

# Computing for Math and Stats

## Lecture 4

# Creating Matrices

- Matrices can be created like arrays.
- We can specify all the elements explicitly arranged in rows
  - $A = [1\ 2\ 3; 4\ 5\ 6; 7\ 8\ 9]$
- We can specify them implicitly
  - $A = [1:3; 4:6; 7:9]$
  - (semicolons can be replaced by newlines, according to taste)
- We can build them up from submatrices

# Building up Matrices

- Consider the following
  - $A = [1:3; 4:6; 7:9]$
- Expression  $1:3$  looks like a row vector...
- We can put in there whatever row vector we like
  - $B = [A(3,:); A(2,:); A(1,:)]$
- We can do the same with column vectors
  - $C = [A(:,3), A(:,2), A(:,1)]$

# Building up matrices

- We can build up matrices as a series of rows separated by semicolons
- We can build up matrices as a series of columns, separated by commas
- Why not build up matrices as a series of submatrices separated by either colons or commas

# Building up Matrices

- For example
  - $C = [A, A, A]$
  - $D = [A; A; A]$
- We can carry the idea further
  - $G = [A, \text{ones}(3, 1); \text{ones}(1, 4)]$
  - $F = [\text{eye}(3), \text{ones}(3, 1); \text{ones}(1, 4)]$
  - $H = [A, A'; A', A]$

# Building up Matrices

- These techniques can be used to generate matrices
  - for testing
  - that are sparse (have many zeros)
  - that have some regularity
- These are rather powerful and very elegant techniques
  - Test them to make sure that they work the way you think they work
  - Use them with care
  - Only when they are the simplest route to solve the problem

# Accessing Matrices

- Matrices are accessed with parentheses “(“ and “)”
- This is different from most programming languages that use square brackets for array (matrix, vector) accessing
- Everything in Matlab is a matrix (kind of)
  - In old languages like lisp everything was a list

# Accessing Matrices

- Consider the following
  - $A(1:2,2:3)$
- This is a submatrix of  $A$  that comprises the first two rows and the last two columns
- Can also write
  - $A(1:2,:)$
- Saves keystrokes and confuses outsiders

# Accessing Matrices

- The expression
  - 1:2 is a row vector
- We can put in there any row vector we want
  - $A([1, 3],[3, 1])$
- It is quite flexible
- See `shuffle2x2.m`

# Adding More Elements

- Let
  - $V=[1:2:10]$
- $V(6)$  is undefined
- But
  - $V(6) = 4$  expands the size of the matrix
- $V(1,6)$  is what?
- Can we now do  $V(3,2)=12$  ?

# Deleting Elements

- We do not need this too often, but useful to have
- Let  $V=[1:10]$
- We delete an element with
- $V(3)=[ ]$

# Usefull Built-in Functions

- We know about `eye()`, `ones()`, `zeros()`
- We laso have
  - `reshape(A,m,n)` to put the elements of a into an  $m \times n$  matrix
  - `length(V)` the number of elements in vector  $V$
  - `size(M)` returns  $[m,n]$  the # of rows and # of columns of  $M$
  - `diag(V)` a diagonal matrix with the elements of  $V$  as its diagonal
  - `diag(M)` the vector of diagonal elements of  $M$
- See `playdiag.m`, `playsize.m`