Assertions

How to write correct programs and know it

- Harlan Mills

Assertions

- Boolean expressions or predicates that evaluate to true or false in every state
- In a program they express constraints on the state that must be true at that point
- Associate with
 - » Individual program statements
 - » functions
 - » classes

Assertions & Correct Programs

- Specify clearly, precisely and succinctly
 - » What is expected and guaranteed by each component class, function and statement
- The essence of documentation
- Essential for debugging
- Aids in fault tolerance

Assertion Language Symbols

Arithmetic operators

```
+ - * / ^ (exponent)
// div (integer division)
\\ mod (modulus / remainder)
```

Relational operators

```
= \neq \leq \geq < >
```

Boolean operators & logic

```
\wedge and \vee or \oplus xor \neg ~ not \rightarrow implies \leftrightarrow iff
```

Assertion Language Symbols – 2

- Semi-strict and and or Eiffel only for practical and efficiency reasons
 - » Also called lazy evaluation in other programming languages

and then

A and then B Evaluate B only if A is true

or else

A or else B Evaluate B only if A is false

Assertion Language Symbols – 3

Predicate logic

```
\forall forall \exists exists (there exists)
```

- such that
- it is the case that (it holds that)
- Set operators

```
∈ member_of ∉ not_member_of
```

```
\supset \supseteq \subset \subseteq contains
```

- **⊄** does_not_contain
- ∩ intersection ∪ union \ set difference
- **#S** number of members of the set S

Assertion Language Special Symbols

Special variables related to program semantics

Result – result of a function

Current @ - current object

Void – not attached

Variable before and after values

Mathematical notation

name

value of the variable name before its value is changed name'

value of the variable name after a its value has changed

Unlimited context

Eiffel notation

name

value of the variable name after a routine terminates old name

value of the variable name before a routine starts

Limited context

Quantified Expression

Used to express properties about sets of objects

```
such that it is the case that

Quantifier Range_Expr [ I Restriction ] • Property

Quantifier ∀ forall ∃ exists (there exists)
```

Range_Expr var_name : set_of_values

Restriction Boolean expression or, recursively, a quantified expression

Property Boolean expression or, recursively, a quantified expression

Range Expression examples

Type range – each value is of a given type

v: VEHICLE

Sequence range – each value is in a sequence

k: low .. high

Member range – each value is a member in a set

c ∈ children



Mathematical Notation example

class CITIZEN feature name, sex, age: VALUE spouse: CITIZEN children, parents : SET[CITIZEN] single: BOOLEAN ensure Result \leftrightarrow (spouse = Void) divorce require ~ single ensure single ∧ (old spouse). single end invariant single \vee spouse . spouse = @ parents . count = 2 \forall c \in children • (\exists p \in c. parents • p = @) end

Textual Notation example

```
class CITIZEN feature
  name, sex, age: VALUE
  spouse: CITIZEN
  children, parents : SET[CITIZEN]
  single : BOOLEAN ensure Result iff( spouse = Void )
  divorce
    require not single
    ensure single and (old spouse). single
  end
invariant
    single or spouse.spouse = Current
    parents.count = 2
    for_all c member_of children it_holds
       (exists p member_of c.parents it_holds p = Current)
end
```

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Specifying Members of a Set

Set enumeration – list the members

$$S = \{ a, e, i, o, u \}$$

The set of vowels in the English alphabet

Set comprehension – logically specify members
 Notice that the forall is implicit not explicit

$$\{x, y : Integer \mid (0 < x < 10) \land (1 \le y \le 9) \cdot x^3 + y^3\}$$

The set of the sums of pairs of the cubes of single digit integers greater than zero

Pre-Conditions

- Statement syntax
 - » require boolean expression
- Where within function/procedure
 - » write immediately after the routine header

```
nonZero (row, col: INTEGER): BOOLEAN
-- Result true if non-zero element at <row, col>
require 0 < row and row < MaximumRow + 1
0 < col and col < MaximumCol + 1
do
...
end
```

Post-Conditions

- Statement syntax
 - » ensure boolean expression
- Where within function/procedure
 - » write just before the end for the routine body

State changes

- Show relationship between initial and final values
- At the end of the body the final values are in effect
- Refer to initial values using the keyword old

```
addElement ( element : TYPE )
require size < Capacity
do
...
ensure size = old size + 1
end
```

Assertions are tagged

Tag names are used to identify assertions

```
addElement ( element : TYPE )
require enough_space: size < Capacity
do
...
ensure one_larger: size = old size + 1
end
```

Non-executable assertions

- Use comments if you cannot write an executable assertion
- Use already defined functions or custom written functions

```
insert_in_row(matElem : MATRIX_ELEMENT)
   -- Insert the matrix element in the current row
   require ...
   local ...
   do ...
   ensure
   -- contains(MatrixElement(data, row, column)) at < row, column > end
```

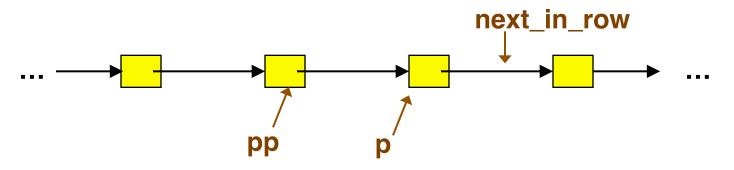
Loop Invariants & Loop Syntax

init statements
invariant
 assertions for invariant
until
 exit condition
loop
 body statements
variant
 integer expression
end

- Can invoke Boolean functions
- Use agents to implement predicate calculus expressions
- Always non negative
- Body decreases value on every iteration
- Ideally 0 on loop exit

Loop Invariant Example

Insert an element into a sorted by column singly linked list



```
row := matElem.row ; column := matElem.column
from p := rowList @ row
invariant ???
until
 p = void or p.column >= column
loop
 pp := p ; p := p.next_in_row
end
```

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Loop Invariant Example – 2

Using mathematical notation

Loop Invariant Example – 3

- Eiffel executable assertion.
- Column_less_than uses an agent to implement the invariant
 - > Agents and loop invariant details are in other slide sets

Check Assertion

- Within the body of a routine you can insert a check clause
- The check clause is executed and if an assertion is false then an exception occurs
- Used to remind the reader of a non obvious fact

```
If full then error := overflow
else
    check
    representation_exists : representation /= Void
    end
    representation.put(x) ; error := none
end
```

Class Invariants

Appear in the invariant clause just before the end of the class definition

```
class SPARSE_MATRIX
...
invariant
    actualRows <= maxRowCol
    actualCols <= maxRowCol
    -- forall row : maxNonzeroRow + 1 .. actualRows
    -- :: empty ( rowList [ row ] )
    -- forall col : maxNonzeroCol + 1 .. actualCols
    -- :: empty ( colList [ col ] )
end -- SPARSE_MATRIX
```

Class Invariants – 2

- Class invariants define which states of the ADT are valid
- True at stable times
 - » After make (object creation)
 - » Before and after every exported feature call
 - > Could be false during a feature call as various substates change
- Invariant is implicitly a part of every pre and post condition

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Class Invariants – examples

- See slides 9 & 10 in this set of slides
 - » Relationship between parents and children
 - » Relationship between spouses
- See Abstract data type documentation slides 18..23
 - » Relationship between first and last pointers in a circular queue and the length of the queue
- Case studies
 - » Sparse matrix
- Report 1 system

General Guideline

- Assertions may be written in many ways
 - » Select the representation to be as clear and easy to understand as possible
 - > Point is to convey information, not provide a puzzle to be solved
 - When the second is a second in the second

```
> Set notation { ... }
```

- > Bag notation [[...]]
- > Sequence notation < ... >

Assertion Monitoring

Eiffel provides multiples levels of assertion monitoring

Always should be on during debugging

 Turn off as little as possible only if time is critical and the system can be trusted