

declarative/logic programming

- idea: write a program that is a logical theory about some domain and then query it
- most well known instance is Prolog
- core constructs, terms and statements, are inherited from first order logic

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terms

- Prolog statements express relationships among terms
- terms are (a generalization) of the same notion in first order logic, i.e. a constant, a variable, or a function applied to some argument terms
- E.g. john, john_smith, X, Node, _person, fatherOf(paul), date(25,10,2005)
- fatherOf and date are functors; date has arity
 3; it takes 3 arguments

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terms

- variables begin with upper-case letter or _
- constants and functors (symbols) begin with lower-case
- terms denote objects
- compound terms are called structures
- E.g. course(complexity,time(Monday, 9,11),lecturer(patrick,dymond),location(LAS, 3033))
- used to represent complex data
- terms (usually) have a tree structure



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- rules are conditional statements.
- ♦ e.g. mortal(X) :- human(X). i.e. $\forall x \text{Human}(x) \rightarrow \text{Mortal}(x)$,
- daughter(X,Y) :- father(Y,X), female(X).
- ⋆, represents conjunction.
- Iikes(mary,X) :- isSweet(X).

rules ancestor(X,Y) :father(X,Z), ancestor(Z,Y). variables are universally quantified from outside; can think of variables that appear only in rule body as existentially quantified.

queries

- A guery asks whether a given statement is true, i.e. whether it follows from the program.
- ◆ e.g. ?- mortal(ulyssus). given mortal(X) :- human(X). human(ulyssus). human(penelope). god(zeus). Prolog answers Yes















denotation/meaning of Prolog programs

- a Prolog program defines a set of relations, i.e. specifies which tuples of objects/terms belong to a particular relation
- in logic, this is called a model
- declarative programming is very different from usual procedural programming where programs perform many state changing operations

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denotation of Prolog program e.g.

- fatherOf(john,paul).
 fatherOf(mary,paul).
 motherOf(john,lisa).
 parentOf(X,Y) :- fatherOf(X,Y).
 parentOf(X,Y) :- motherOf(X,Y).
- fatherOf is the relation {<john,paul>,
 <mary,paul>}

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 what is the relation associated with motherOf and parentOf?

rules as procedures

- rule has form goal :- body
- goal or head is like name of procedure
- terms on the RHS are like the body of the procedure, the sub-goals that have to be achieved to show that the goal holds
- the sub-goals will be attempted left-toright
- rule succeeds if all sub-goals succeed

passing values

- calling/querying a goal can instantiate its variables
- a sub-goal's success can bind a variable within it, also binding the same variable in the goal
- binding or instantiating a variable is giving it a value
- compare to passing values into or out of a procedure



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in Prolog, formulate statements about function values as relational facts, e.g. factorial(0,1).
 factorial(N,M):- K is N -1, factorial(K,L), M is N * L.
 to compose functions, e.g. Y = f(g(X)), you must name intermediate results

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fg(X,Y):- g(X,Z), f(Z,Y).

almost everything is syntactically a term

- Iists are terms; what is the functor?
- rules are terms: grandfather(X,Y):- father(X,Z), father(Z,Y).
 What are the functors?
- queries are terms

arithmetic functions

- Prolog retains arithmetic functions as functions (more intuitive):
 ?- X is exp(1). % exp(1) = e¹ X = 2.71828 Yes
 ?- X is (4 + 2) * 5. X = 30 Yes
- How does is compare with =, assignment?



help is sometimes helpful

?- help(reverse).

reverse(+List1, -List2) Reverse the order of the elements in List1 and unify the result with the elements of List2.

+arg: arg is input and should be instantiated.

-arg: arg is output and can be initially uninstantiated; if the query succeeds, the arg is instantiated with the "output" of the query.

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?arg: arg can be either input or output

online help ?- help(lists). No help available for lists Yes ?- apropos(lists). merge/3 Merge two sorted lists append/3 Concatenate lists "lists: List Manipulation" Section 11-1 Section 15-2-1 "lists" Yes ?- help(append/3). append(?List1, ?List2, ?List3) Succeeds when List3 unifies with the concatenation of List1 and List2. The predicate can be used with any instantiation pattern (even three variables). 27

















Prolog's query answering

• a query is a conjunction of terms answer to the query is yes if all terms succeed • A term in a query *succeeds* if * it matches a fact in the database or it matches the head of a rule whose body succeeds the substitution used to unify the term and the fact/head is applied to the rest of the query works on query terms in left to right order; databases facts/rules that match are tried in





selecting an element from a list

- To select an element from a list, can either select the first leaving the rest, or select some element from the rest and leaving the first plus the unselected elements from the rest.
- In Prolog: select(X,[X|R],R).
 select(X,[Y|R],[Y|RS]):- select(X,R,RS).





reverse

 Tail recursive definition: reverse(L,RL):- reverse(L,[],RL). reverse([],Acc,Acc). reverse([F|R],Acc,RL):reverse(R,[F|Acc],RL).
 recursive call is last thing done
 can avoid saving calls on stack















predicates for defining constraints

- "just to the left of"? "lives next to"?
- define sublist2(S,L)
 sublist2([S1, S2], [S1, S2 | _]).
 sublist2(S, [_ | T]) :- sublist2(S, T).
- define nextto predicate
 nextto(H1, H2, L) :- sublist2([H1, H2], L).
 nextto(H1, H2 ,L) :- sublist2([H2, H1], L).







how Prolog finds solution

After first 8 constraints:

List = [house(red, englishman, snail, _G251, old_gold), house(green, spaniard, dog, coffee, _G264), house(ivory, ukrainian, _G274, tea, _G276), house(green, _G285, _G286, _G287, _G288), house(yellow, _G297, _G298, _G299, kools)]

bow Prolog solves the puzzle Then need to satisfy "the owner of the third house drinks milk", i.e. List = [_, _, house(_, _, _ milk, _), _], Can't be done with current instantiation of List. So Prolog will backtrack and find another.

how Prolog solves the puzzle

The unique complete solution is L = [house(yellow, norwegian, fox, water, kools), house(blue, ukrainian, horse, tea, chesterfields), house(lower, englishman, snail, milk, old_gold), house(ivory, spaniard, dog, orange, lucky_strike), house(green, japanese, zebra, coffee, parliaments)] See course web page for code of the example.