



How do we plan our holiday? We must take into account various preferences and constraints to develop a schedule. An important technique in developing such a schedule is "hypothetical" reasoning. e.g., if I fly into Kingston and drive a car to Port Antonio, I' II have to drive on the roads at night. How desirable is this? If I'm in Port Antonio and leave at 6:30am, I can arrive a Dunns river falls by 8:00am.

How do we plan our holiday?

- This kind of hypothetical reasoning involves asking
- "what state will I be in after the following sequence of events?"
- From this we can reason about what sequence of events one should try to bring about to achieve a desirable state.
- Search is a computational method for capturing a particular version of this kind of reasoning.

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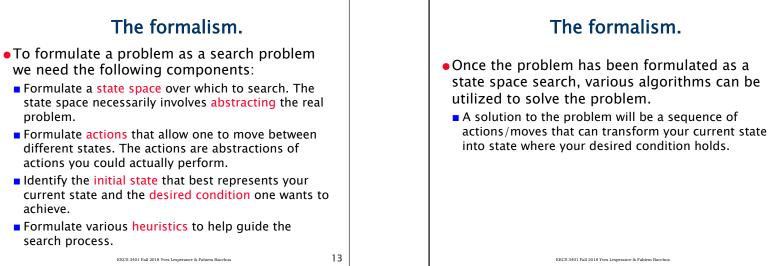
Search

- There are many difficult questions that are not resolved by search. In particular, the whole question of how does an intelligent system formulate its problem as a search problem is not addressed by search.
- Search only shows how to solve the problem once we have it correctly formulated.

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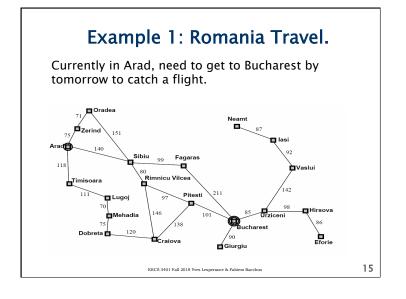
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The formalism. • Once the problem has been formulated as a

state space search, various algorithms can be utilized to solve the problem. • A solution to the problem will be a sequence of

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Example 1.

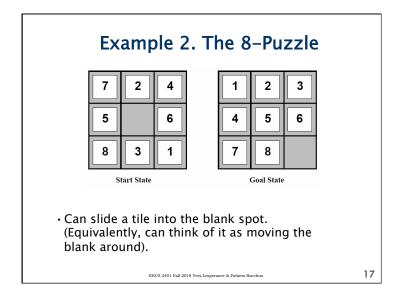
• State space.

- States: the various cities you could be located in.
 - Note we are ignoring the low level details of driving, states where you are on the road between cities, etc.
- Actions: drive between neighboring cities.
- Initial state: in Arad
- Desired condition (Goal): be in a state where you are in Bucharest. (How many states satisfy this condition?)

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• Solution will be the route, the sequence of cities to travel through to get to Bucharest.

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Example 2. The 8-Puzzle

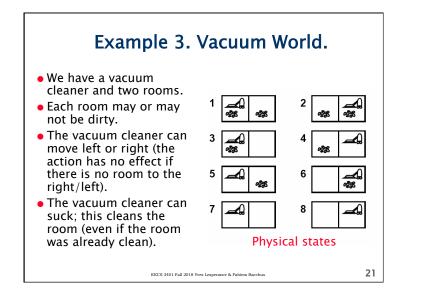
- Although there are 9! different configurations of the tiles (362,880), in fact the state space is divided into two disjoint parts.
- Only when the blank is in the middle are all four actions possible.
- Our goal condition is satisfied by only a single state. But one could easily have a goal condition like
 - The 8 is in the upper left hand corner.
 - How many different states satisfy this goal?

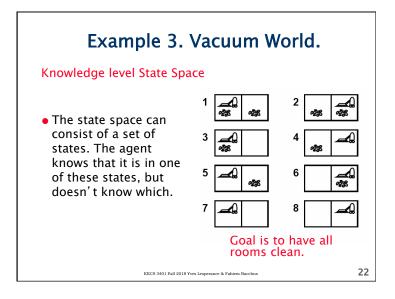
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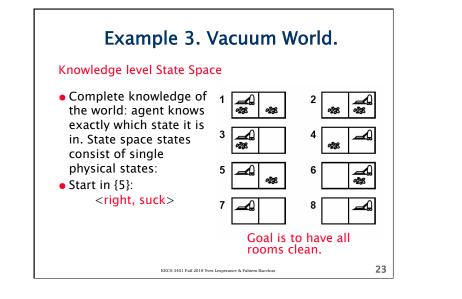
Example 3. Vacuum World.

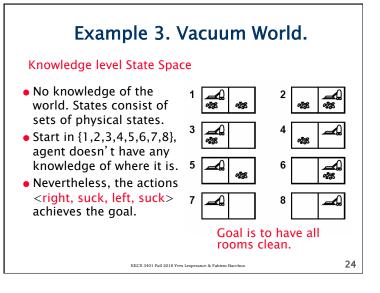
- In the previous two examples, a state in the search space corresponded to a unique state of the world (modulo details we have abstracted away).
- However, states need not map directly to world configurations. Instead, a state could map to the agent's mental conception of how the world is configured: the agent's knowledge state.

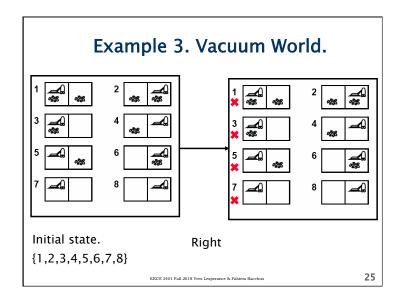
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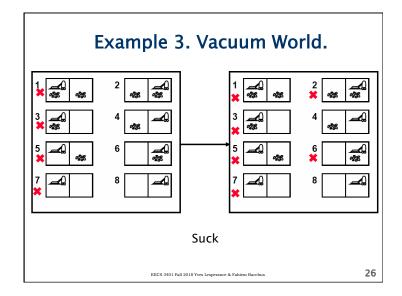


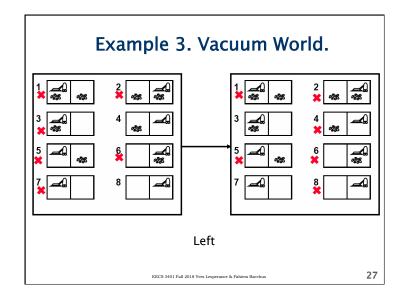


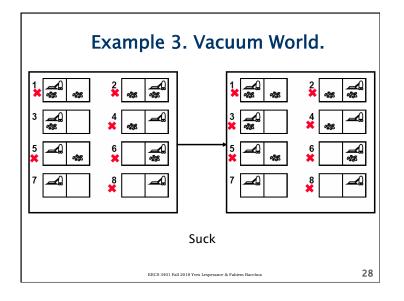














- The agent might be able to perform some sensing actions. These actions change the agent's mental state, not the world configuration.
- With sensing can search for a contingent solution: a solution that is contingent on the outcome of the sensing actions
 - right, if dirt then suck>
- Now the issue of interleaving execution and search comes into play.

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More complex situations.

- Instead of complete lack of knowledge, the agent might think that some states of the world are more likely than others.
- This leads to probabilistic models of the search space and different algorithms for solving the problem.
- Later we will see some techniques for reasoning and making decisions under uncertainty.

Algorithms for Search.

- Inputs:
 - a specified initial state (a specific world state or a set of world states representing the agent's knowledge, etc.)
 - a successor function S(x) = {set of states that can be reached from state x via a single action}.
 - a goal test a function that can be applied to a state and returns true if the state is satisfies the goal condition.
 - A step cost function C(x,a,y) which determines the cost of moving from state x to state y using action a. $(C(x,a,y) = \infty$ if a does not yield y from x)

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Algorithms for Search.

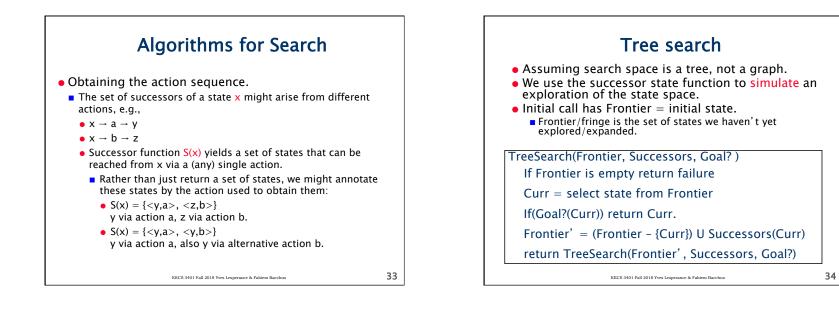
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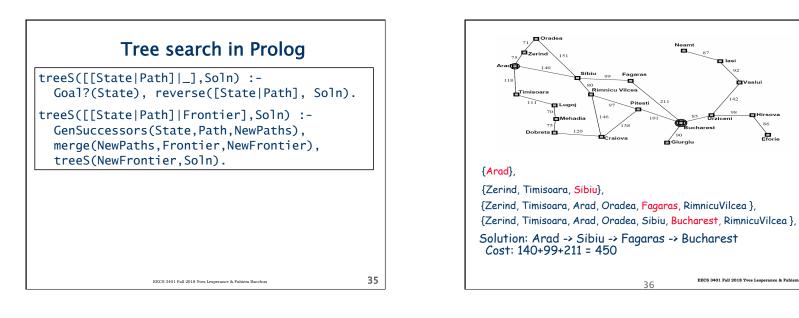
- Output:
 - a sequence of states leading from the initial state to a state satisfying the goal test.
 - The sequence might be
 - annotated by the name of the action used.

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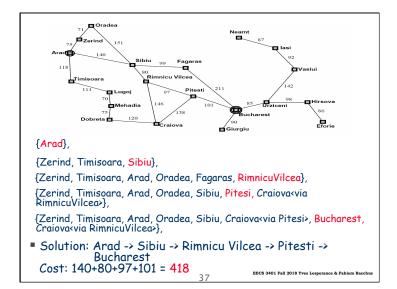
• optimal in cost for some algorithms.

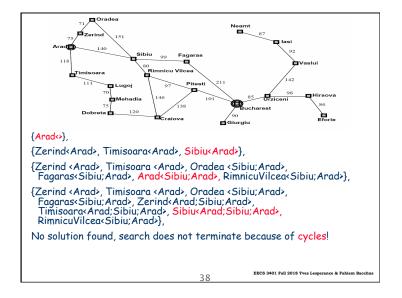
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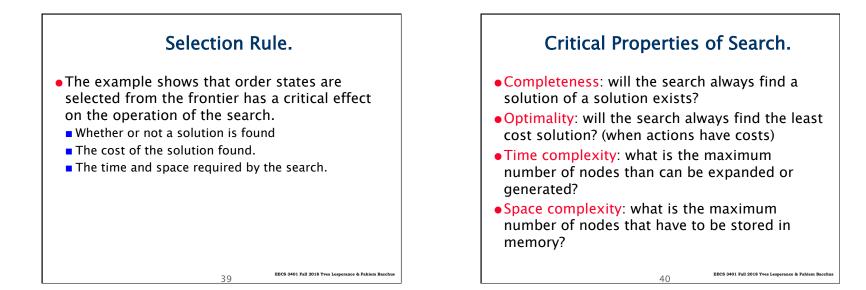


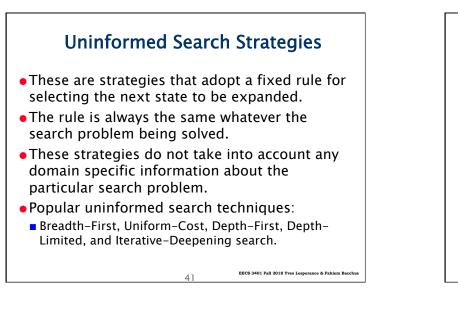


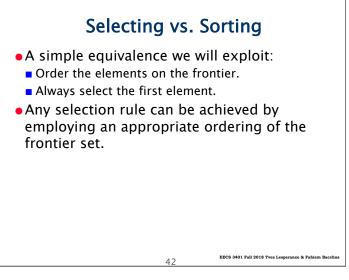
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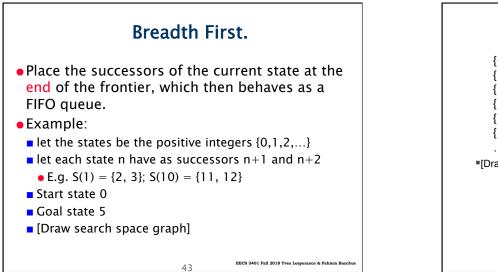


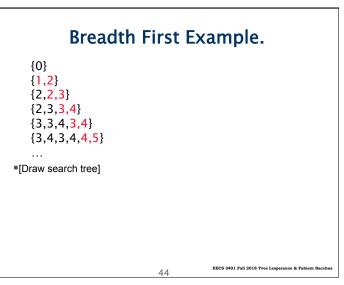


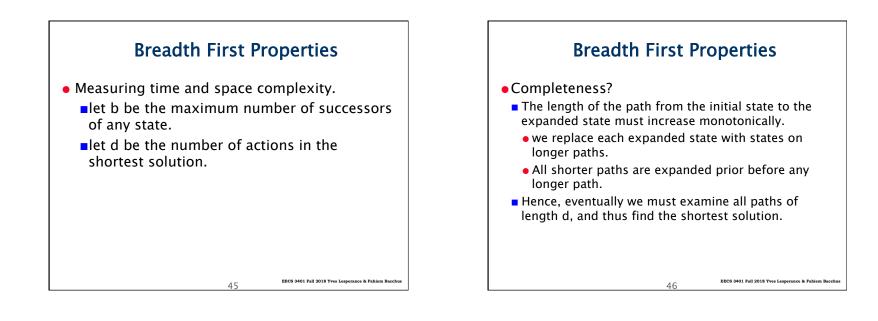


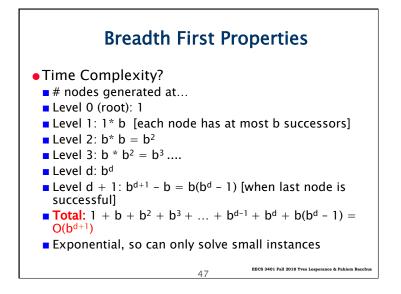


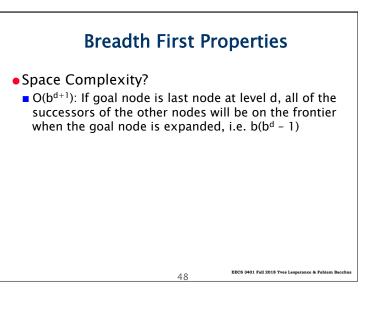


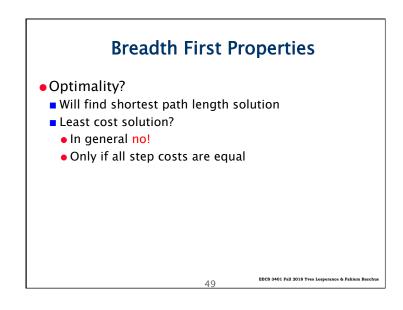












Breadth First Properties

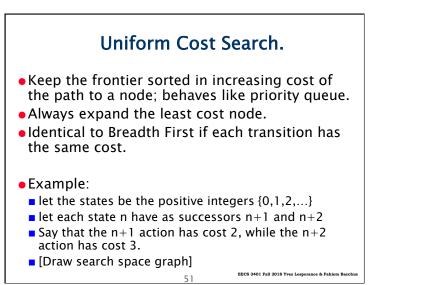
- Space complexity is a real problem.
- E.g., let b = 10, and say 1000 nodes can be expanded per second and each node requires 100 bytes of storage:

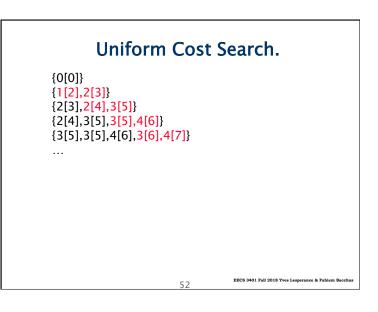
Depth	Nodes	Time	Memory
1	1	1 millisec.	100 bytes
6	10 ⁶	18 mins.	111 MB
8	10 ⁸	31 hrs.	11 GB

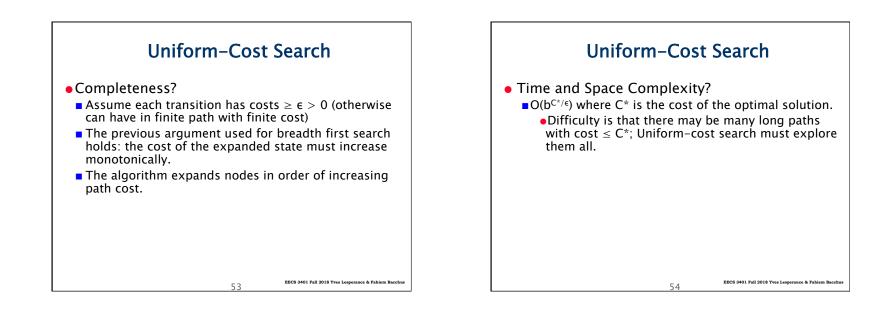
• Run out of space long before we run out of time in most applications.

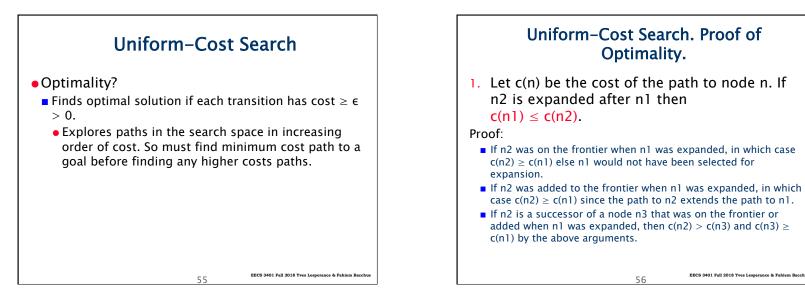
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Uniform-Cost Search. Proof of Optimality.

2. When n is expanded every path with cost strictly less than c(n) has already been expanded (i.e., every node on it has been expanded).

Proof:

- Let <Start, n0, n1, ..., nk> be a path with cost less than c(n). Let ni be the last node on this path that has been expanded. <Start, n0, n1, ni-1, ni, ni+1, ..., nk>.
- ni+1 must be on the frontier, also c(ni+1) < c(n) since the cost of the entire path to nk is < c(n).
- But then uniform-cost would have expanded ni+1 not n!
- So every node on this path must already be expanded, i.e. this path has already been expanded. QED

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Uniform-Cost Search. Proof of Optimality.

3. The first time uniform-cost expands a state, it has found the minimal cost path to it (it might later find other paths to the same state).

Proof:

- No cheaper path exists, else that path would have been expanded before.
- No cheaper path will be discovered later, as all those paths must be at least as expensive.

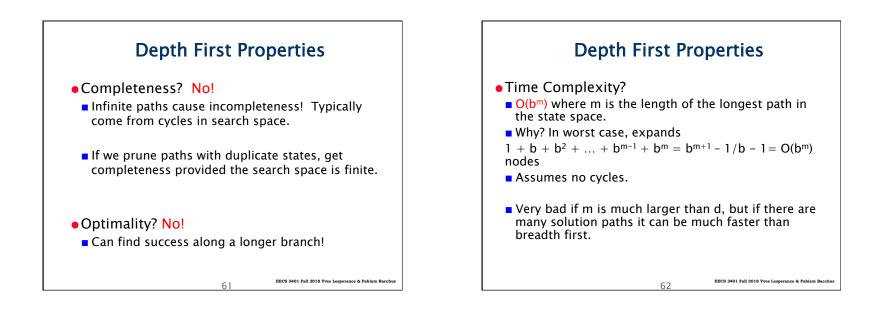
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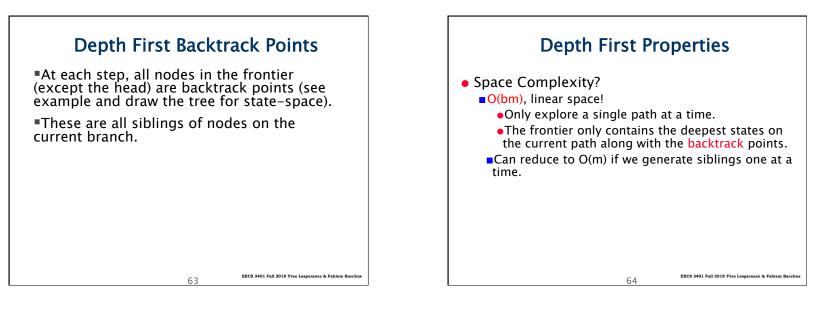
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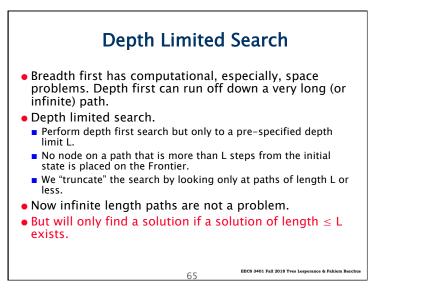
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So, when a goal state is expanded, the path to it must be optimal.

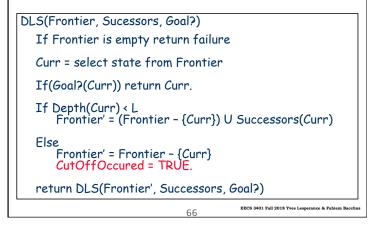
Depth First Search Depth First Search Example (applied to the example of Breadth First • Place the successors of the current state at search) the front of the frontier. {0} Frontier behaves like a stack. {**1**,**2**} {**2**,**3**,**2**} {**3,4,**3,2} **{4,5,4,3,2} {5,6,5,4,3,2}** ... [draw search tree] EECS 3401 Fall 2018 Yves Lesperance & Fahiem Ba EECS 3401 Fall 2018 Yves Lesperance & Fahie







Depth Limited Search



terative Deepening Search. • Take the idea of depth limited search one step further. • Starting at depth limit L = 0, we iteratively increase the depth limit, performing a depth limited search for each depth limit. • Stop if no solution is found, or if the depth limited search failed without cutting off any nodes because of the depth limit.

Iterative Deepening Search Example

$\{0\}$ [DL = 0]	$\{0\} [DL = 3]$ $\{1,2\}$
{0} [DL = 1] {1,2} {2}	{2,3,2} {3,4,3,2}, {4,3,2}, {3,2} {4,5,2}, {5, 2} Success!
$\{0\} [DL = 2] \\ \{1,2\} \\ \{2,3,2\}, \{3,2\}, \{2\} \\ \{3, 4\}, \{4\} \}$	
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