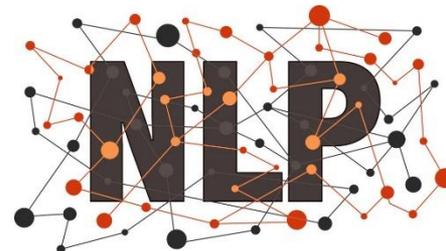
C. Streaming & Dynamic Graphs



D. Social Media Mining & Analysis

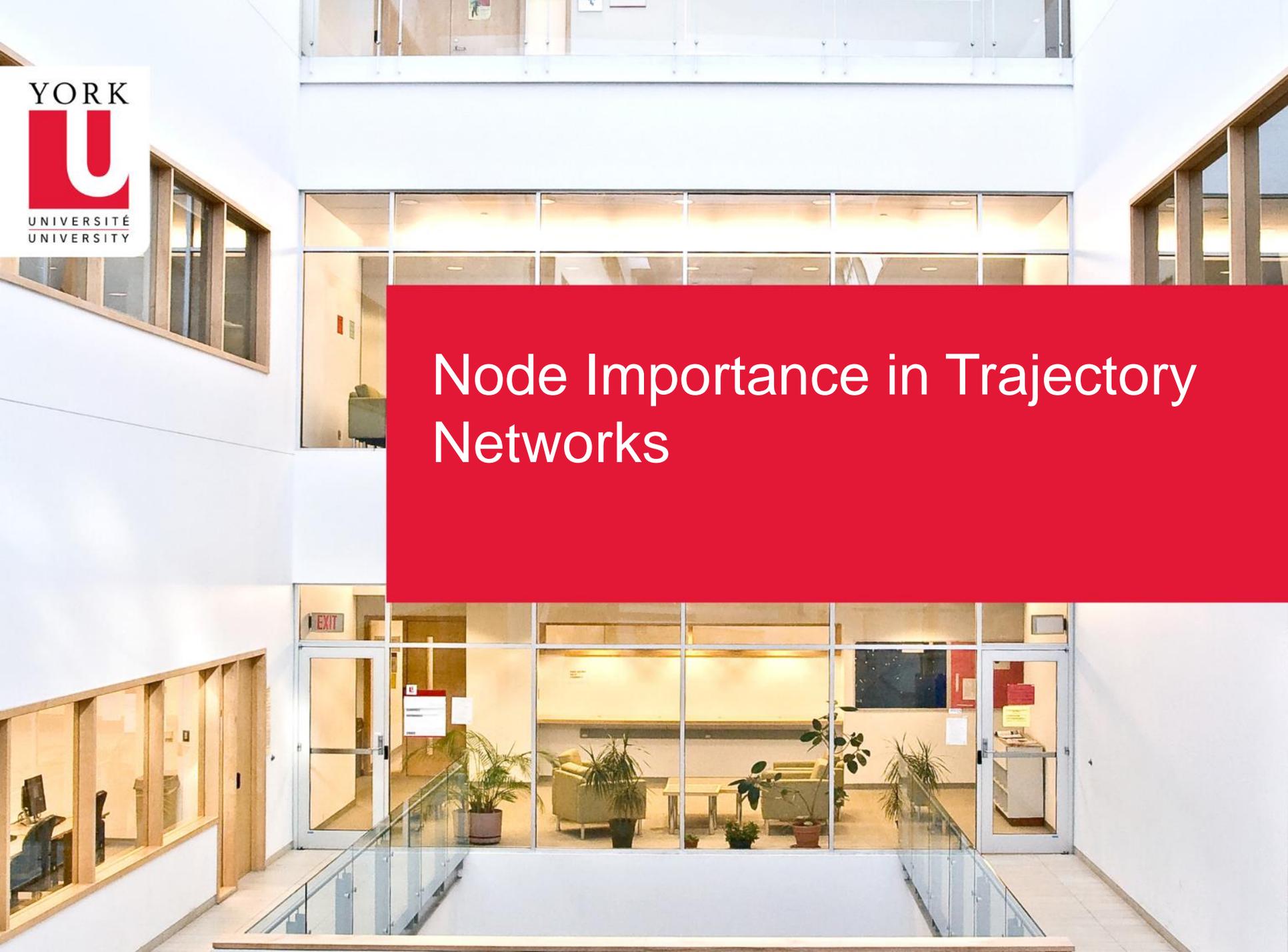


E. City Science / Urban Informatics / IoT

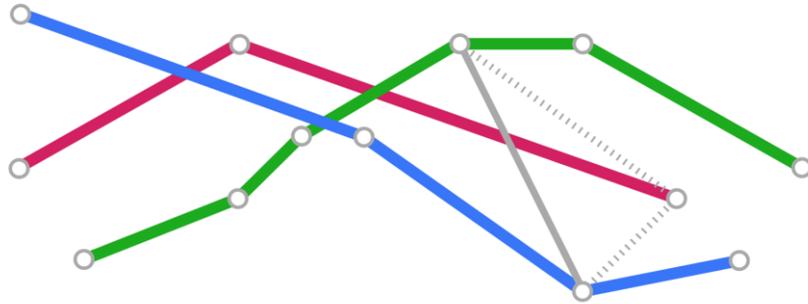


F. Natural Language Processing

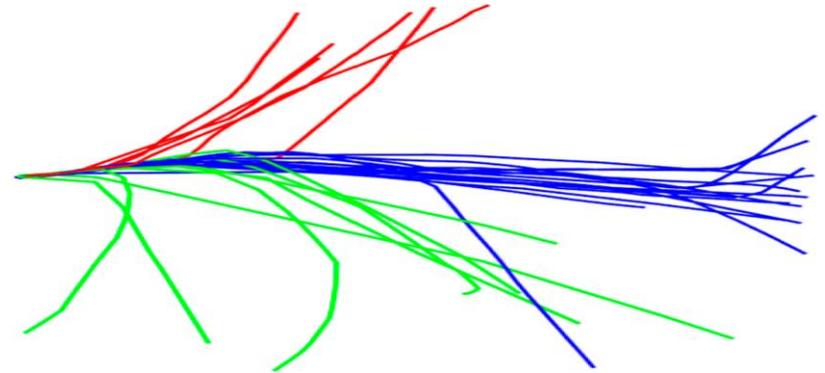
Node Importance in Trajectory Networks



Trajectory data mining



trajectory similarity

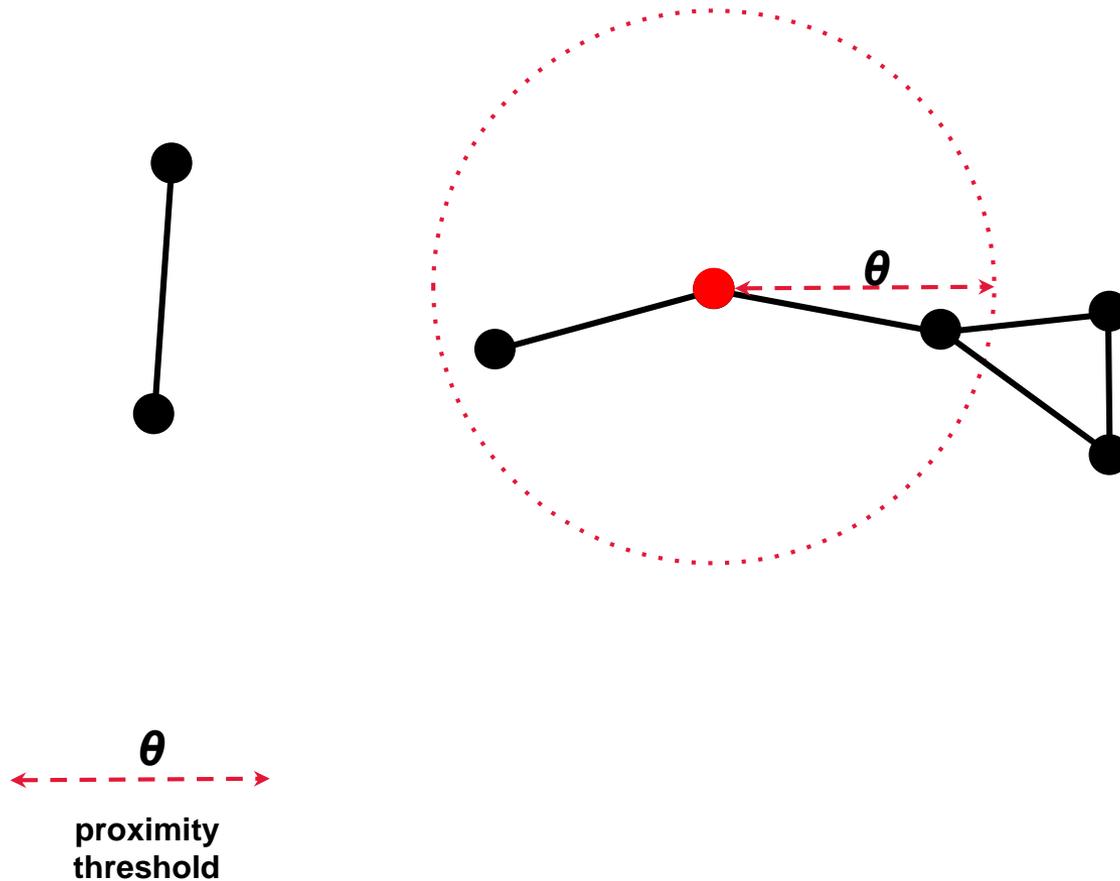


trajectory clustering

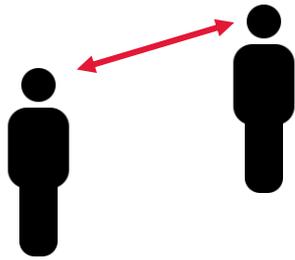
trajectory anomaly detection
trajectory pattern mining
trajectory classification
...more

we care about **network analysis** of moving objects

Proximity networks



Distance can represent



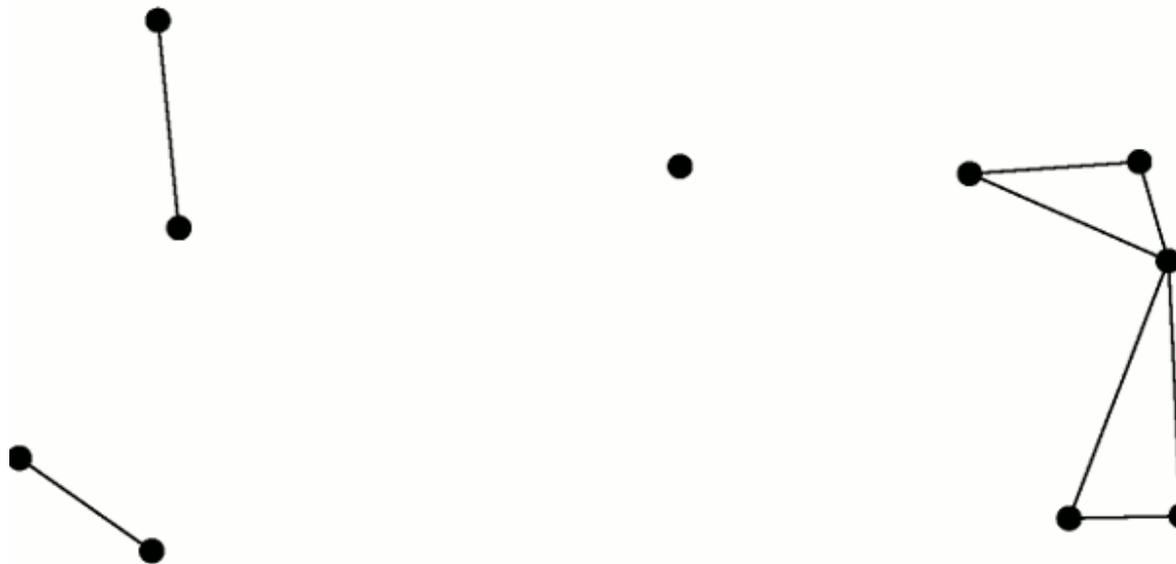
line of sight



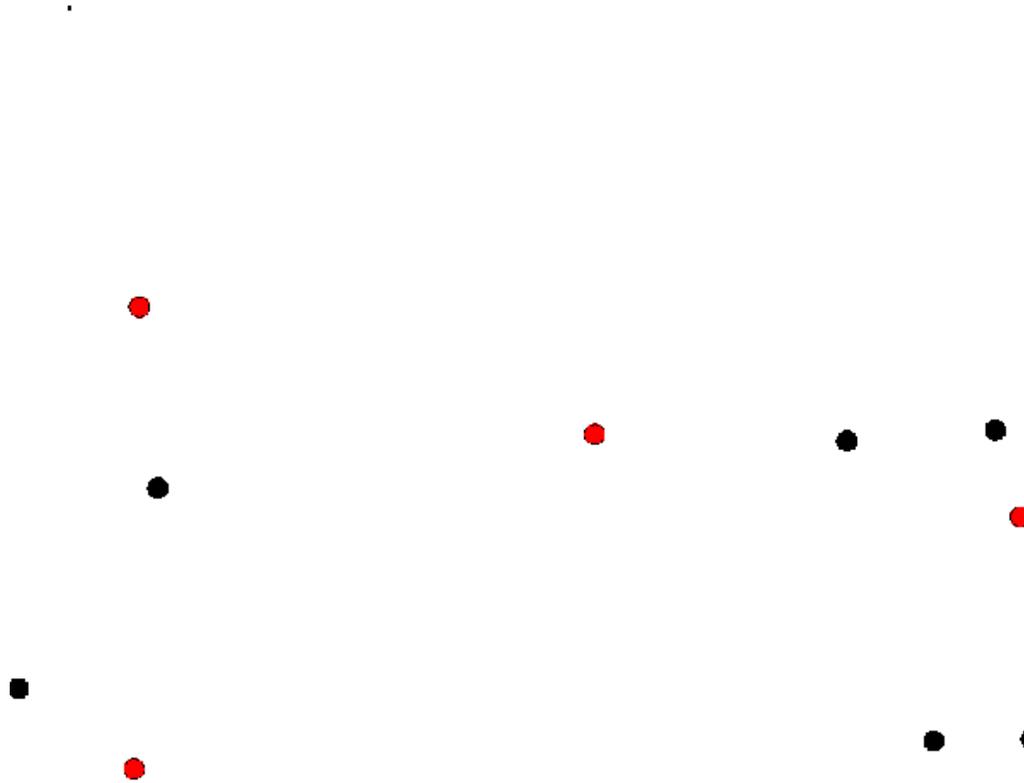
wifi/bluetooth signal range

Trajectory networks

0



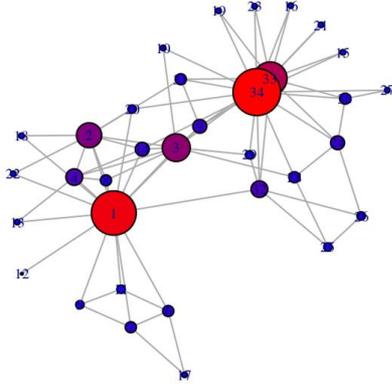
The problem



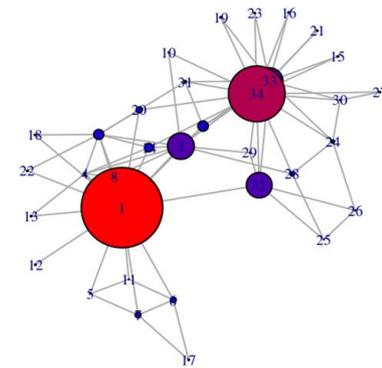
Input: logs of trajectories (x, y, t)
Output: node importance metrics

Node Importance

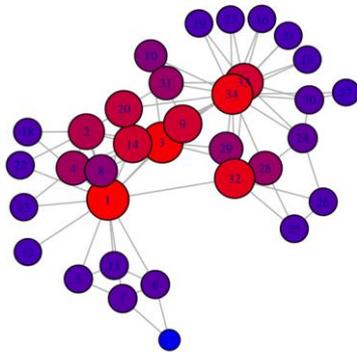
Node importance in static networks



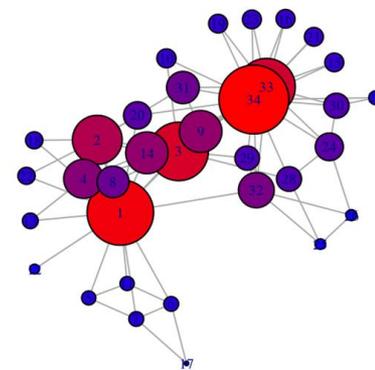
Degree centrality



Betweenness centrality

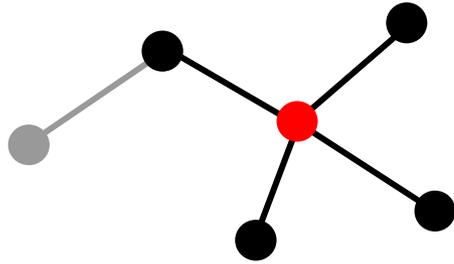


Closeness centrality

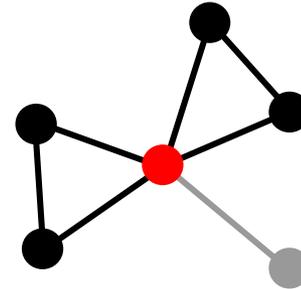


Eigenvector centrality

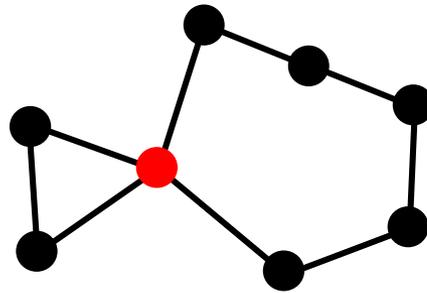
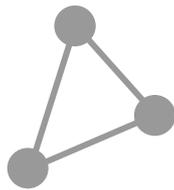
Node importance in TNs



node degree **over time**

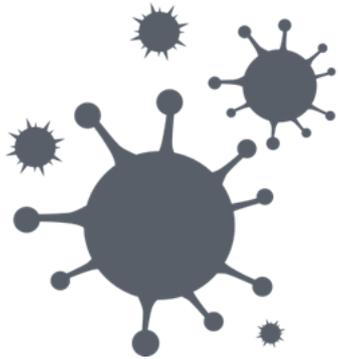


triangles **over time**



connected components **over time**
(connectedness)

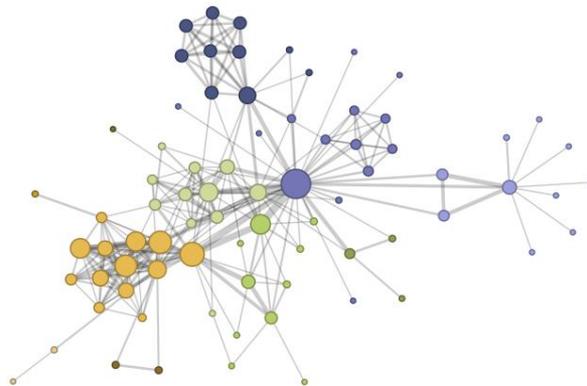
Applications



infection spreading



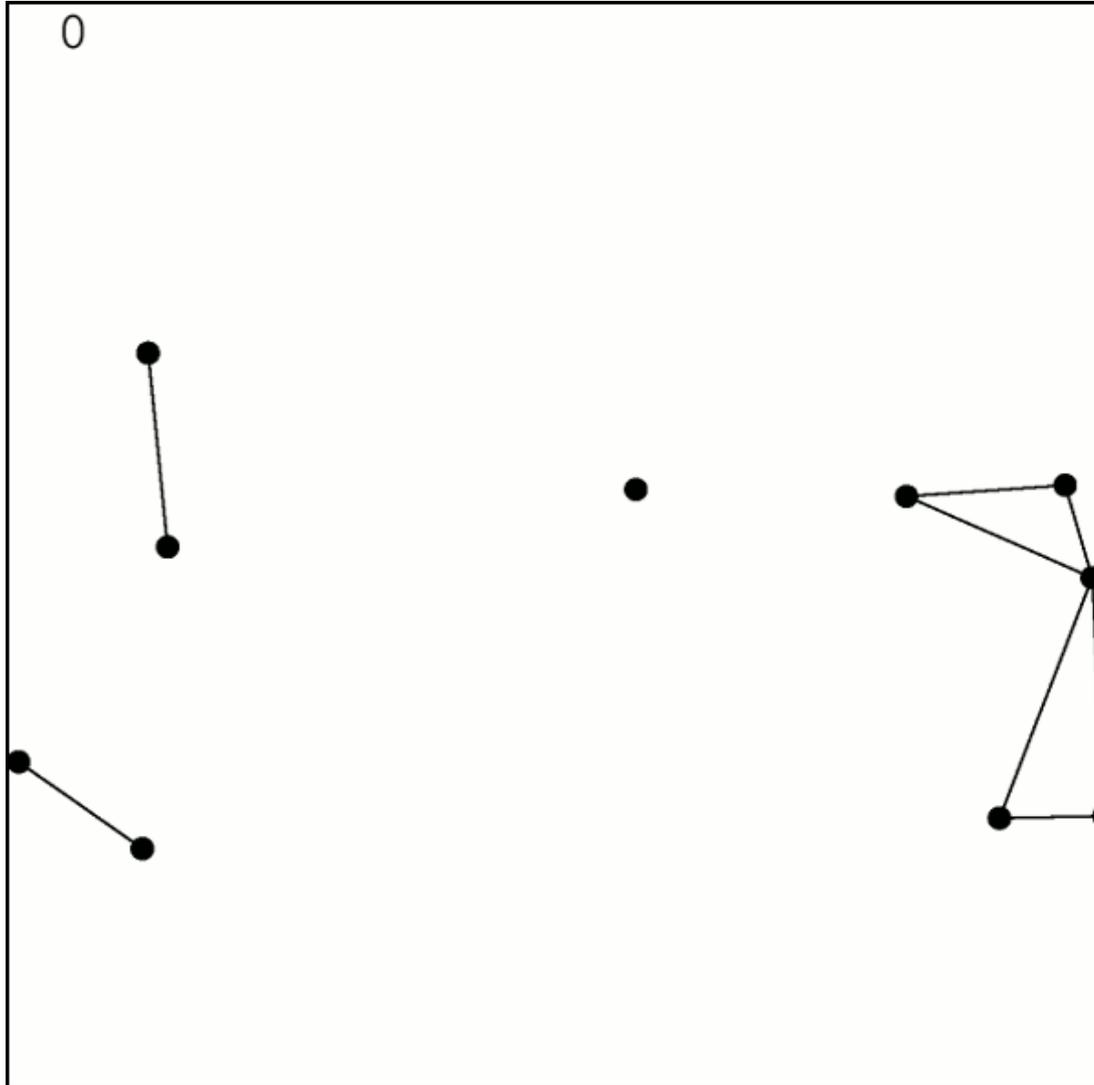
wireless signal security



rich dynamic network analytics

Evaluation of Node Importance in Trajectory Networks

Naive approach



Naive approach

For **every** discrete time unit:

1. get static **snapshot** of network
2. run **static** node importance **algorithms** on snapshot

Aggregate results at the end

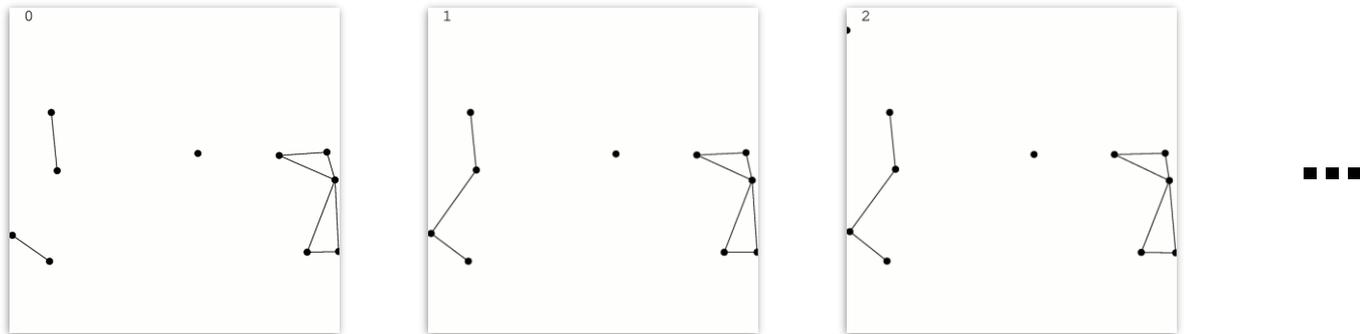
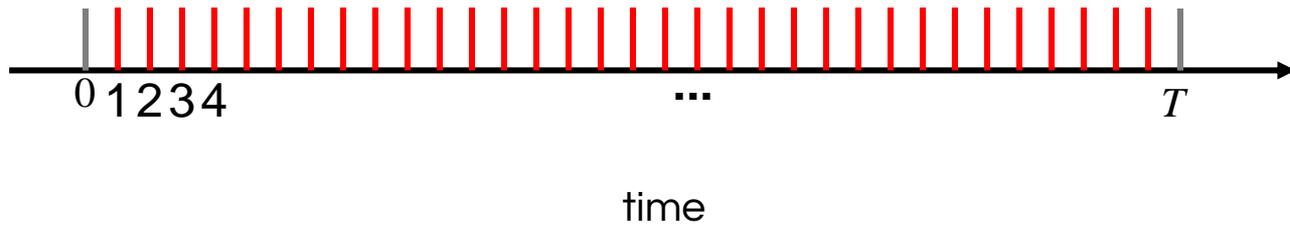
Streaming approach

Similar to naive, but:

- **no final aggregation**
- results calculated **incrementally** at every step

Still **every time** unit

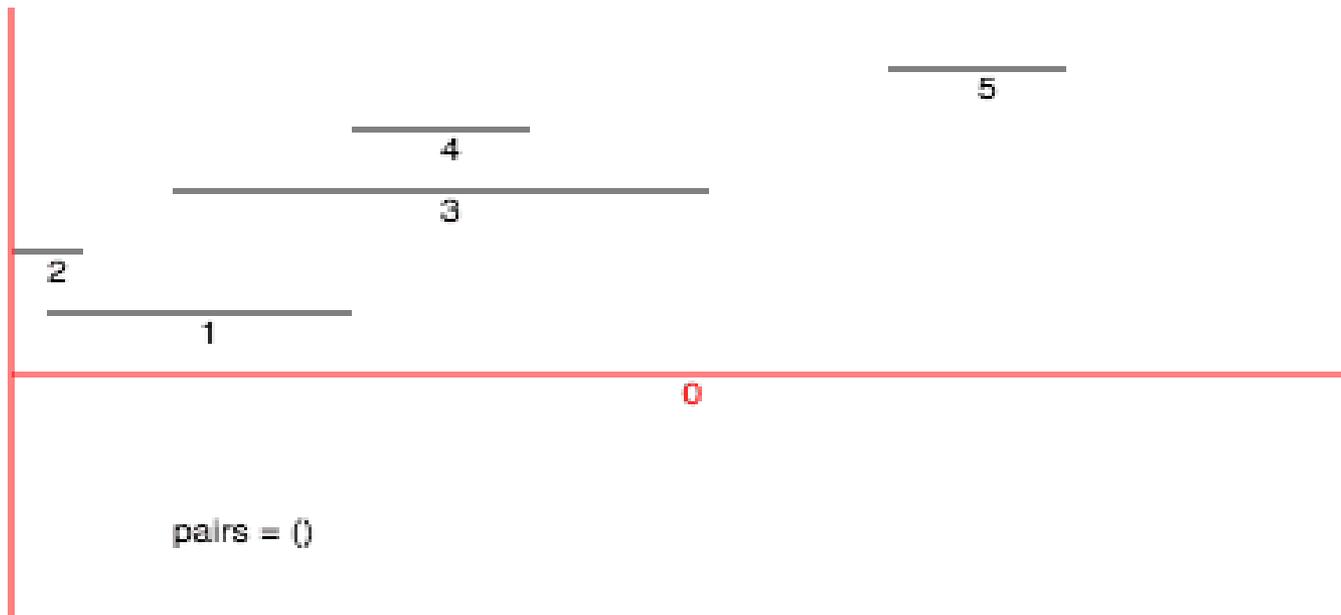
Every discrete time unit



Sweep Line Over Trajectories (SLOT)

Sweep line algorithm

A **computational geometry** algorithm that given **line segments** computes line segment **overlaps**



Efficient **one pass** algorithm that only processes line segments at the **beginning** and **ending** points

SLOT: Sweep Line Over Trajectories

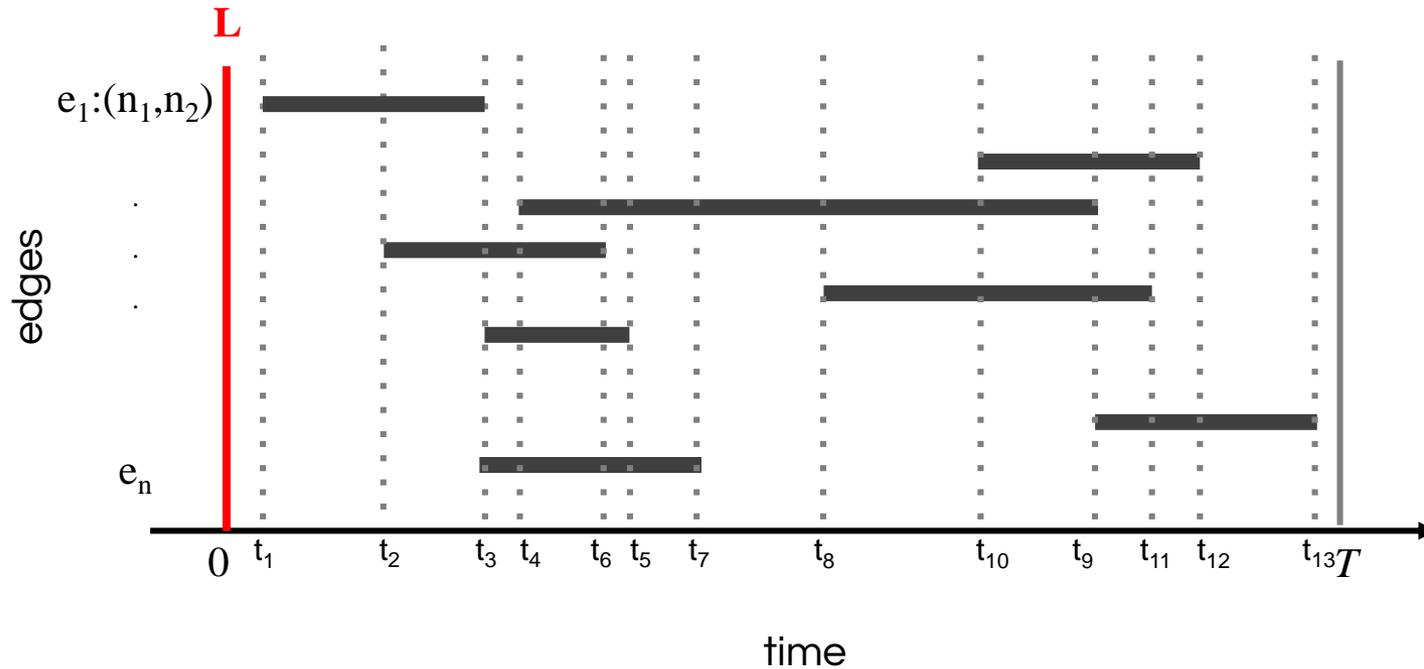
(algorithm sketch)

represent TN **edges** as **time intervals**

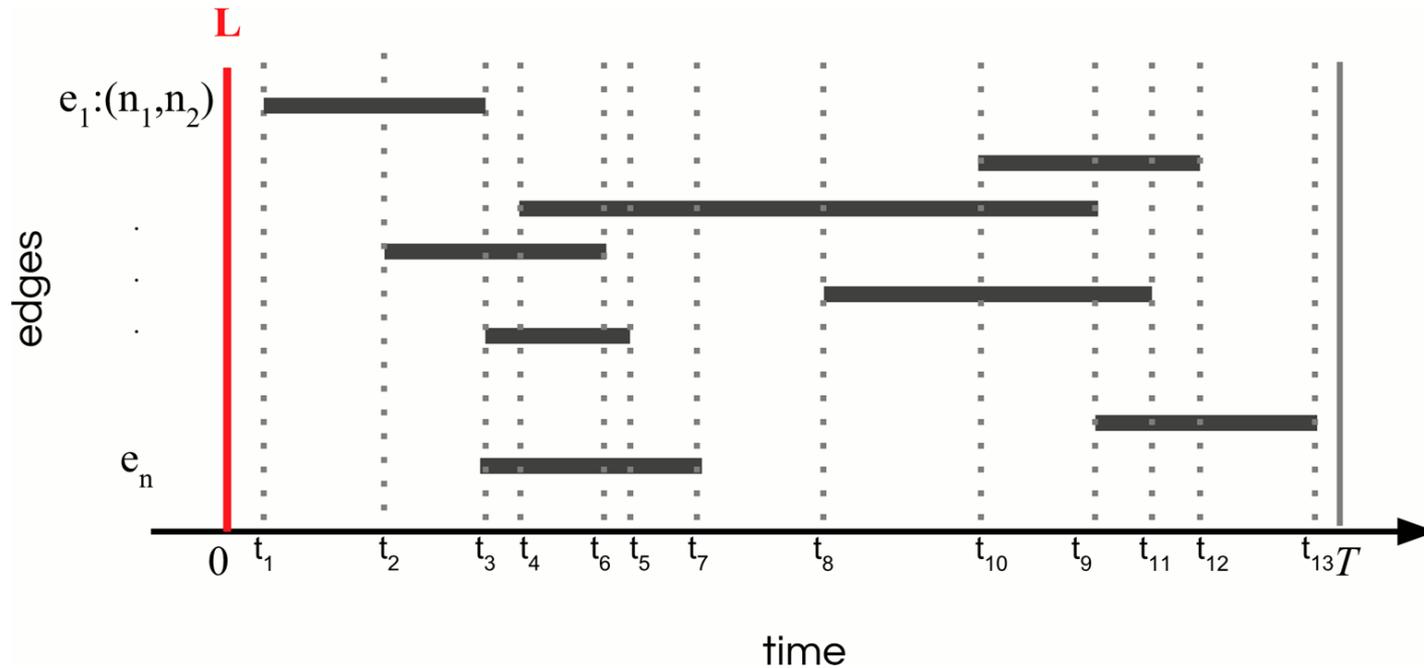
apply **variation** of sweep line algorithm

simultaneously compute *node degree, triangle membership, connected components* in **one pass**

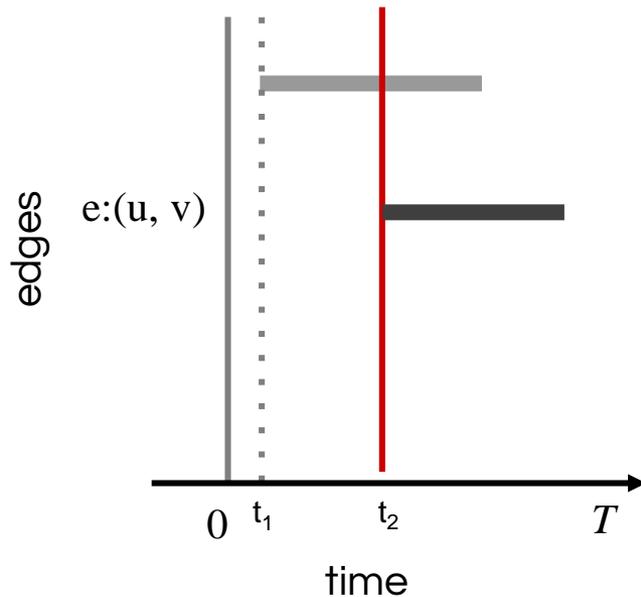
Represent edges as time intervals



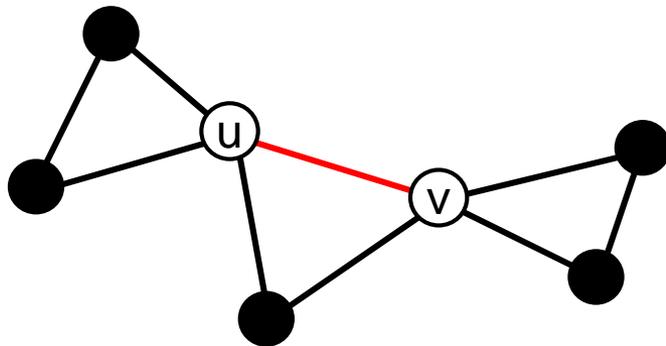
SLOT: Sweep Line Over Trajectories



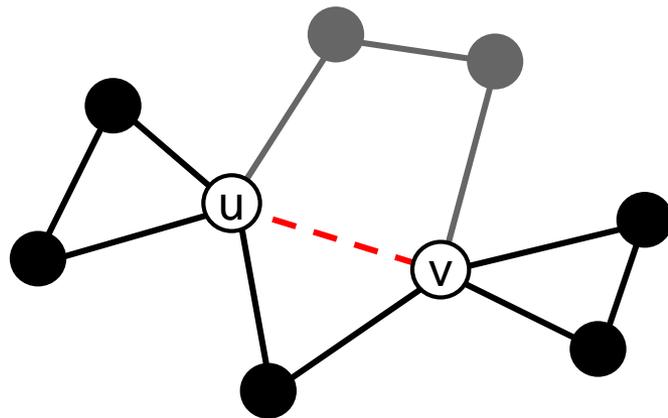
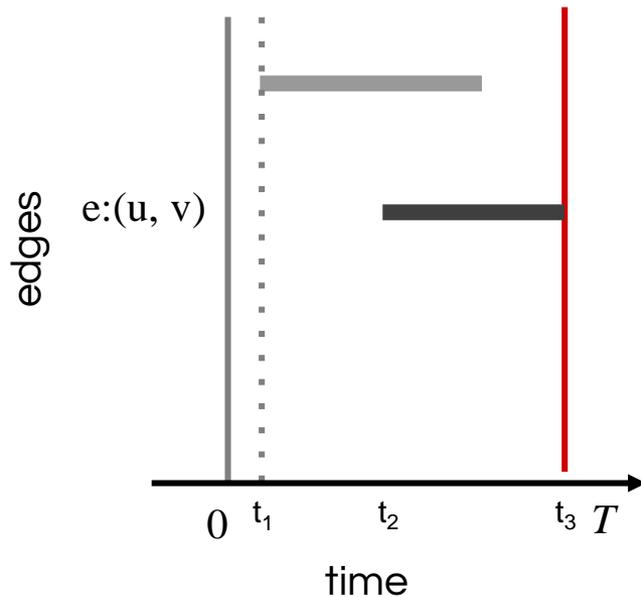
At every edge **start**



- **node degree**
 - nodes **u**, **v** now connected
 - increment **u**, **v** node degrees
- **triangle membership**
 - did a triangle just form?
 - look for **u**, **v** common neighbors
 - increment triangle (**u**, **v**, **common**)
- **connected components**
 - did two previously unconnected components connect?
 - compare old components of **u**, **v**
 - if no overlap, merge them



At every edge **stop**



- **node degree**
 - nodes **u**, **v** now disconnected
 - decrement **u**, **v** degree
- **triangle membership**
 - did a triangle just break?
 - look for **u**, **v** common neighbors
 - decrement triangle (**u**, **v**, **common**)
- **connected components**
 - did a component separate?
 - BFS to see if **u**, **v** still connected
 - if not, split component to two

SLOT: At the end of the algorithm ...

node degrees: start/end time, duration

triangles: start/end time, duration

connected components: start/end time, duration

Exact results (not approximations)

e.g. node degree of u $d(u)$ is:

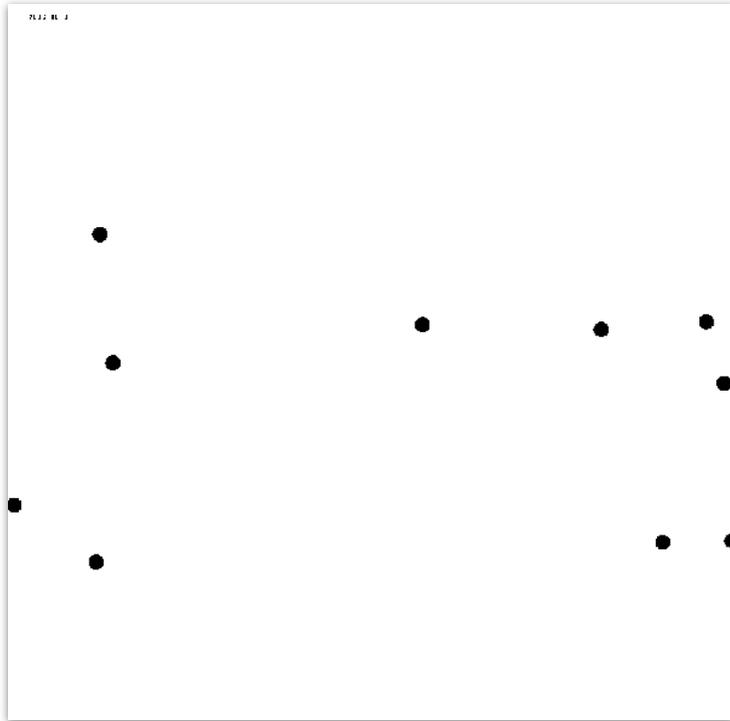
$d(u) = 5$, from $t=0$ until $t=10$ duration=10

$d(u) = 6$, from $t=10$ until $t=50$ duration=40

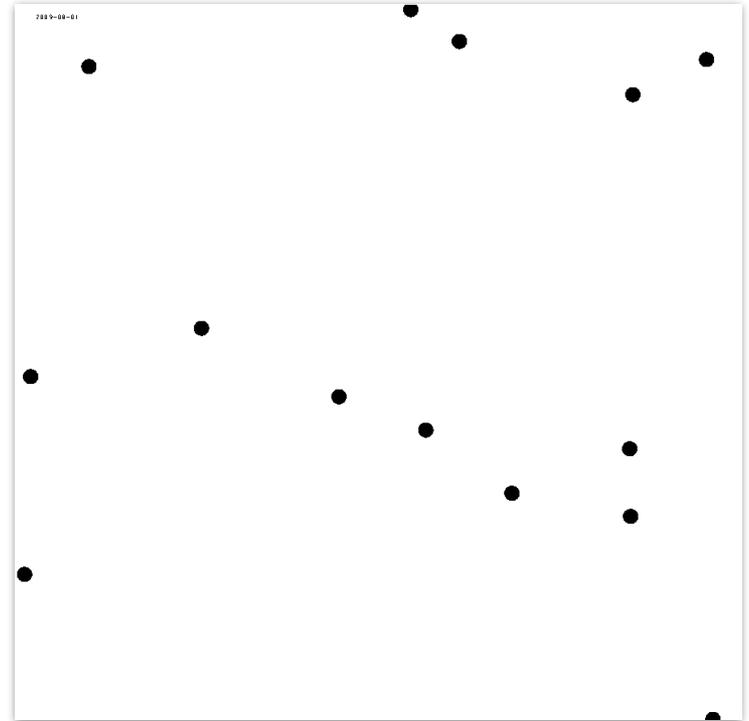
$d(u) = 4$, from $t=50$ until $t=100$ duration=50

Evaluation of SLOT

Simulating trajectories

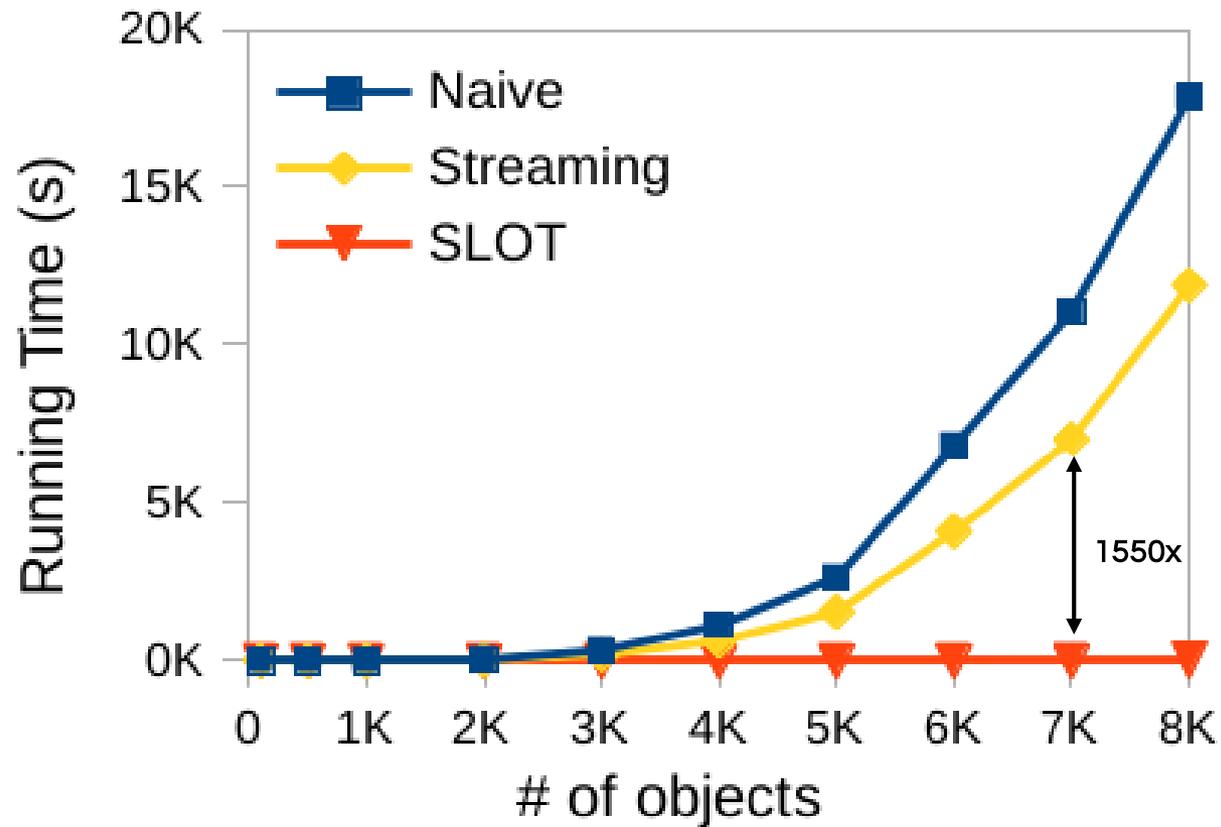


constant velocity

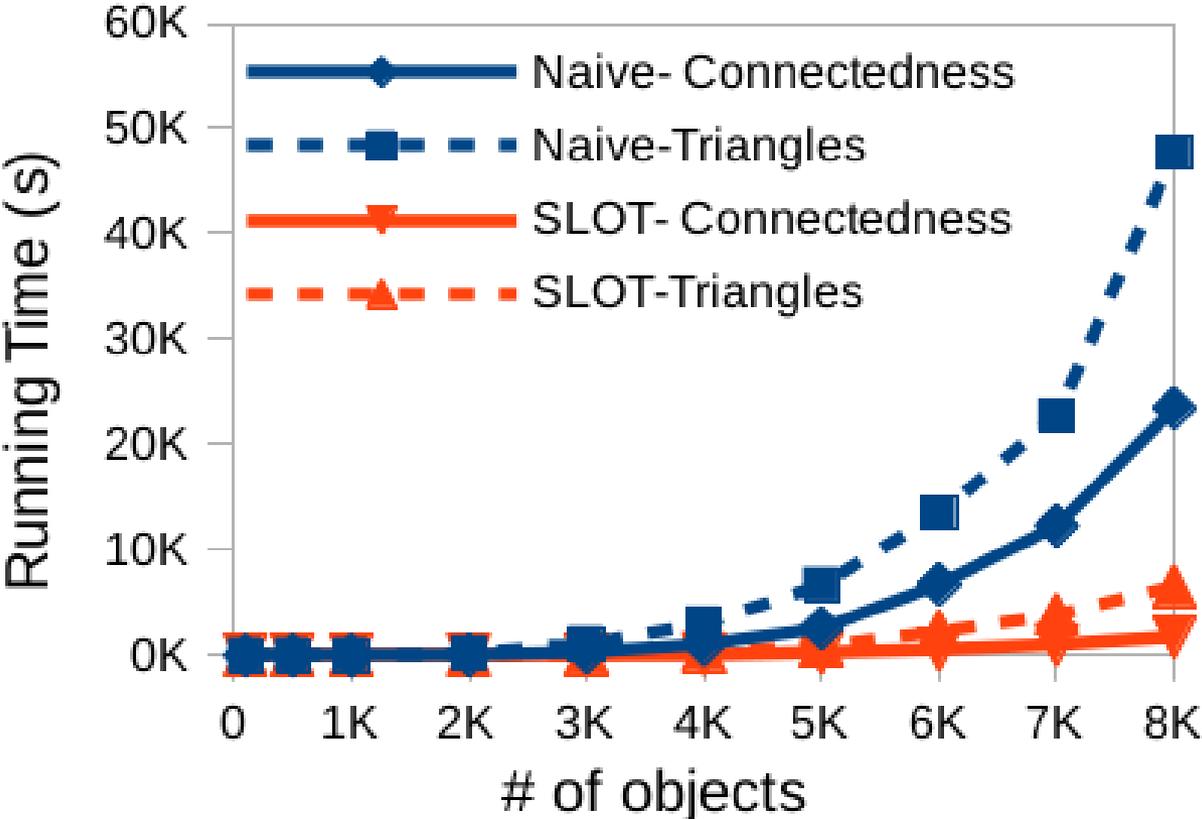


random velocity

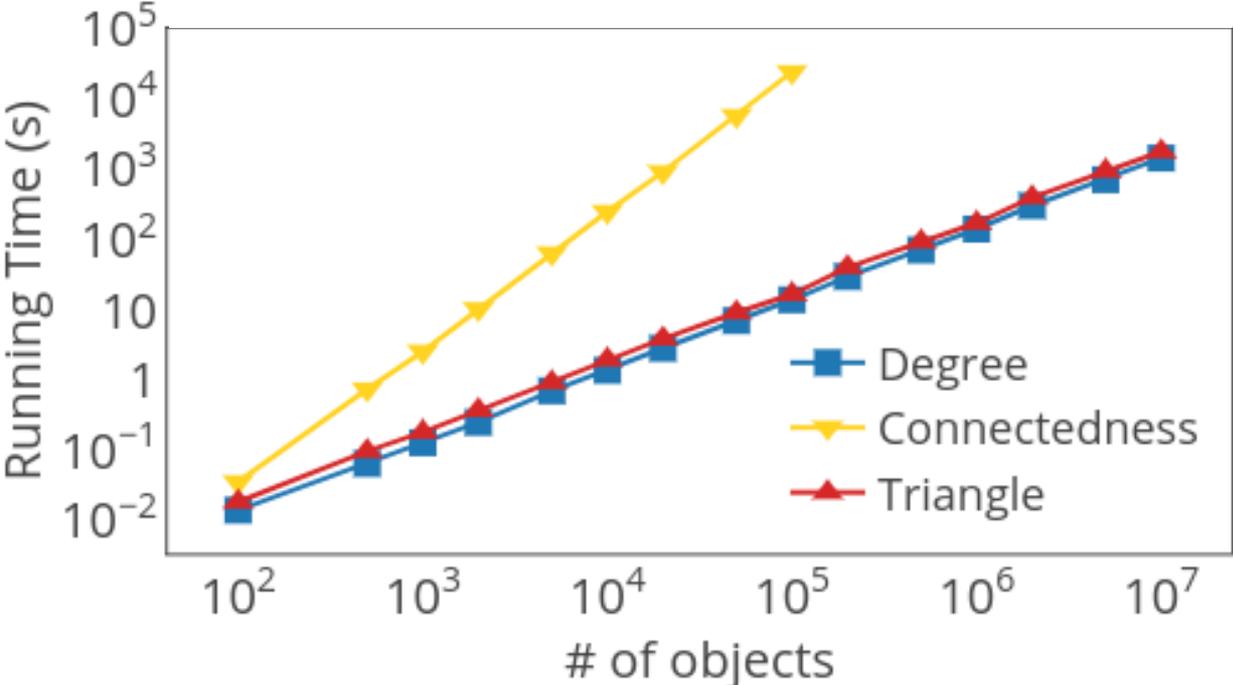
Node degree



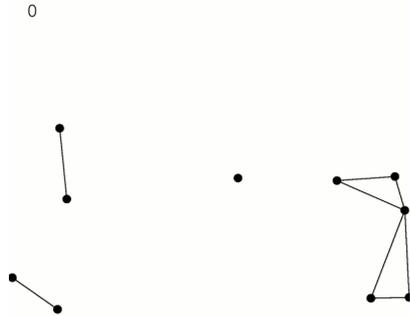
Triangle membership / connected components



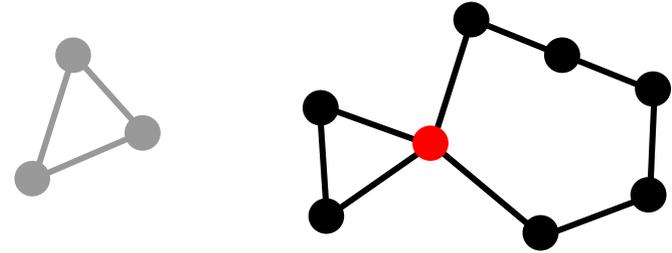
SLOT Scalability



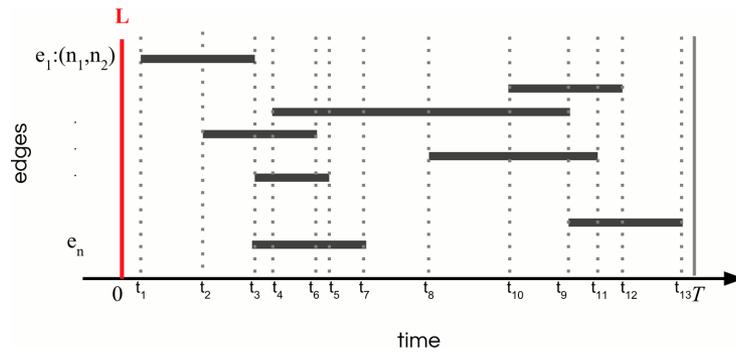
Takeaway



trajectory networks



network importance **over time**



SLOT algorithm

SLOT properties:

- fast
- exact
- scalable

Seagull migration trajectories



data from Wikelski et al. 2015

YORK



UNIVERSITÉ
UNIVERSITY

Group Pattern Discovery of Pedestrian Trajectories



Pedestrian trajectories



**what is a
group?**

**many definitions,
many algorithms**

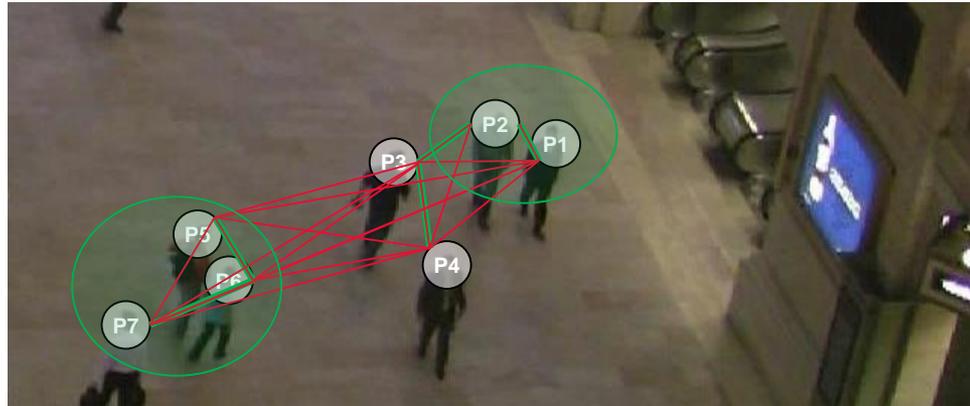
e.g., *flock, convoy, evolving-clusters, gathering-pattern, ...* [ACM TIST Tutorial 2015]

Finding pedestrian groups

Local Grouping

Intuitive method

Spatial-only



proximity threshold θ

key idea

find **pairs** of pedestrians x, y where $\text{distance}(x, y) < \theta$

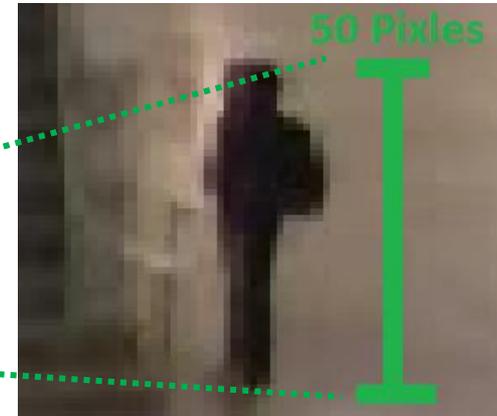
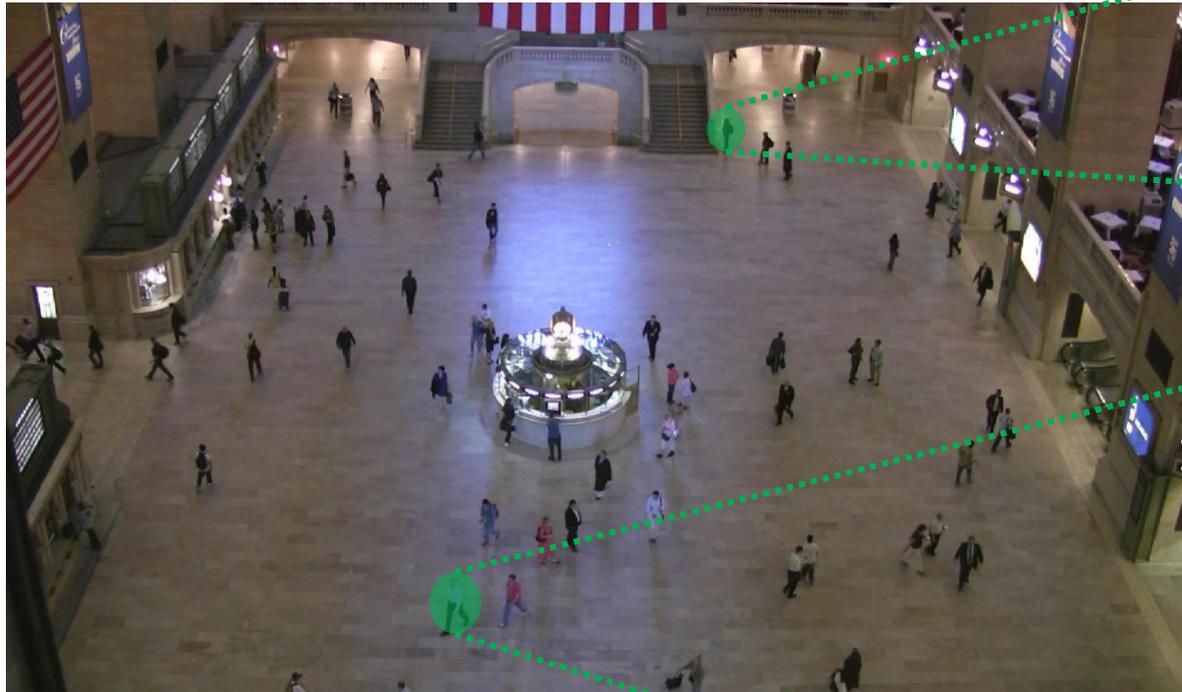
expand **pairs** to discover **groups**

Local grouping



Challenge: Projection into ground plane

High perspective distortion - pedestrians closer to the camera appear larger than the ones farther away



Estimated Homography to overcome this distortion

expand the key idea
to include the
time dimension

Global groups vs. Time-window groups



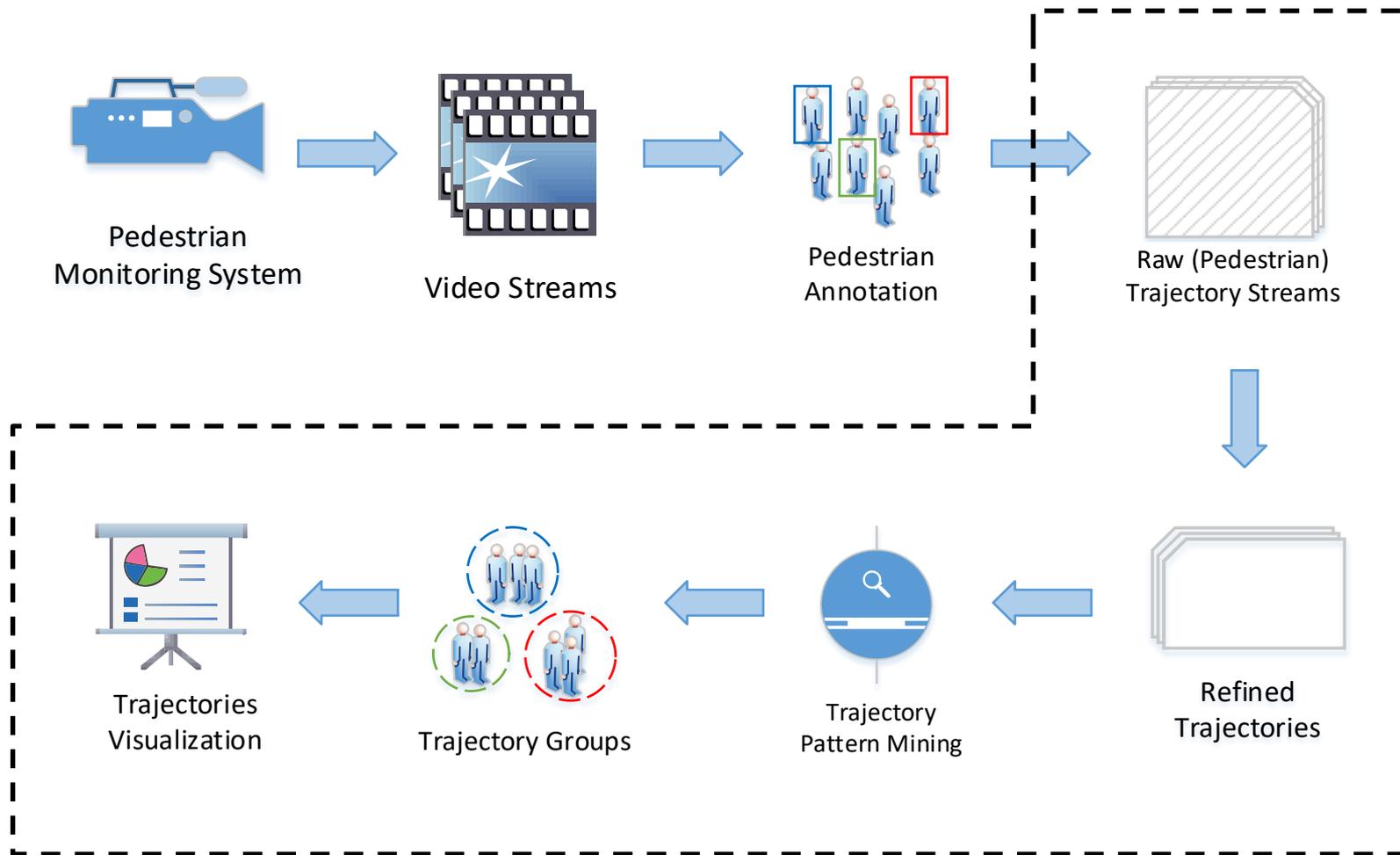
global
grouping

time-window
grouping

Trajectolizer

Demo

Trajectolizer: System Overview





Trajectolizer: Interactive Demo

descriptive statistics about the current frame

timeline slider area to navigate video frames

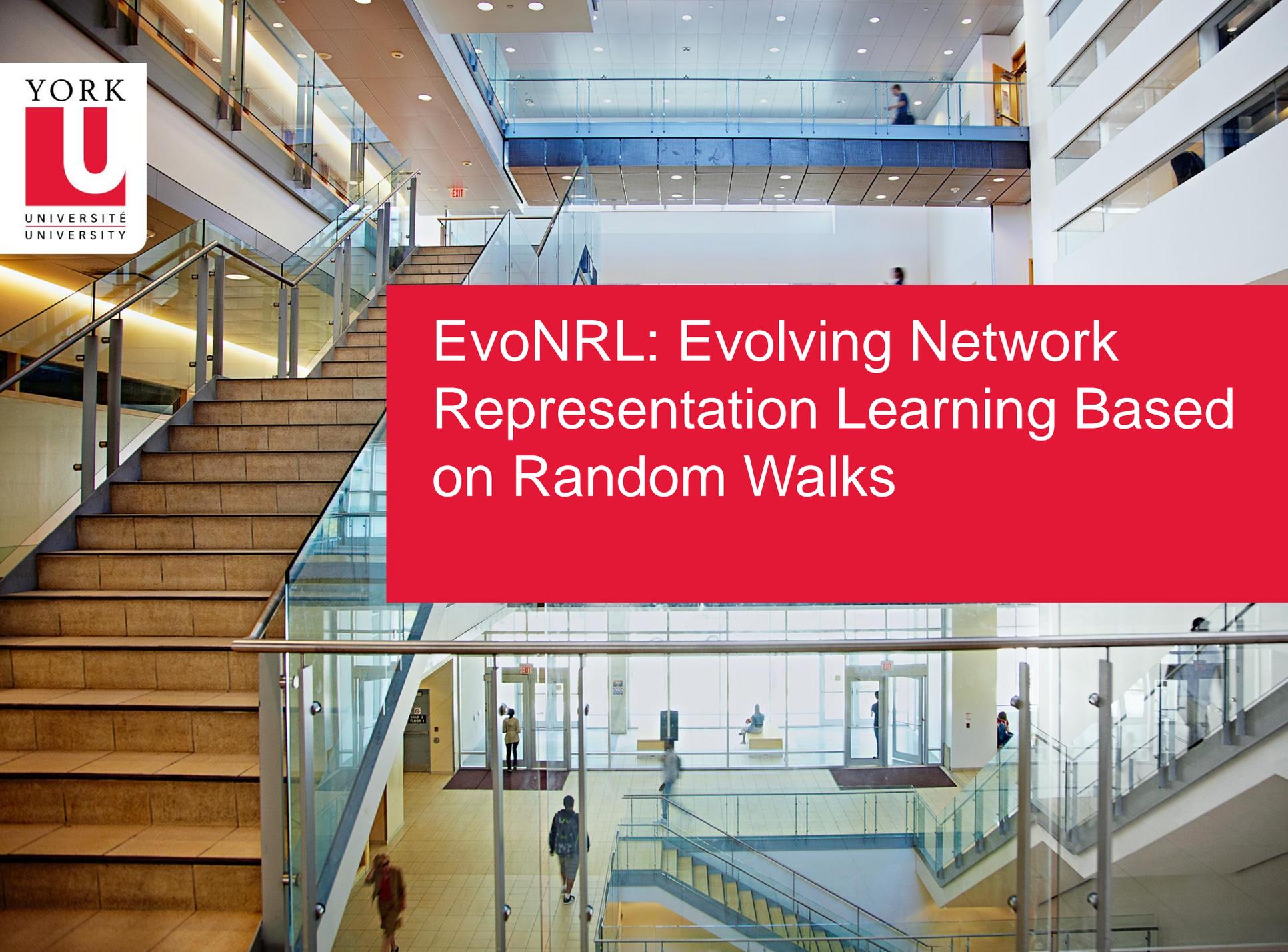
The interface is divided into several sections:

- Video Panel (C):** Displays frame information for Frame:1. It lists the number of pedestrians (70), average time spent (00:01:41), and a list of pedestrian IDs: P2 178, P8 145, P10 432, P11 469, P15 154, P28 228, P29 203, P36 1322, P38 232, P45 196, P46 195, P51 722, P63 743, P65 269, P68 141, P69 243, and P70 144.
- Groups Panel (D):** Shows proximity distance settings (Min: 10, Max: 8) and a list of neighbors for pedestrian 38, including P:2, P:41, P:46, P:65, P:95, P:108, P:123, and P:151.
- Timeline (B):** A line graph at the top showing the number of pedestrians in frames over time.
- Main View (A):** A top-down camera view of a large indoor space with many pedestrians. Green lines represent individual trajectories, and small circles with IDs mark the current positions of the tracked pedestrians.

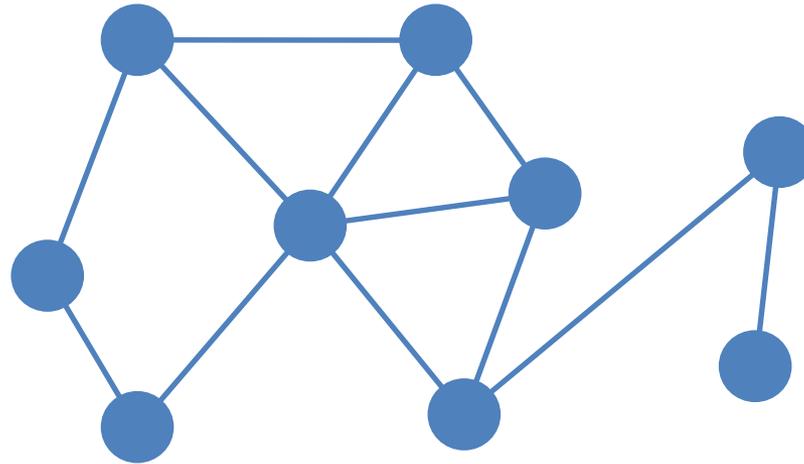
grouping analysis

current frame with pedestrian IDs and trajectories

[Live Demo](#)



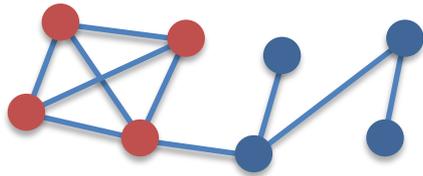
EvoNRL: Evolving Network
Representation Learning Based
on Random Walks



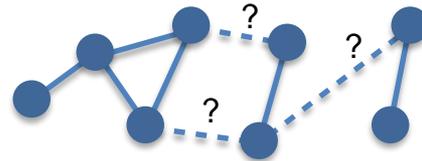
networks

(universal language for describing complex data)

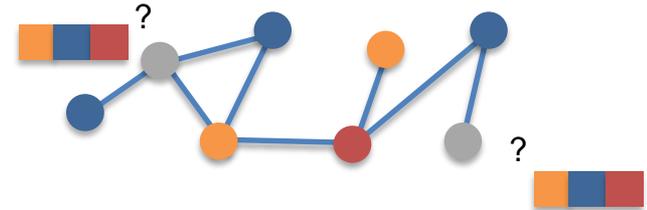
Classical ML Tasks in Networks



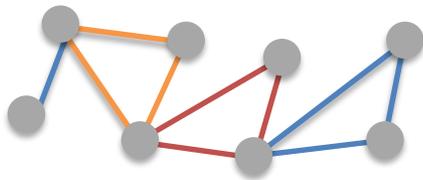
community detection



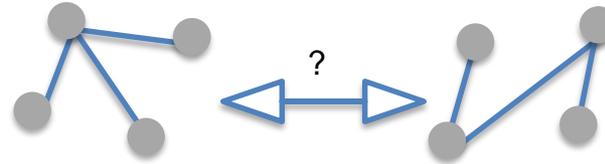
link prediction



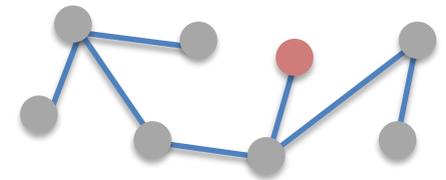
node classification



triangle count



graph similarity



anomaly detection

Limitations of Classical ML Tasks

expensive computation

(high dimension computations)

extensive domain knowledge

(task specific)

Network Representation Learning (NRL)

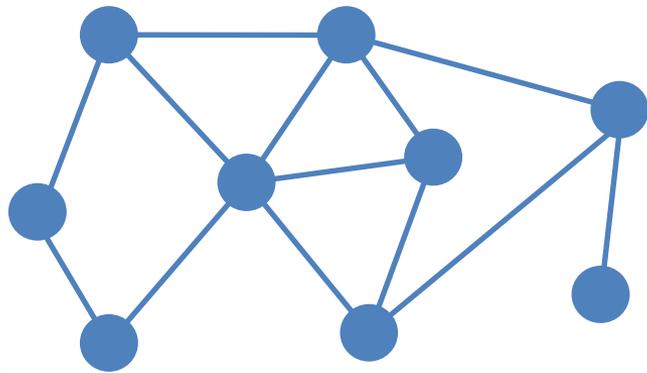
faster computations

(low dimension computations)

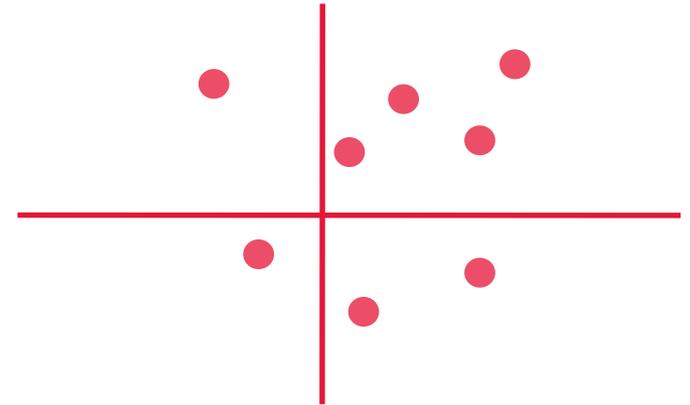
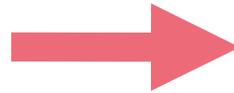
agnostic domain knowledge

(task independent)

Network Representation Learning (NRL)



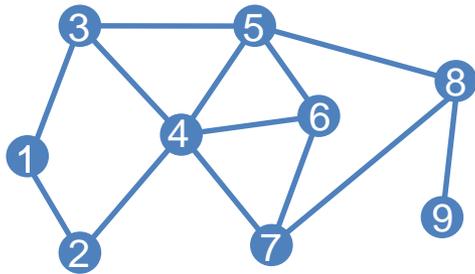
Network



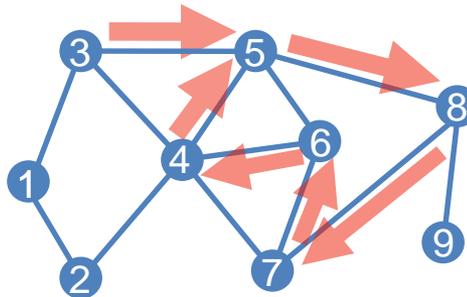
Low-dimension space

several network structural properties can be learned/embedded
(nodes, edges, subgraphs, graphs, ...)

Random Walk-based NRL



Input network



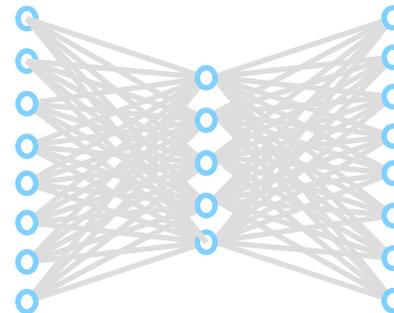
Obtain a set of random walks

3 5 8 7 6 4 5

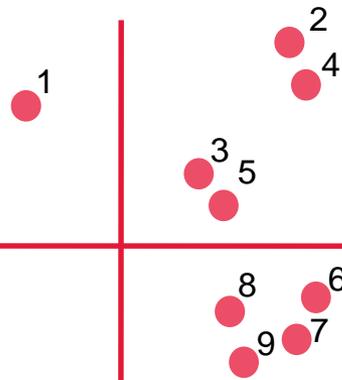


1	3 5 8 7 6 4 5
2	1 3 5 8 7 6 5
·	·
·	·
·	·
·	·
87	8 5 4 3 5 6 7
88	4 5 6 7 8 9
89	2 1 3 5 6 7 8
90	7 4 2 1 3 5 6

Treat the set of random walks as sentences



Feed sentences to Skip-gram NN model



Learn a vector representation for each node

Random Walk-based NRL

StaticNRL

DeepWalk

node2vec

...

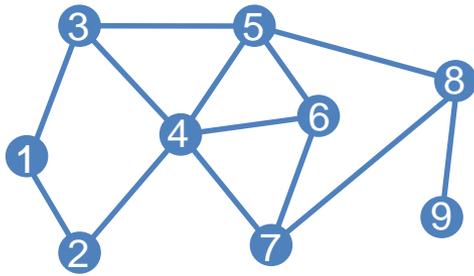
But...

real-world networks are
constantly changing

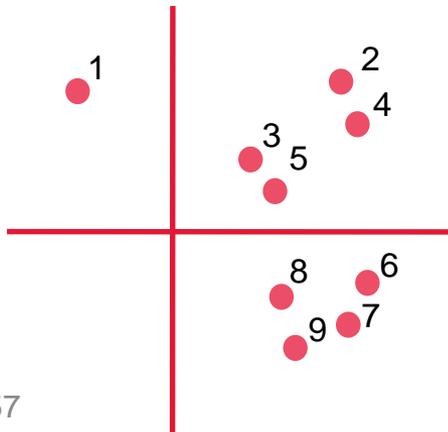
how can we learn
representations of an
evolving network?

Naive Approach

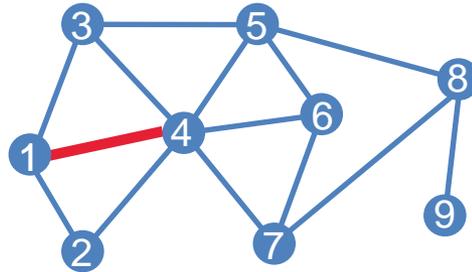
t = 0



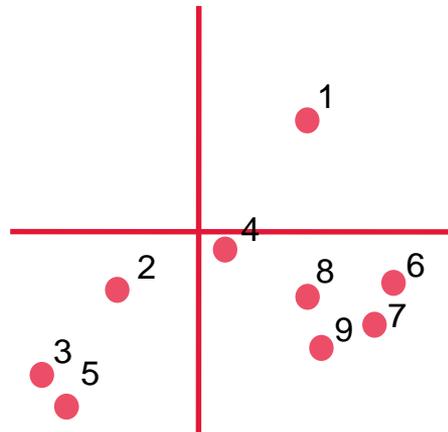
↓
StaticNRL



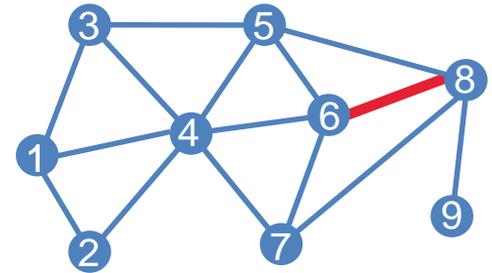
t = 1



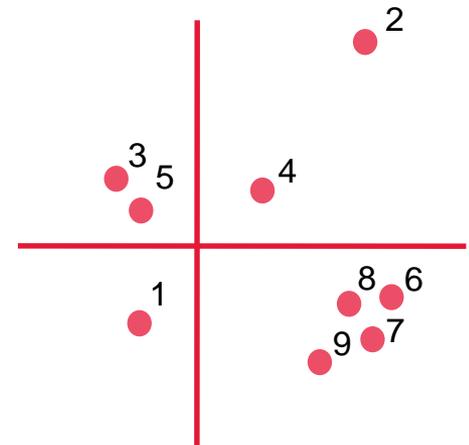
↓
StaticNRL



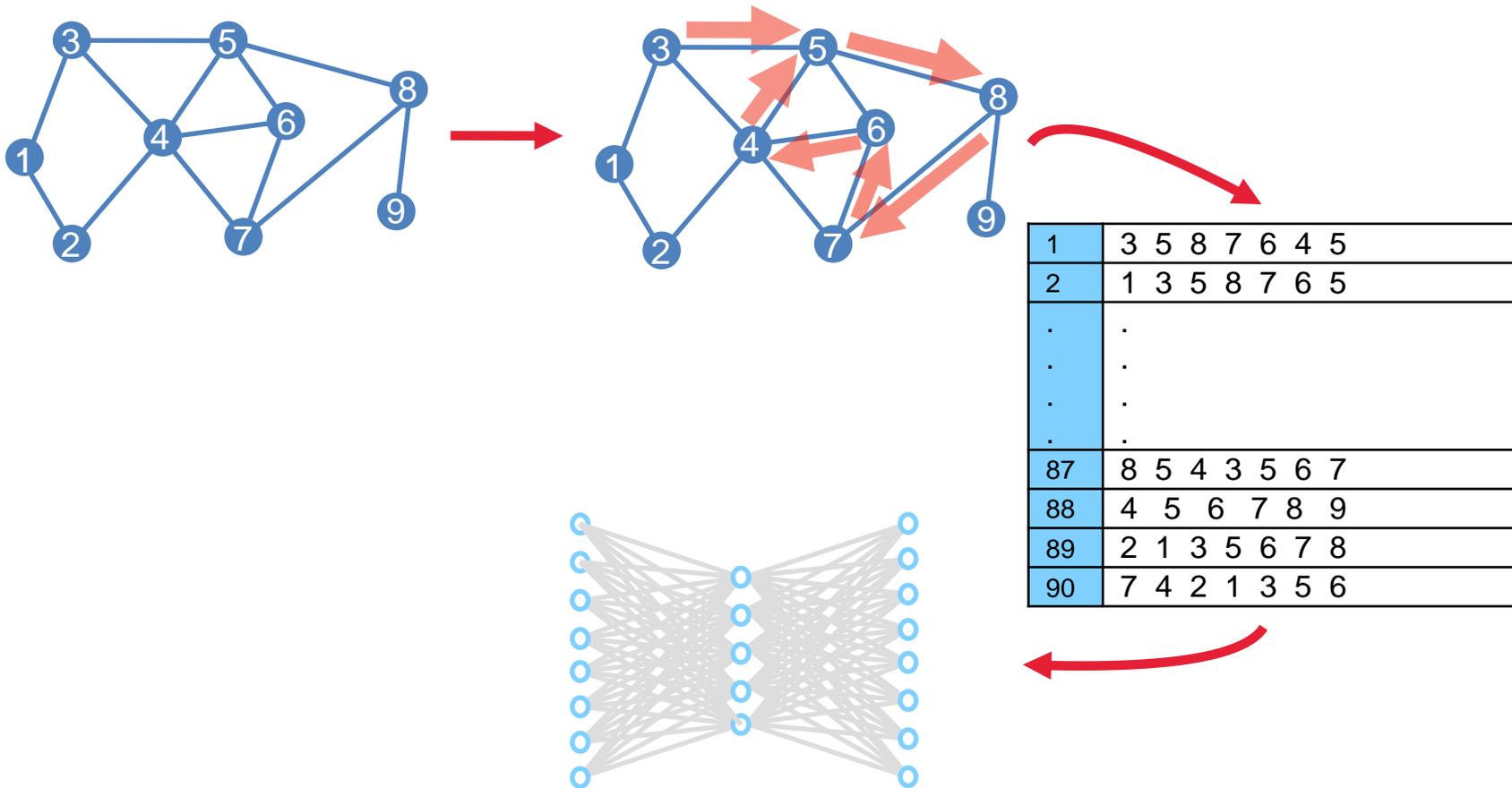
t = 2



↓
StaticNRL



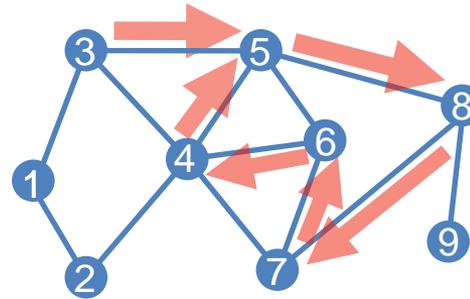
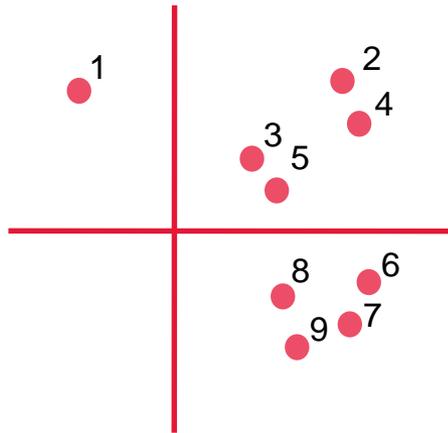
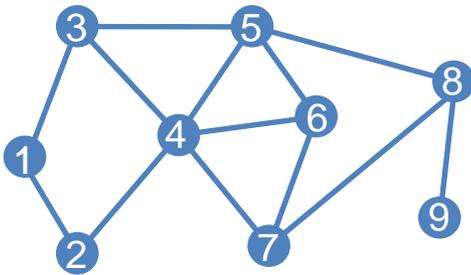
Limitation #1



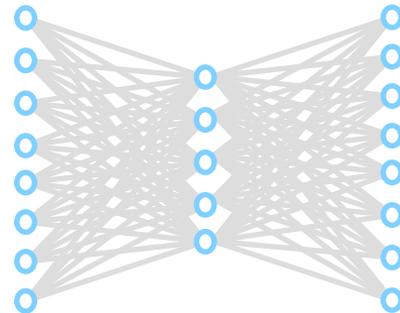
time expensive

Limitation #2

t = 0

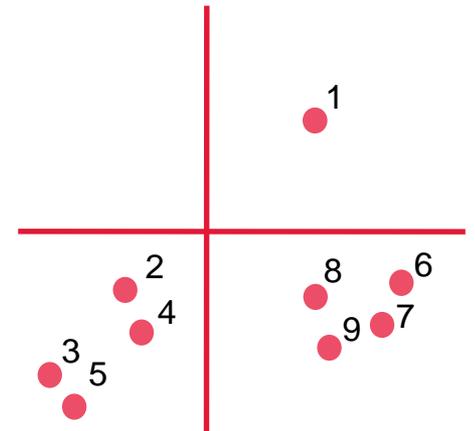
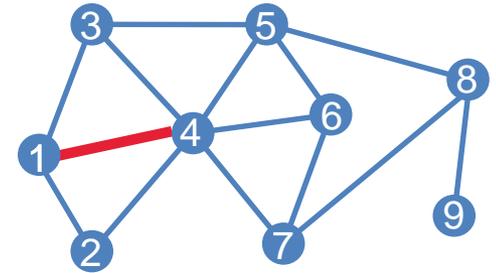


Random Walks



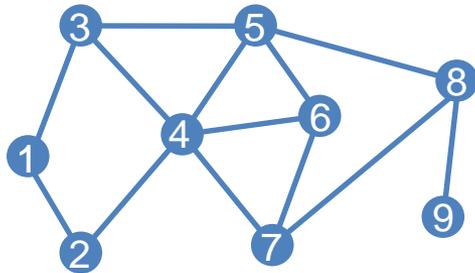
Neural Network Optimization

t = 1

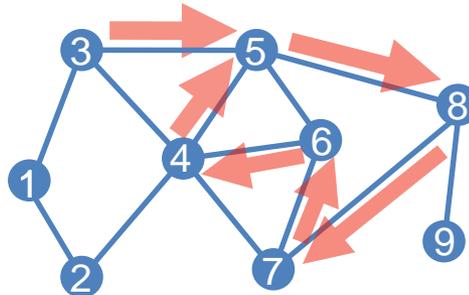


incomparable representations

EvoNRL Key Idea



Input network

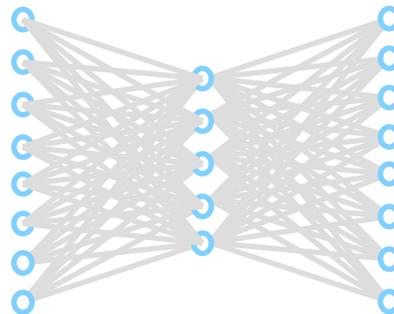


Obtain a set of random walks

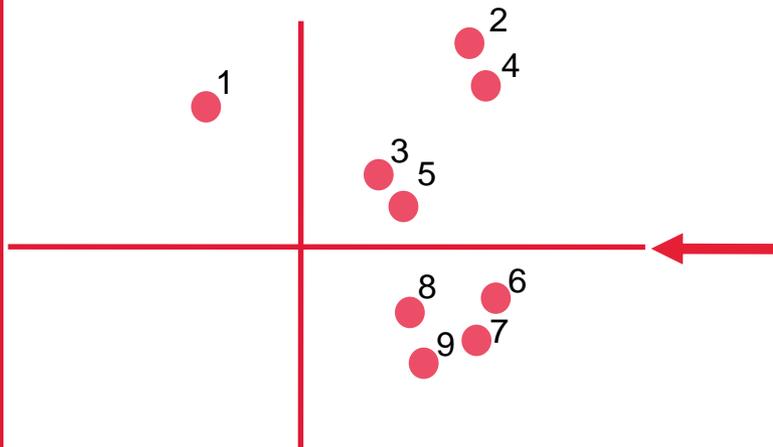


1	3 5 8 7 6 4 5
2	1 3 5 8 7 6 5
.	.
.	.
.	.
.	.
87	8 5 4 3 5 6 7
88	4 5 6 7 8 9
89	2 1 3 5 6 7 8
90	7 4 2 1 3 5 6

Treat the set of random walks as sentences



Feed sentences to Skip-gram NN model

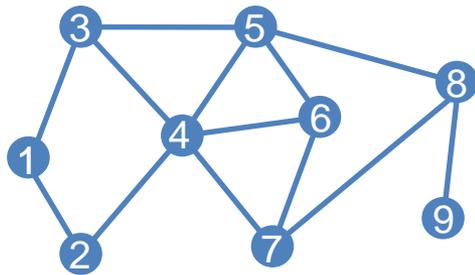


Learn a vector representation for each node

dynamically maintain a set
of random walks for every
change in the network

Example

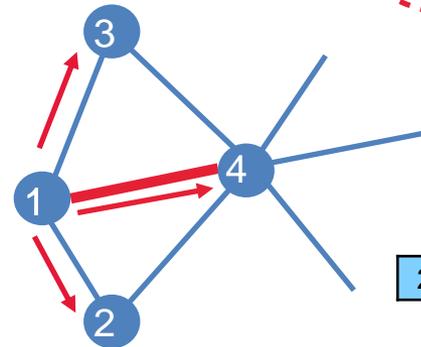
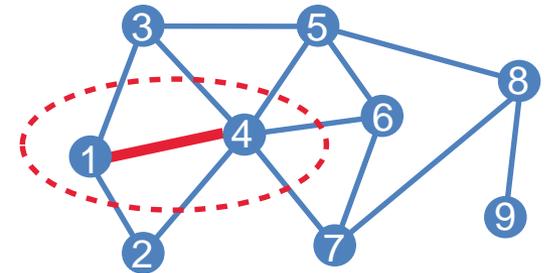
t = 0



addition of edge (1, 4)



t = 1



simulate the rest of the RW

2	1 4 3 5 6 7 8
---	---------------

1	3 5 8 7 6 4 5
2	1 3 5 8 7 6 5
.	.
.	.
.	.
.	.
87	8 5 4 3 5 6 7
88	4 5 6 7 8 9
89	2 1 3 5 6 7 8
90	7 4 2 1 3 5 6



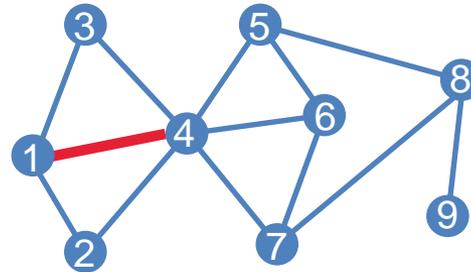
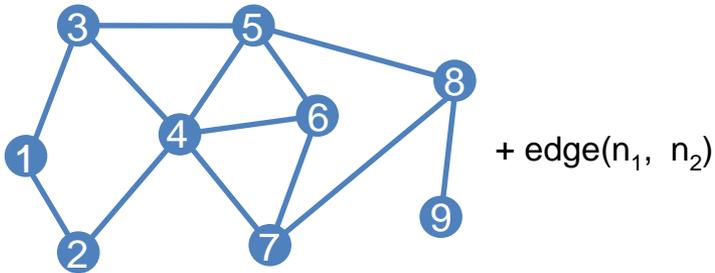
need to update the RW set



1	3 5 8 7 6 4 5
2	1 3 5 8 7 6 5
.	.
.	.
.	.
.	.
87	8 5 4 3 5 6 7
88	4 5 6 7 8 9
89	2 1 3 5 6 7 8
90	7 4 2 1 3 5 6

how can we efficiently
maintain a set of random
walks?

EvoNRL Operations



1	3 5 8 7 6 4 5
2	1 3 5 8 7 6 5
.	.
.	.
.	.
.	.
87	8 5 4 3 5 6 7
88	4 5 6 7 8 9
89	2 1 3 5 6 7 8
90	7 4 2 1 3 5 6



1	3 5 8 7 6 4 5				
2	1	3	5 8 7 6 5		
.	.				
.	.				
.	.				
.	.				
87	8 5 4 3 5 6 7				
88	4 5 6 7 8 9				
89	2	1	3	5 6 7 8	
90	7	4	2	1	3 5 6

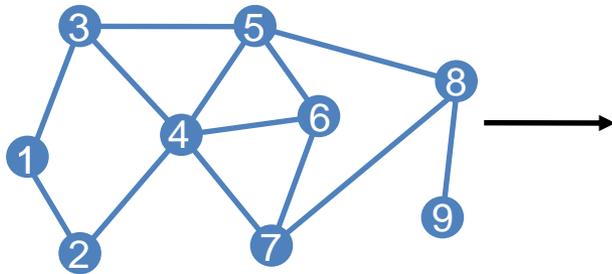
Operations on RW

Search a node

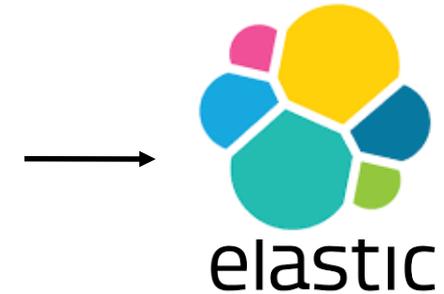
Delete a RW

Insert a new RW

EvoNRL Indexing



1	3 5 8 7 6 4 5
2	1 3 5 8 7 6 5
.	.
.	.
.	.
.	.
87	8 5 4 3 5 6 7
88	4 5 6 7 8 9
89	2 1 3 5 6 7 8
90	7 4 2 1 3 5 6



each node is a **keyword**
 each RW is a **document**
 a set of RWs is a **collection of documents**

Term	Frequency	Postings and Positions
1	3	< 2, 1 >, < 89, 2 >, < 90, 4 >
2	2	<89, 1>, <90, 3>
3	5	<1, 1>, <2, 1>, <87, 3>, <89, 3>, <90, 5>
4	4	<1, 6>, <87, 3>, <90, 2>
5	9	<1, 2>, <1, 7>, <2, 3>, <2, 7>, <87, 5>, <88, 2>, <89, 4>, <90, 6>
6	6	<1, 5>, <2, 6>, <87, 6>, <88, 3>, <89, 3>, <90, 5>
7	5	<1, 4>, <2, 5>, <87, 7>, <88, 4>, <89, 6>, 90, 7>
8	5	<1, 3>, <2, 4>, <87, 1>, <88, 6>, <89, 7>
9	1	<88, 7>

Evaluation: EvoNRL vs StaticNRL

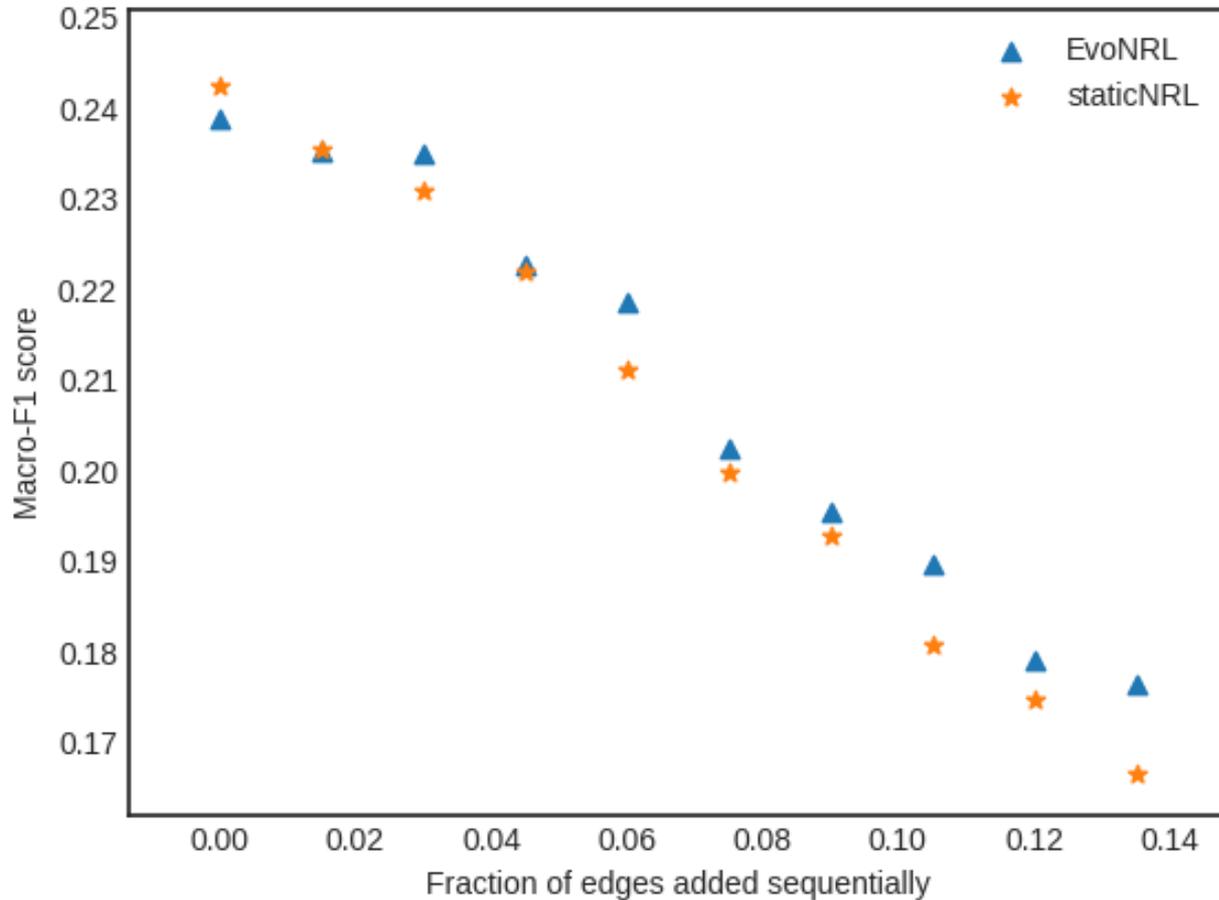
Accuracy

- EvoNRL \approx StaticNRL

Running Time

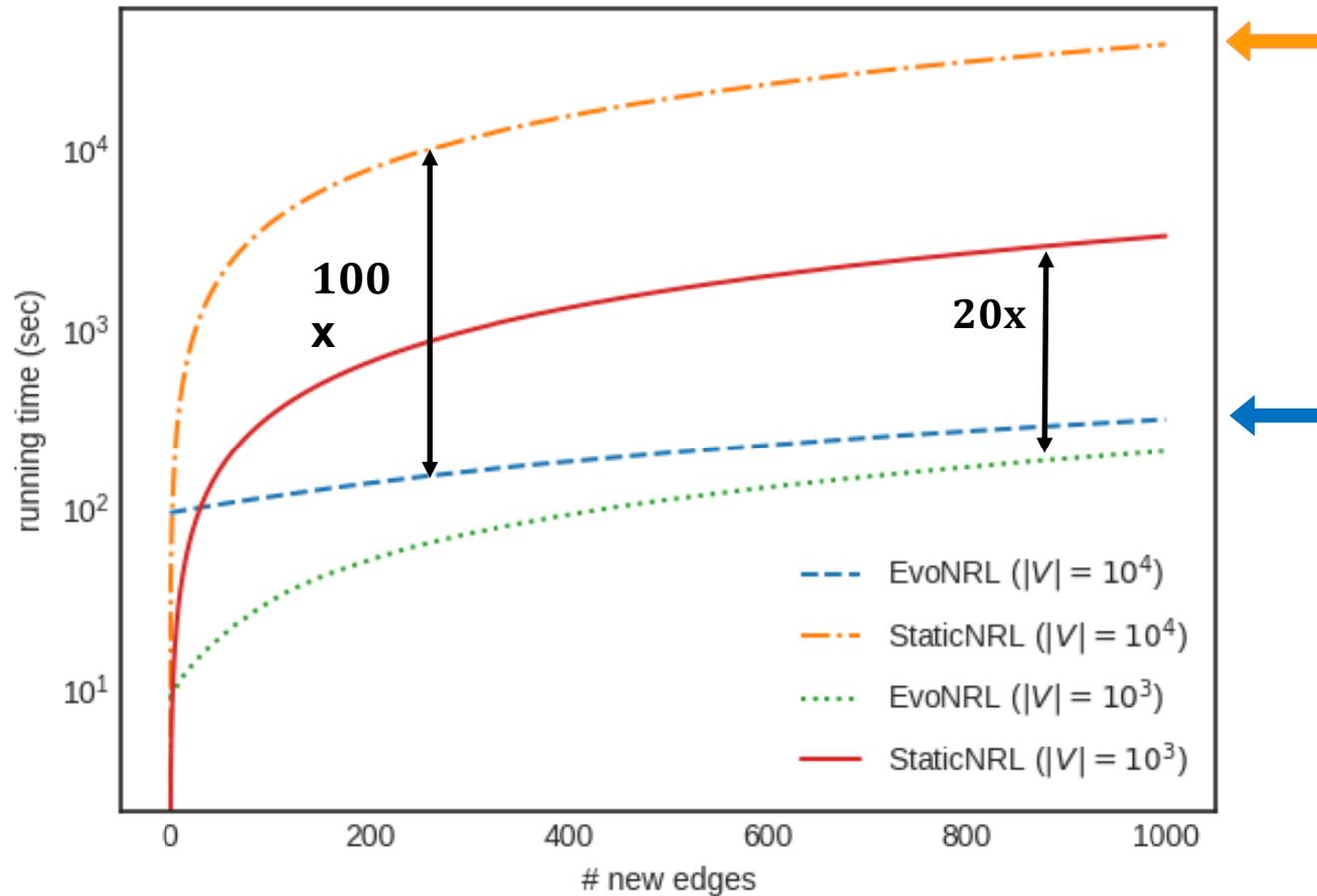
- EvoNRL \ll StaticNRL

Accuracy



EvoNRL has the **similar accuracy** as StaticNRL

Time Performance



Summary

how can we learn representations
of an evolving network?

EvoNRL

time efficient
accurate
generic method

Thank you!

Questions?

Credits



Farzaneh Heidari



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**Data Mining
Lab @ YorkU**



Mahmoud Afifi



Abdullah Abuolaim

References

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[Complex Networks 2018] EvoNRL: Evolving Network Representation Learning Based on Random Walks. Farzaneh Heidari, Manos Papagelis. Proceedings of the 7th International Conference on Complex Networks and Their Applications.