

Homework Assignment #7**Due: November 3, 2023 at 7:00 p.m.**

1. If L is a language over the alphabet Σ , then $SUPER(L)$ is the set of all superstrings of L . More formally, $SUPER(L) = \{xyz : x, z \in \Sigma^* \text{ and } y \in L\}$. Suppose there is an algorithm $DECIDE(L, w)$ that decides whether a given string w is in L . Show that $SUPER(L)$ is also decidable by giving pseudocode for an algorithm that decides $SUPER(L)$. Your pseudocode can call $DECIDE$ as a subroutine, and it can be deterministic or non-deterministic. Explain why your answer is correct.
2. If L is a language over the alphabet Σ , then $SUB(L)$ is the set of all substrings of L . More formally, $SUB(L) = \{y : \exists x, z \in \Sigma^* \text{ such that } xyz \in L\}$. Suppose there is an algorithm $RECOGNIZE(L, w)$ that recognizes L . Show that $SUB(L)$ is also recognizable by giving pseudocode for an algorithm that recognizes $SUB(L)$. Your pseudocode can call $RECOGNIZE$ as a subroutine, and it can be deterministic or non-deterministic. Explain why your answer is correct.