

**Math/CSE 1028:**  
**Discrete Mathematics for Engineers**  
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**Suprakash Datta**

[datta@cse.yorku.ca](mailto:datta@cse.yorku.ca)

Office: CSEB 3043

Phone: 416-736-2100 ext 77875

Course page: <http://www.cse.yorku.ca/course/1028>

## 6.5 Permutations with Repetition

- Thm 1: The number of  $r$ -permutations of a set with  $n$  objects with repetitions allowed is  $n^r$
- Thm 2: There are  $C(n+r-1, n-1)$   $r$ -combinations from a set with  $n$  elements when repetition is allowed.

# Permutations with Identical Objects

Thm 3 (page 428)

- Reasoning 1: Assume distinguishable and then divide by number of times the same arrangement is counted
- Reasoning 2: Choose places for the indistinguishable objects and then they can be arranged in only one way.

# Distinguishable Objects into Distinguishable Boxes

Thm 4 (page 429)

- Reasoning: Choose elements for the first box, then the second box, and so on and use the product rule.
- Reasoning 2: Map this to permutation with identical objects.

# Indistinguishable Objects into Distinguishable Boxes

- $r$  indistinguishable objects can be placed in  $n$  distinguishable boxes in  $C(n+r-1, r-1)$  ways
- The case of indistinguishable boxes is much harder and is omitted (pp 430-431)