

**Homework Assignment #8**  
**Due: March 27, 2023 at 7:00 p.m.**

1. Let  $A$  be a set of  $n$  positive integers  $a_1, a_2, \dots, a_n$  and let  $s$  and  $t$  be positive integers, with  $s \leq n$ . We wish to count the number of  $s$ -element subsets of  $A$  that have the property that the sum of the squares of the elements in the subset is exactly  $t$ .
  - (a) Use dynamic programming to solve this problem. (Use the usual steps: define an array and state its size, give a definition in precise English of what should be stored in each entry of your array, give a recurrence for computing the entries, say what order to compute the entries, and say which entry of the array holds the final answer.)
  - (b) What is the worst-case running time of your algorithm? How much space does it use? State your answers using  $\Theta$  notation in terms of  $n, s$  and  $t$ .