

P.2-1 Given three vectors **A**, **B**, and **C** as follows,

$$\mathbf{A} = a_x + a_y 2 - a_z 3,$$

$$\mathbf{B} = -a_y 4 + a_z,$$

$$\mathbf{C} = a_x 5 - a_z 2,$$

find

a) a_A

c) $\mathbf{A} \cdot \mathbf{B}$

e) the component of **A** in the direction of **C**

g) $\mathbf{A} \cdot (\mathbf{B} \times \mathbf{C})$ and $(\mathbf{A} \times \mathbf{B}) \cdot \mathbf{C}$

b) $|\mathbf{A} - \mathbf{B}|$

d) θ_{AB}

f) $\mathbf{A} \times \mathbf{C}$

h) $(\mathbf{A} \times \mathbf{B}) \times \mathbf{C}$ and $\mathbf{A} \times (\mathbf{B} \times \mathbf{C})$

P.2-2 Given

$$\mathbf{A} = a_x - a_y 2 + a_z 3,$$

$$\mathbf{B} = a_x + a_y - a_z 2,$$

find the expression for a unit vector **C** that is perpendicular to both **A** and **B**.

P.2-16 The position of a point in cylindrical coordinates is specified by $(4, 2\pi/3, 3)$. What is the location of the point

a) in Cartesian coordinates?

b) in spherical coordinates?

P.2-21 Given a vector function $\mathbf{E} = a_x y + a_y x$, evaluate the scalar line integral $\int \mathbf{E} \cdot d\ell$ from $P_1(2, 1, -1)$ to $P_2(8, 2, -1)$

a) along the parabola $x = 2y^2$,

b) along the straight line joining the two points.

P.2-23 Given a scalar function

$$V = \left(\sin \frac{\pi}{2} x \right) \left(\sin \frac{\pi}{3} y \right) e^{-z},$$

determine

a) the magnitude and the direction of the maximum rate of increase of V at the point $P(1, 2, 3)$,

b) the rate of increase of V at P in the direction of the origin.

P.2-25 The equation in space of a plane containing the point (x_1, y_1, z_1) can be written as

$$\ell(x - x_1) + m(y - y_1) + p(z - z_1) = 0,$$

where ℓ , m , and p are direction cosines of a unit normal to the plane:

$$\mathbf{a}_n = a_x \ell + a_y m + a_z p.$$

Given a vector field $\mathbf{F} = a_x + a_y 2 + a_z 3$, evaluate the integral $\int_S \mathbf{F} \cdot d\mathbf{s}$ over the square plane surface whose corners are at $(0, 0, 2)$, $(2, 0, 2)$, $(2, 2, 0)$, and $(0, 2, 0)$.