Sequences

- Finite or infinite
- Calculus limits of infinite sequences (proving existence, evaluation...)
- E.g.
 - Arithmetic progression (series)

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1, 4, 7, 10, ...
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Geometric progression (series)

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3, 6, 12, 24, 48 ...
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Similarity with series

- $S = a_1 + a_2 + a_3 + a_4 + \dots$ (n terms)
- Consider the sequence

$$S_1$$
, S_2 , S_3 , ... S_n , where

$$S_i = a_1 + a_2 + ... + a_i$$

In general we would like to evaluate sums of series – useful in algorithm analysis.

e.g. what is the total time spent in a nested loop?

Sums of common series

Arithmetic series

e.g. 1 + 2 + ... + n (occurs in the analysis of running time of simple for loops)

general form
$$\Sigma_i t_i$$
, t_i = a + ib

Geometric series

e.g.
$$1 + 2 + 2^2 + 2^3 + ... + 2^n$$

general form $\Sigma_i t_i$, t_i = ar^i

More general series (not either of the above)

$$1^2 + 2^2 + 3^2 + 4^2 + ... + n^2$$

Sums of common series - 2

Technique for summing arithmetic series

Technique for summing geometric series

More general series – more difficult

Caveats

- Need to be very careful with infinite series
- In general, tools from calculus are needed to know whether an infinite series sum exists.
- There are instances where the infinite series sum is much easier to compute and manipulate, e.g. geometric series with r < 1.