

# node2vec: Scalable Feature Learning for Networks

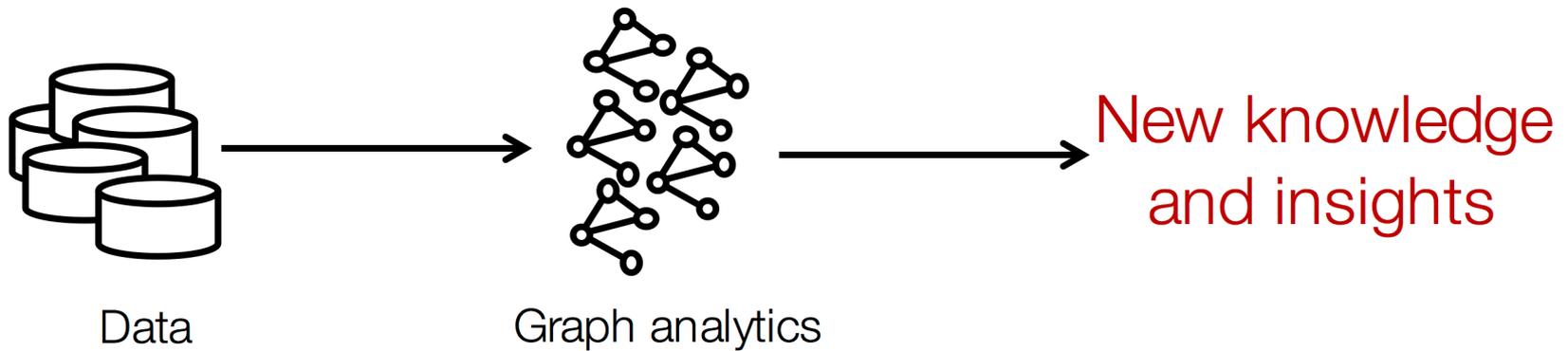
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# Outline

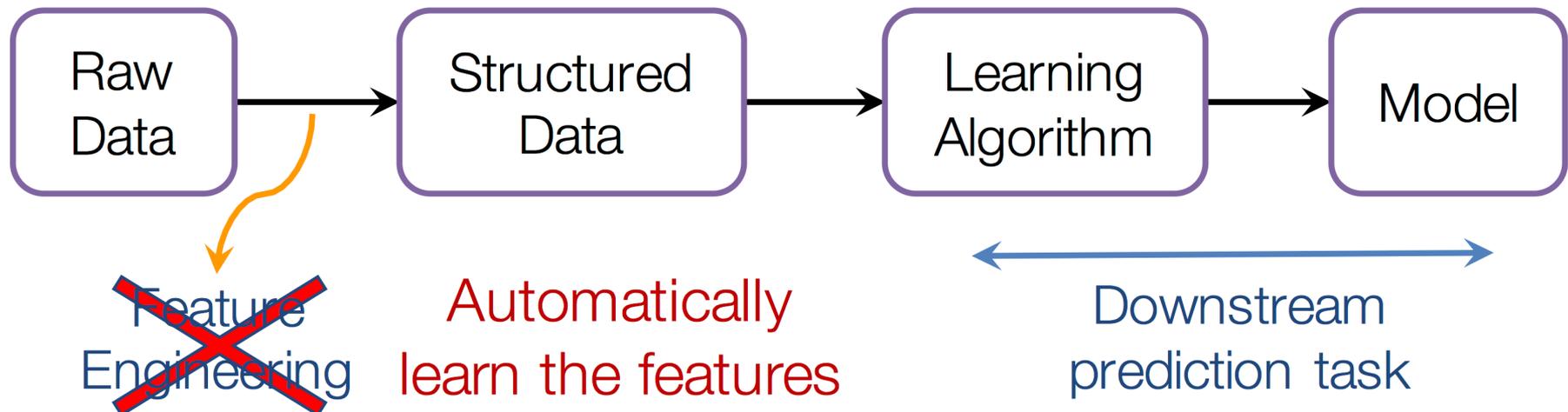
- word2vec (Background)
- Random Walk (Background)
- node2vec
- Evaluation Results
- Deficiencies

# End-to-End Graph Analytics



# Machine Learning Lifecycle

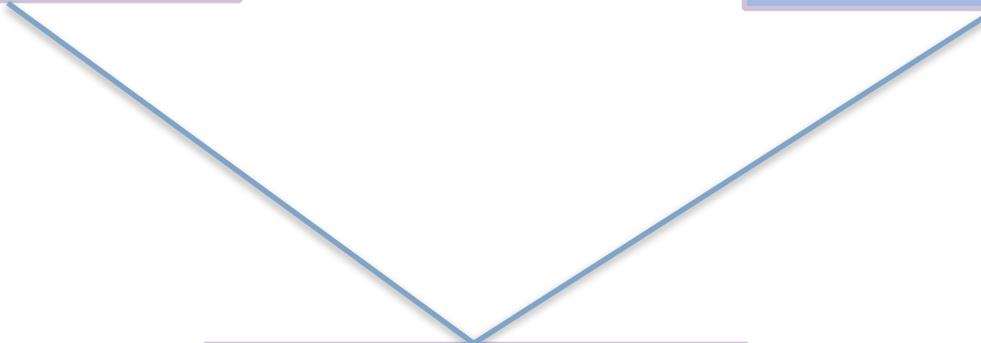
- (Supervised) Machine Learning Lifecycle: This feature, that feature.  
Every single time!



Random  
Walk

word2vec

node2vec



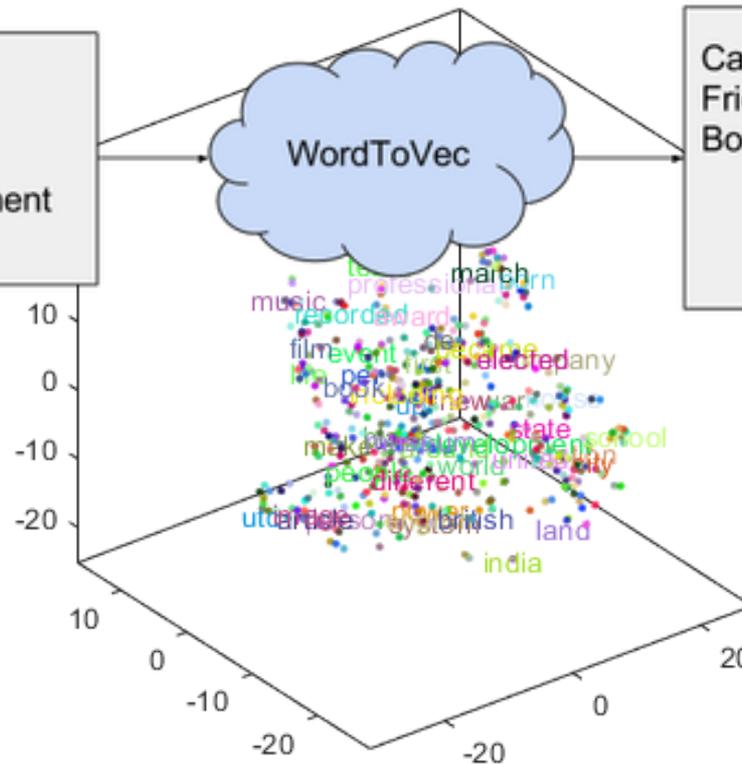
# word2vec

Input

Cat Fridays are the best  
Cats in boxes  
Cats on heads  
In every small compartment  
Entangled in threads

Output

Cats	0.434	0.239	0.123	0.934
Fridays	0.126	0.996	0.453	0.124
Boxes	0.924	0.534	0.195	0.845
	.	.	.	.



# word2vec's backbone

$$J(\theta) = \frac{1}{T} \sum_{t=1}^T \sum_{-m \leq j \leq m, j \neq 0} \log p(w_{t+j} | w_t)$$

$$p(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w=1}^W \exp(u_w^T v_c)}$$

# Window in Graph

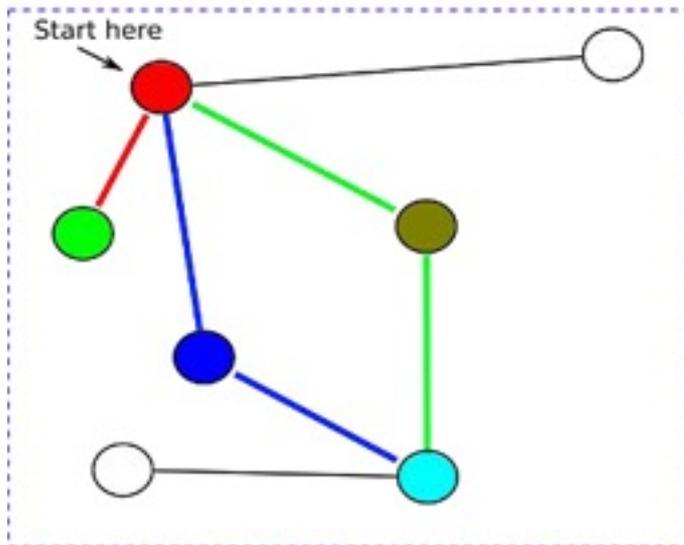


# Random Walk

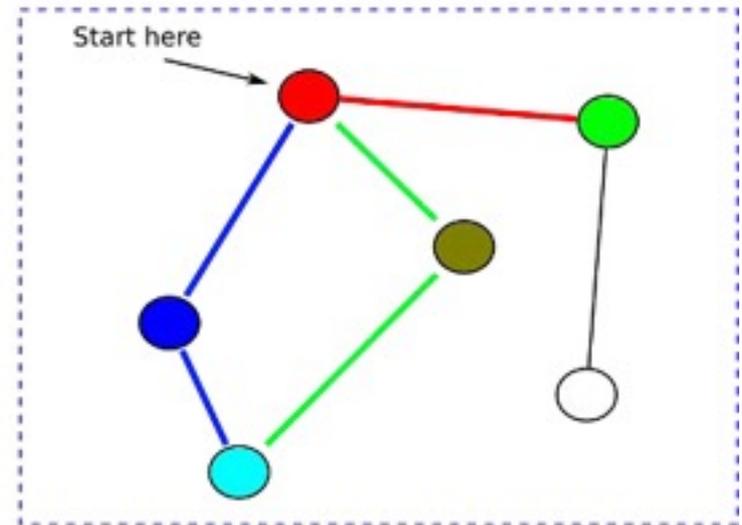
Stochastic Process

Path of random steps

Graph 1



Graph 2



# Feature Learning in Graphs

**Goal:** Learn features for a set of objects

Feature learning in graphs:

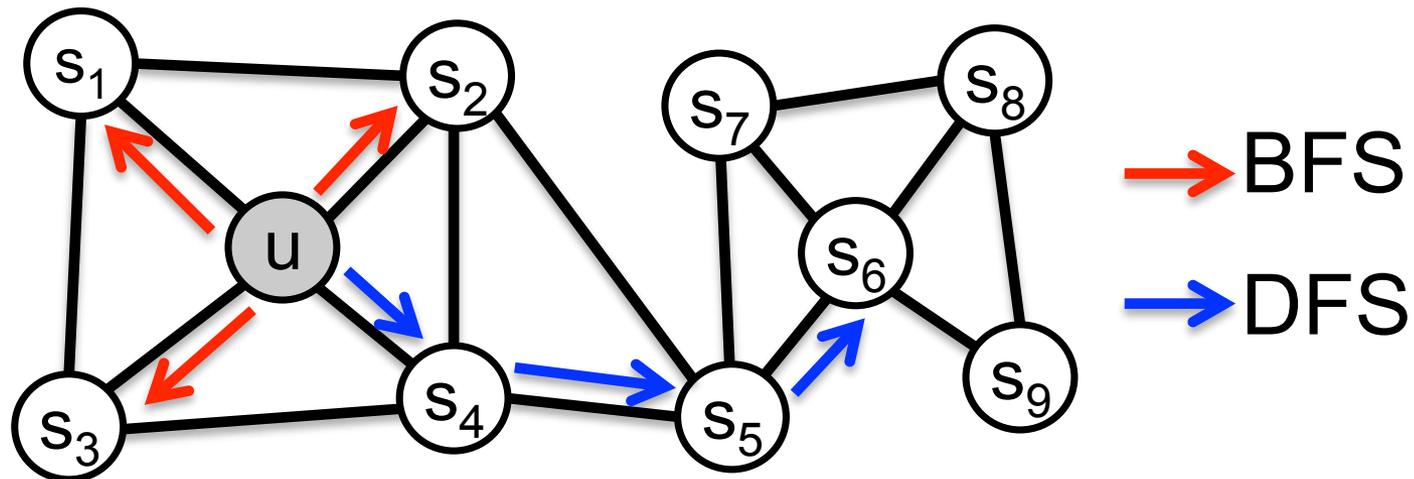
- Given:  $G = (V, E)$
- Learn a function:  $f : V \rightarrow \mathbb{R}^d$ 
  - **Not task specific:** Just given a graph, learn  $f$ . Can use the features for any downstream task!

# Unsupervised Feature Learning

- **Intuition:** Find a mapping of nodes to  $d$ -dimensions that preserves some sort of node similarity
- **Idea:** Learn node embedding such that nearby nodes are close together
- Given a node  $u$ , how do we define nearby nodes?
  - $N_S(u)$  ... neighbourhood of  $u$  obtained by sampling strategy  $S$

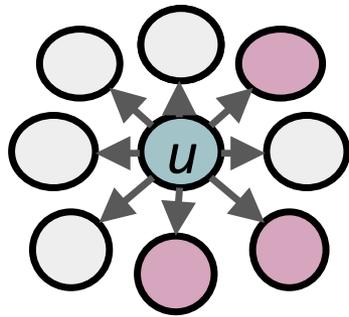
# How to determine $N_S(u)$

Two classic search strategies to define a neighborhood of a given node:



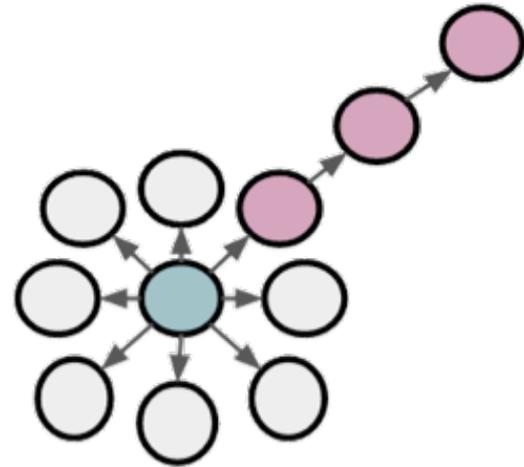
for  $|N_S(u)| = 3$

# BFS vs. DFS



**BFS:**

Micro-view of  
neighbourhood



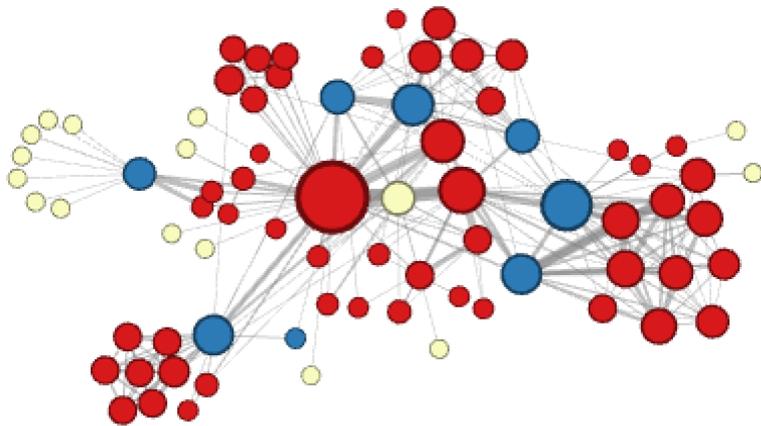
**DFS:**

Macro-view of  
neighbourhood

**Structural vs. Homophilic equivalence**

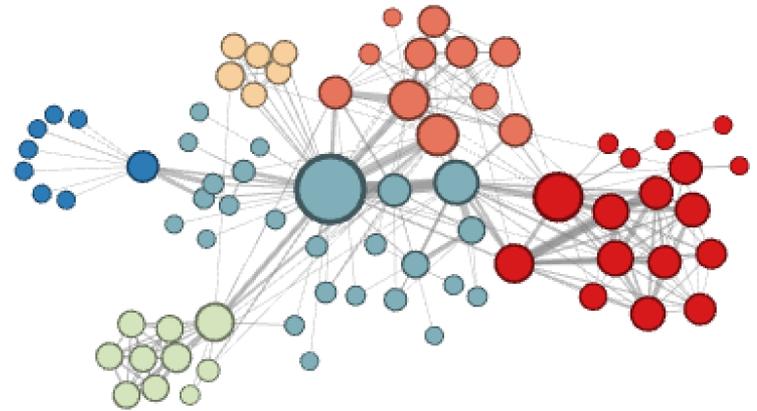
# BFS vs. DFS

## Structural vs. Homophilic equivalence



**BFS-based:**

Structural equivalence  
(structural roles)

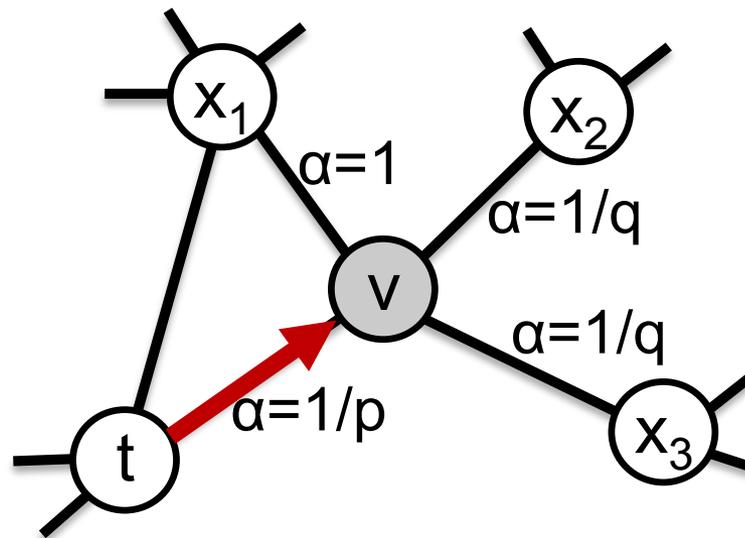


**DFS-based:**

Homophily  
(network communities)

# Interpolating BFS and DFS

- Biased random walk procedure, that given a node  $u$  samples  $N_S(u)$



The walk just traversed  $(t, v)$  and aims to make a next step.

# Multilabel Classification

Algorithm	Dataset		
	BlogCatalog	PPI	Wikipedia
Spectral Clustering	0.0405	0.0681	0.0395
DeepWalk	0.2110	0.1768	0.1274
LINE	0.0784	0.1447	0.1164
<i>node2vec</i>	<b>0.2581</b>	<b>0.1791</b>	<b>0.1552</b>
<i>node2vec</i> settings (p,q)	0.25, 0.25	4, 1	4, 0.5
<b>Gain of <i>node2vec</i> [%]</b>	<b>22.3</b>	<b>1.3</b>	<b>21.8</b>

- Spectral embedding
- DeepWalk [B. Perozzi et al., KDD '14]
- LINE [J. Tang et al., WWW '15]

# Trade-offs

task-specific heuristics  
inefficient usage of statistics

Thank you