

Abstract Data Types Documentation

Documentation

- Users are only interested in the properties of the ADT
- Programmers and designers require all the information which a user needs AND all information pertaining to the design and implementation
- Useful to think of the documentation as being an annotated definition of an abstract data type

Documentation Table of Contents

- Cover page, table of contents and abstract
- Document introduction
 - » **Informal overview of the facilities provided. Help readers determine if this is what they need**
- Data type objects
 - » **Description of all the objects – include diagrams**
 - » **Split into**
 - > **Imported – which predefined objects are used**
 - > **Exported – for others to use**
 - > **Hidden – used in the implementation**

Operations TOC – 2

- Operations
 - » **Give**
 - > **Signature**
 - > **Informal description**
 - > **pre- and post- conditions**
 - » **Use natural language, mathematics, diagrams – whatever best gets the meaning across.**
 - » **Be simple, complete, clear, precise, concise as possible**

Operations TOC – 3

- Example – partial axiomatic description of bank accounts
 - » **The operation signatures only – no pre- post- given**

new : [] -> **account**

- Create an account with a zero balance

withdraw : **account X amount** -> **account**

- Remove amount from account

deposit : **account X amount** -> **account**

- Add amount to account

balance : **account** -> **amount**

- What is the amount in the account?

Operations TOC – 4

- Operation interaction
 - » **Previous section describes operations in isolation**
 - » **Provide better understanding by showing properties when operations are used in combination**
 - » **Common descriptive method in use is axiomatic**
 - > **List of axioms or statements which must be true if the ADT is implemented and used correctly**

Operations TOC – 5

- Axioms about the data type
 - » **Axiom 1: New account has a balance of zero dollars**
 $\text{balance}(\text{new}) = 0$
 - » **Axiom 2: Cannot withdraw from a new account**
 $\text{withdraw}(\text{new}, \text{amt}) = \text{error}$
 - » **Axiom 3: Deposit amt and then withdraw amt with no intervening operations the balance does not change**
 $\text{balance}(\text{withdraw}(\text{deposit}(\text{acct}, \text{amt}), \text{amt})) = \text{balance}(\text{acct})$
 - » **Axiom 4: Only withdraw if the balance is \geq the amount to withdraw. The amount is deducted from the balance**
 $\text{balance}(\text{acct}) < \text{amt} \rightarrow \text{withdraw}(\text{acct}, \text{amt}) = \text{error}$
 $\text{balance}(\text{acct}) \geq \text{amt} \rightarrow$
 $\text{balance}(\text{withdraw}(\text{acct}, \text{amt})) = \text{balance}(\text{acct}) - \text{amt}$

TOC – 6

- How to use the ADT
 - » **Tutorial guide on use. Dwell on nuances. Describe various examples**
- Dictionary
 - » **Define new terminology or domain specific jargon that implementers or users may not know**
- Undesired Event Dictionary
 - » **Description of possible errors which can occur**
 - » **Contains warnings**
 - » **How to recognize error situations**
 - » **How to recover from error situations**
 - » **What to do if recovery is impossible**

TOC – 7

- ADT generation parameters
 - » **Describe how instances and variations can be implemented from this generic data type**
 - > **How to change base types**
 - > **How to change amount of storage for a customer name**
 - » **Describe changes that can be made that will not violate assumptions and specifications. Design for a class of similar data types**
 - » **State what programming tools can be used to modify the implementation**

TOC – 8

- Design issues
 - » **What were the design choices and why were the actual choices chosen. Help guide future changes to keep in the spirit of the original**
 - > **Why was fixed memory allocation used instead of dynamic?**
 - > **Why were size limits imposed?**
 - > **Why was a particular data structure chosen?**

TOC – 9

- Implementation notes
 - » **Designer may have information of use to the implementer. Know properties that can improve implementation**
- List of assumptions – those assumptions that
 - » **Cannot be violated**
 - » **Not implicit in the context**
 - » **Global**
 - » **Note: cannot state all assumptions so state those that**
 - > **Are most important**
 - > **Most likely to cause problems if violated**
 - > **Are not easily detected as causing problems until a long time later**

TOC – 10

- Normal use assumptions
 - » **Information available from the ADT**
 - » **Information that must be supplied to the ADT**
 - » **Events reported by the ADT**
 - » **Tasks that can be performed by the ADT**
 - » **Operating states of the ADT and how they affect the Information obtained from and supplied to the ADT**
 - » **Failure states of the ADT and how they affect the information obtained from and supplied to the ADT**

TOC – 11

- Incorrect use assumptions
 - » **Associated with run time undesired events**
 - » **What may or may not happen if the production version has undesired event handling code removed to speed up the system**
- Program source text
 - » **If the source test is small may be included with the description of the operations**
- Facilities index
 - » **A quick look up reference of all programs, modules, operations, objects and terms defined**

Minimal Documentation

- Objects

- » **Types**

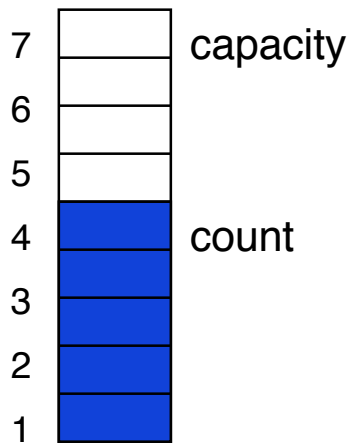
Diagrams where possible

- Example – stack

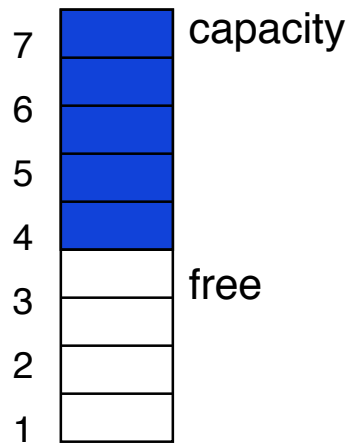
- » **Imported – none**

- » **Exported – STACK [G]**

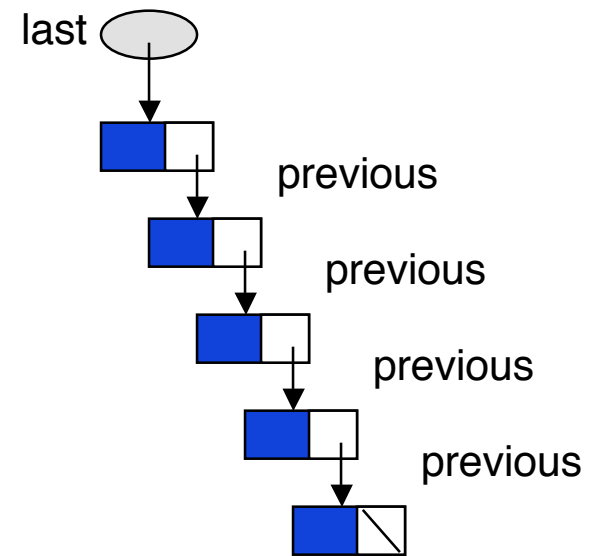
- » **Hidden – implementation**



Array up



Array down



Linked list

Minimal Documentation – 2

- Operations – example for a stack

- » **Signatures, pre & post conditions**

- > **push : STACK [G] x G → STACK [G]**

- **require** true
 - ensure** result = x ^ s & count = old count + 1

- > **pop : STACK [G] → STACK [G]**

- **require** not empty (s)
 - ensure** result = s' & count = old count - 1

- > **top : STACK [G] → G**

- **require** not empty (s)
 - ensure** result = s₁

Minimal Documentation – 3

- Operations – example for a stack cont'd

> **empty** : **STACK [G]** → **BOOLEAN**

– **require** true
– **ensure** result = (count = 0)

> **new** : [] → **STACK [G]**

– **require** true
– **ensure** result = **STACK [G]** & count = 0

- » **Note: often "require true" is not written but is assumed**
- » **It is better to write it as then one can wonder if it was left out by accident**
- > **"nothing" is often represented with a special symbol.
e.g. nil , λ , ε , Δ**

Minimal Documentation – 4

- Operations – example for a stack cont'd

» **axioms**

> $\forall x : G, s : \text{STACK} [G] \cdot$
 $\text{top} (\text{push} (s, x)) = x$
 $\wedge \text{pop} (\text{push} (s, x)) = s$
 $\wedge \text{empty} (\text{new})$
 $\wedge \sim \text{empty} (\text{push} (s, x))$

- is read as
"it is the case that"

» **Alternately can use natural language**

> forall $x : G, s : \text{STACK} [G] ::$
 $\text{top} (\text{push} (s, x)) = x$
 and $\text{pop} (\text{push} (s, x)) = s$
 and $\text{empty} (\text{new})$
 and not $\text{empty} (\text{push} (s, x))$

ADT Invariants

- Conditions that must be true after the execution of any method in the the class
- The conditions that hold, at all times, among the objects in an instance of the ADT
 - » **More on this when we discuss design by contract**

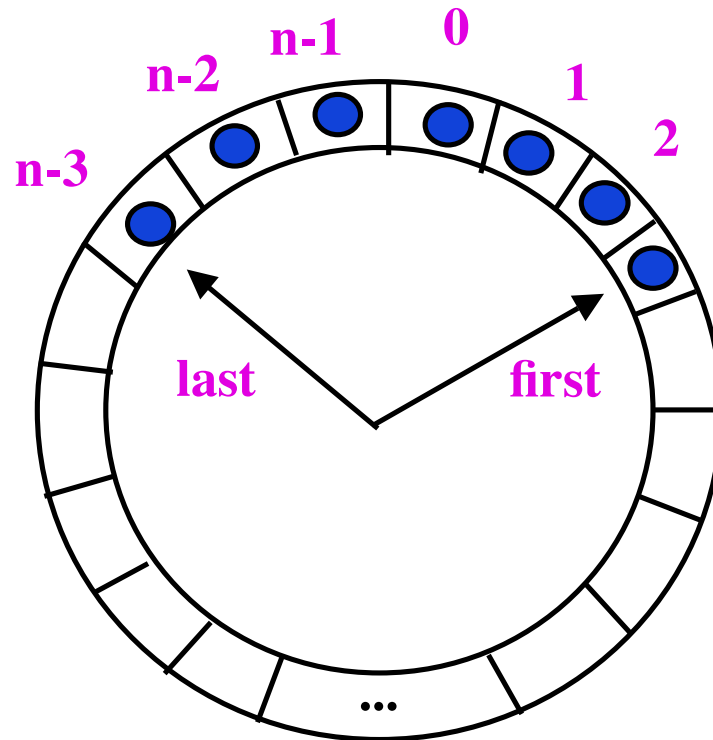
Example Circular Queue

isEmpty → $\text{length} = 0$ & $(\text{last}-1) \bmod \text{Size} = \text{first}$

isFull → $\text{length} = \text{Size} - 1$

not isFull → $\text{length} = (\text{Size} + \text{first} - \text{last} + 1) \bmod \text{Size}$

last is the last
Item to remove



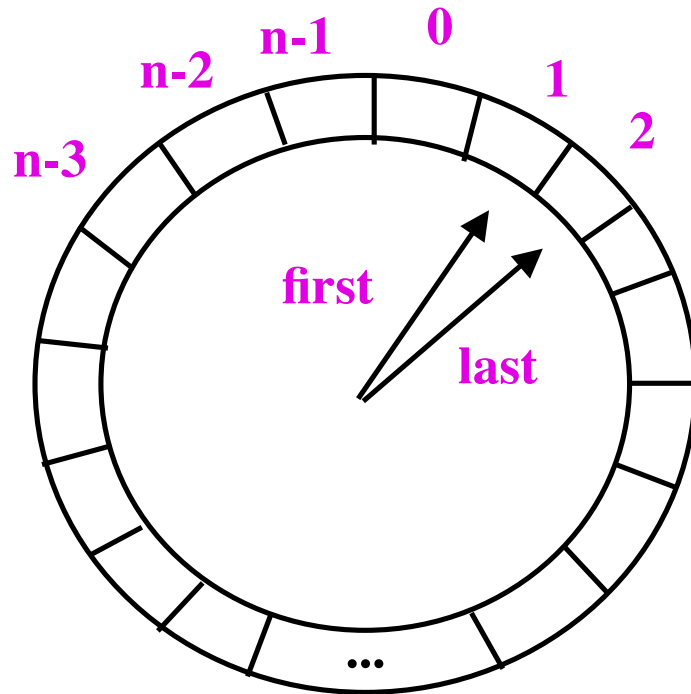
first is the first
Item to remove

Empty Circular Queue

isEmpty → **length = 0** & **(last-1) mod Size = first**

isFull → **length = Size - 1**

not isFull → **length = (Size + first - last + 1) mod Size**



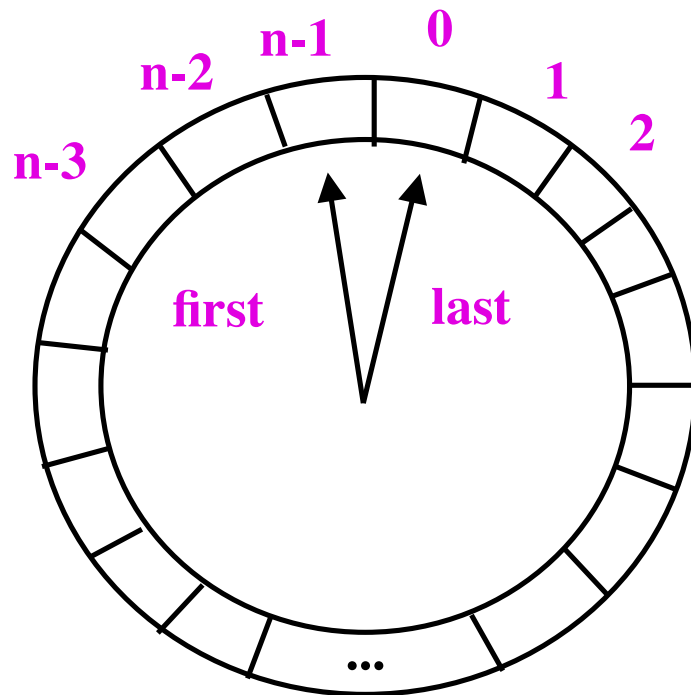
$$\begin{aligned} \text{length} &= (n + 1 - 2 + 1) \bmod n \\ &= (n + 0) \bmod n \\ &= 0 \end{aligned}$$

Empty Circular Queue – 2

isEmpty → length = 0 & (last-1) mod Size = first

isFull → length = Size - 1

not isFull → length = (Size + first - last + 1) mod Size



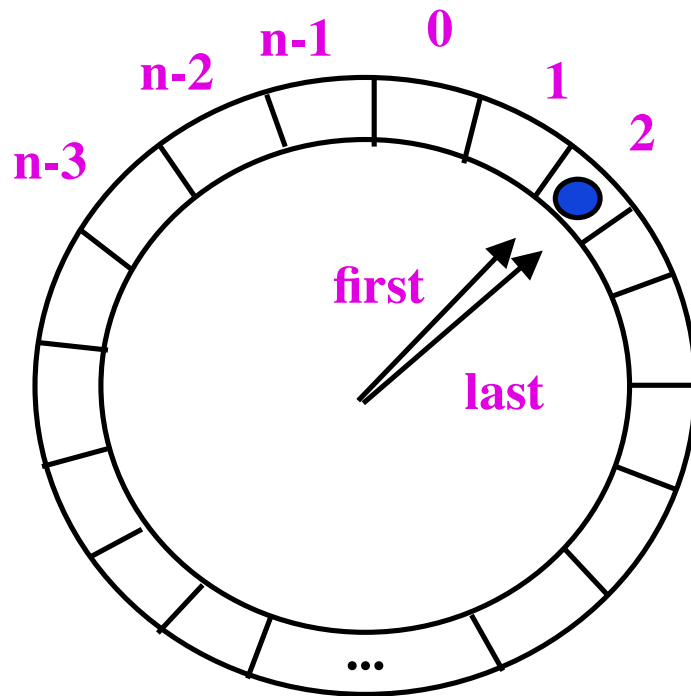
$$\begin{aligned} \text{length} &= (n + (n-1) - 0 + 1) \bmod n \\ &= (2n + 0) \bmod n \\ &= 0 \end{aligned}$$

Length 1 Circular Queue

isEmpty → length = 0 & $(last-1) \bmod \text{Size} = first$

isFull → length = Size - 1

not isFull → length = $(\text{Size} + first - last + 1) \bmod \text{Size}$



$$\begin{aligned} \text{length} &= (n + 2 - 2 + 1) \bmod n \\ &= (n + 1) \bmod n \\ &= 1 \end{aligned}$$

Longer length Circular Queue

$$\text{length} = (\text{Size} + \text{first} - \text{last} + 1) \bmod \text{Size}$$

$$\begin{aligned} \text{length} &= (n + 3 - (n-3) + 1) \bmod n \\ &= (7) \bmod n \\ &= 7 \end{aligned}$$

