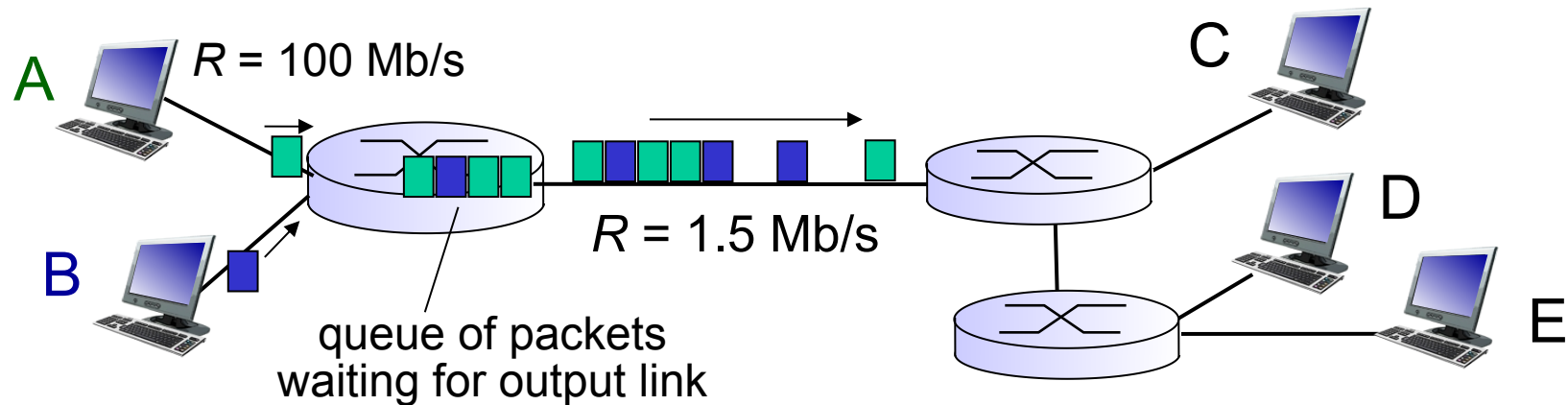


# Packet Switching: queueing delay, loss



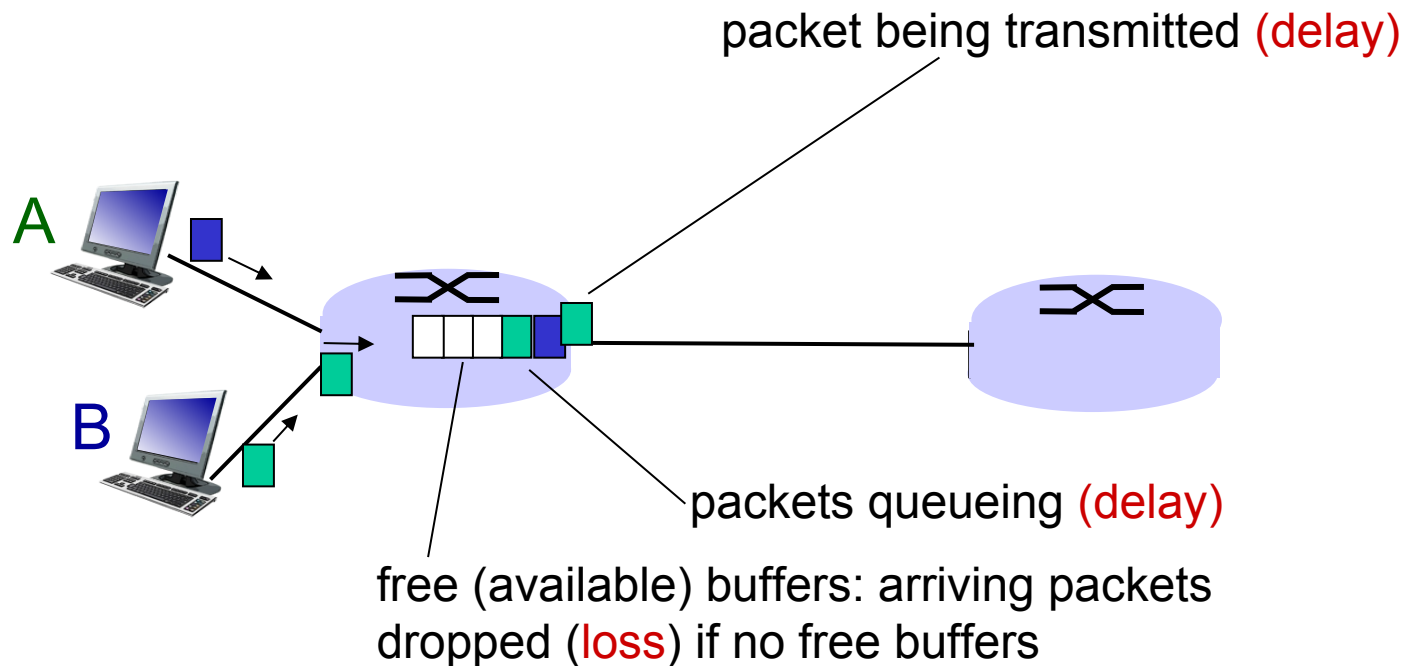
## queueing and loss:

- ❖ If arrival rate (in bits) to link exceeds transmission rate of link for a period of time:
  - packets will queue, wait to be transmitted on link
  - packets can be dropped (lost) if memory (buffer) fills up

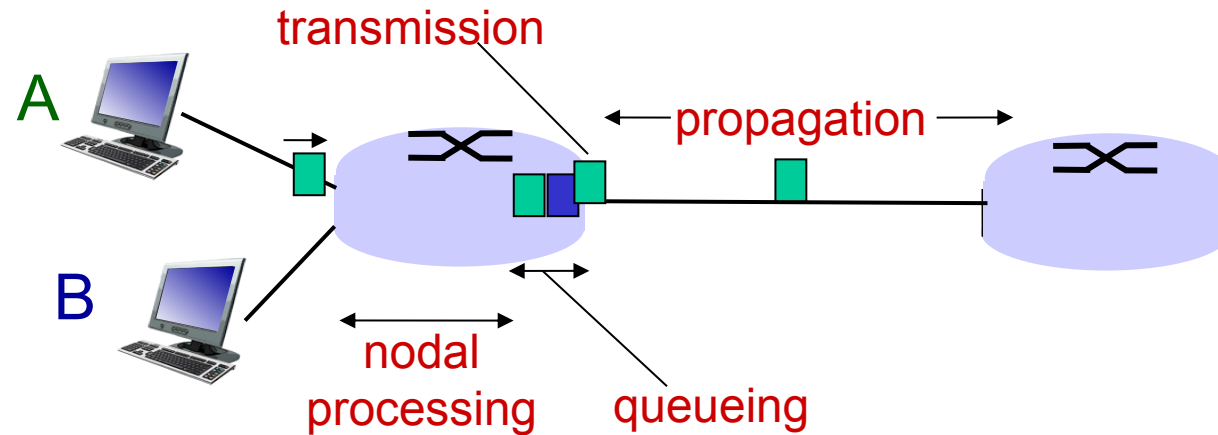
# How do loss and delay occur?

packets *queue* in router buffers

- ❖ packet arrival rate to link (temporarily) exceeds output link capacity
- ❖ packets queue, wait for turn



# Four sources of packet delay



$$d_{\text{nodal}} = d_{\text{proc}} + d_{\text{queue}} + d_{\text{trans}} + d_{\text{prop}}$$

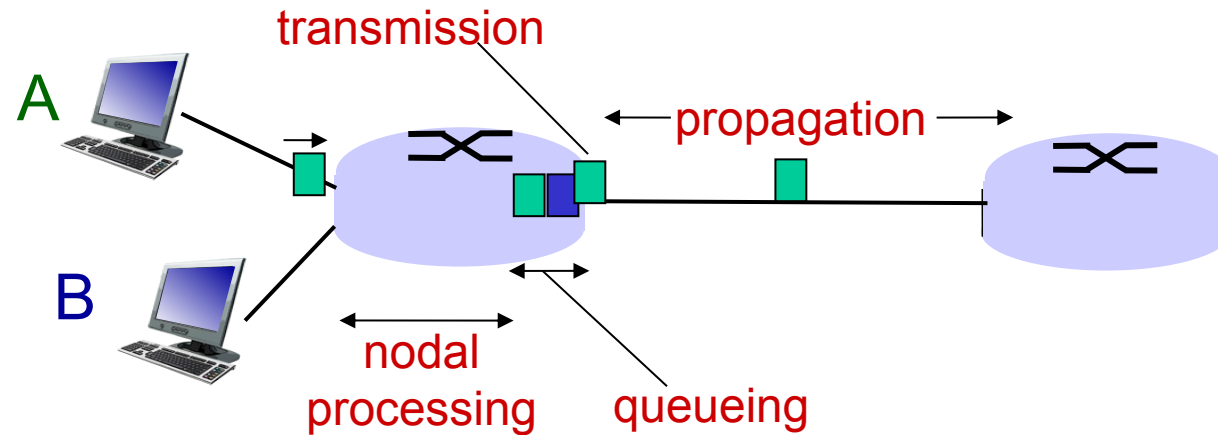
## $d_{\text{proc}}$ : nodal processing

- check bit errors
- determine output link
- typically < msec

## $d_{\text{queue}}$ : queueing delay

- time waiting at output link for transmission
- depends on congestion level of router

# Four sources of packet delay



$$d_{\text{nodal}} = d_{\text{proc}} + d_{\text{queue}} + d_{\text{trans}} + d_{\text{prop}}$$

$d_{\text{trans}}$ : transmission delay:

- $L$ : packet length (bits)
- $R$ : link *bandwidth* (bps)
- $d_{\text{trans}} = L/R$

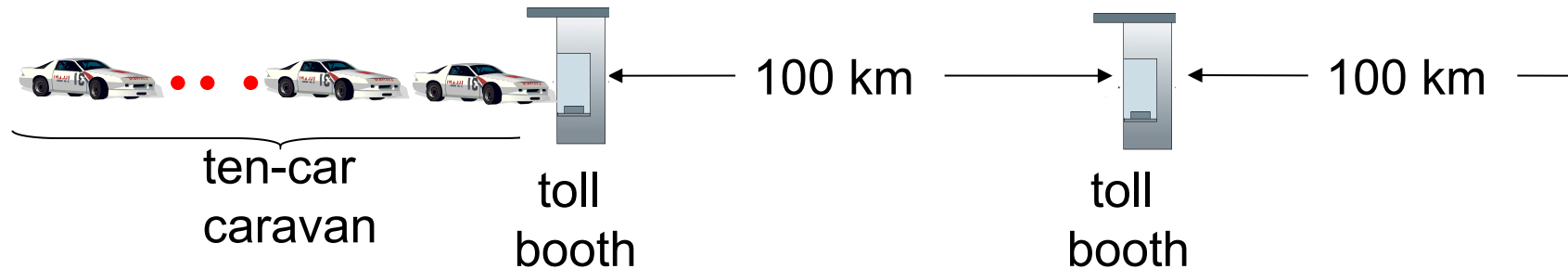
$d_{\text{prop}}$ : propagation delay:

- $d$ : length of physical link
- $s$ : propagation speed in medium ( $\sim 2 \times 10^8$  m/sec)
- $d_{\text{prop}} = d/s$

$d_{\text{trans}}$  and  $d_{\text{prop}}$   
very different

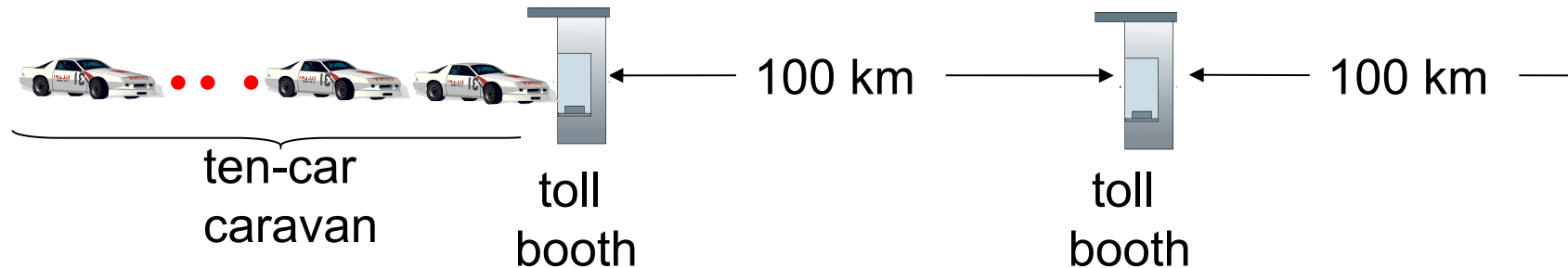
\* Check out the Java applet for an interactive animation on trans vs. prop delay

# Caravan analogy



- ❖ cars “propagate” at 100 km/hr
  - ❖ toll booth takes 12 sec to service car (bit transmission time)
  - ❖ car~bit; caravan ~ packet
  - ❖ **Q: How long until caravan is lined up before 2nd toll booth?**
- time to “push” entire caravan through toll booth onto highway =  $12 \times 10 = 120$  sec
  - time for last car to propagate from 1st to 2nd toll booth:  $100\text{km}/(100\text{km/hr}) = 1$  hr
  - **A: 62 minutes**

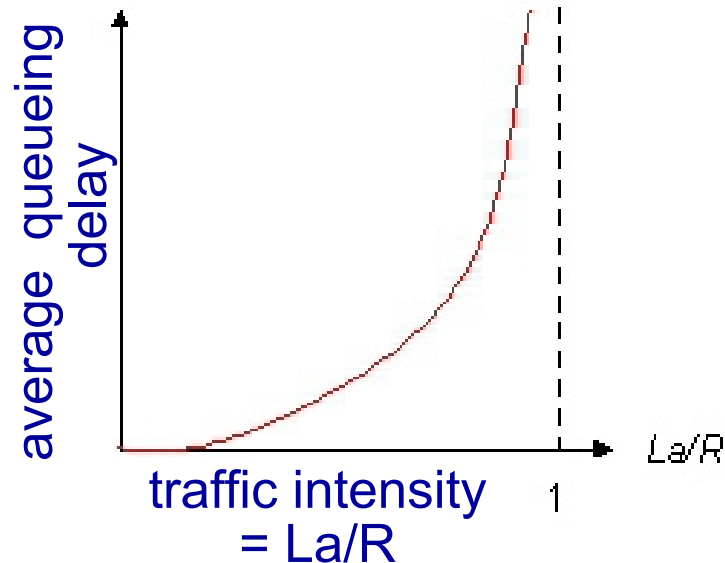
# Caravan analogy (more)



- ❖ suppose cars now “propagate” at 1000 km/hr
- ❖ and suppose toll booth now takes one min to service a car
- ❖ **Q: Will cars arrive to 2nd booth before all cars serviced at first booth?**
  - **A: Yes!** after 7 min, 1st car arrives at second booth; three cars still at 1st booth.

# Queueing delay (revisited)

- ❖  $R$ : link bandwidth (bps)
- ❖  $L$ : packet length (bits)
- ❖  $a$ : average packet arrival rate



- ❖  $La/R \sim 0$ : avg. queueing delay small
- ❖  $La/R \rightarrow 1$ : avg. queueing delay large
- ❖  $La/R > 1$ : more “work” arriving than can be serviced, average delay infinite!



$La/R \sim 0$



$La/R \rightarrow 1$

\* Check out the Java applet for an interactive animation on queueing and loss

# Queueing Theory Basics

- ❖ Each 'node' or 'station' or router called a queue
- ❖ Each packet called a 'job'
- ❖ A queue has a servicing/processing station and a buffer or queue where jobs wait for service
- ❖ The behaviour of a queue is determined by the queueing policy (e.g. FIFO) and the service time (e.g. proportional to packet length or fixed)
- ❖ The performance (throughput, delay etc) depends on the queue parameters and the arrival process of jobs

# Analysis

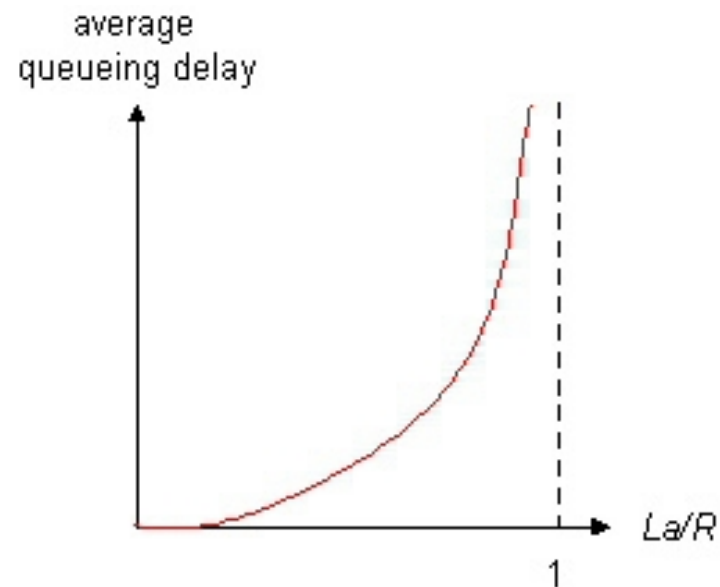
- ❖ Analysis of a single queue is difficult
- ❖ Analysis of networks of queues is even more difficult.
- ❖ The best-known results are derived with strong assumptions on all parameters.
- ❖ The standard naming scheme of queues is of the form  $X/Y/k/b$  where  $X$  = arrival process,  $Y$  = service time process,  $k$  = number of service stations,  $b$  = length of buffer
- ❖ We will only look at  $M/M/1/\infty$  queues (M=markovian)
- ❖ For networks of  $M/M/1/\infty$  queues, it is enough to analyze single queues. Network performance can be very easily obtained from individual queue performance.

# M/M/1/ $\infty$ queues

- ❖ The first M: Poisson arrival process.  
Probability of  $N(t)$  packets arriving in any interval of time  $t$  is  
$$P(N(t)=k) = (\lambda t)^k \exp(-\lambda t)/k!, \quad k = 0, 1, 2, \dots$$
- ❖ The second M: Exponential interarrival times  
Probability of job  $k$  arriving  $t$  units after job  $k-1$  is  $P(x=t) = \mu \exp(-\mu t)$  if  $t > 0$  and 0 otherwise.  
It follows that  $E[x] = 1/\mu$ ,  $\text{variance}[x] = 1/\mu^2$
- ❖ Under these assumptions, utilization =  
 $\text{Prob}(\text{queue is non-empty}) = \rho$   
where  $\rho = \lambda/\mu$
- ❖ So when  $\lambda$  approaches  $\mu$  (cannot exceed  $\mu$ ), utilization goes towards 100%

# M/M/1/ $\infty$ queues - contd.

- ❖ However, expected number of jobs in the queue is  $= \rho / (1 - \rho)$  where  $\rho = \lambda / \mu$
- ❖ So when  $\lambda$  approaches  $\mu$  the number of jobs in the queue approaches infinity!!
- ❖ As a result delay goes up.
- ❖ Therefore most systems cannot be driven at capacity.



# Little's Law

- ❖ One of the very few general laws:

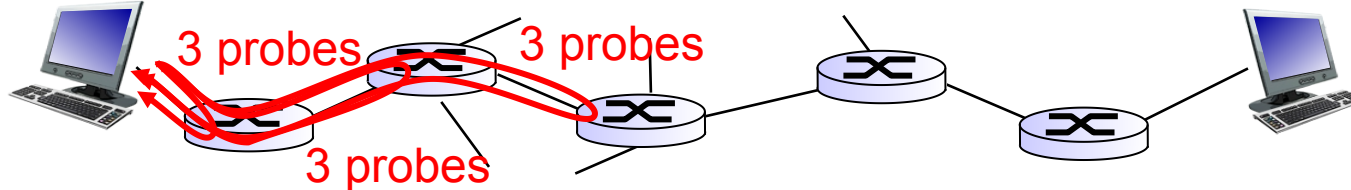
The average number of customers in a (stable) queueing system  $L$  is equal to the long-term average effective arrival rate,  $\lambda$ , multiplied by the average time a customer spends in the system,  $W$ ; or  $L = \lambda W$ .

Applies to single queues or networks

So average delay seen by a packet (from previous slide) =  $\rho / [\lambda (1 - \rho)]$

# “Real” Internet delays and routes

- ❖ what do “real” Internet delay & loss look like?
- ❖ `traceroute` program: provides delay measurement from source to router along end-end Internet path towards destination.  
For all  $i$ :
  - sends three packets that will reach router  $i$  on path towards destination
  - router  $i$  will return packets to sender
  - sender times interval between transmission and reply.



# “Real” Internet delays, routes

**traceroute:** gaia.cs.umass.edu to www.eurecom.fr

3 delay measurements from  
gaia.cs.umass.edu to cs-gw.cs.umass.edu



1 cs-gw (128.119.240.254) 1 ms 1 ms 2 ms  
2 border1-rt-fa5-1-0.gw.umass.edu (128.119.3.145) 1 ms 1 ms 2 ms  
3 cht-vbns.gw.umass.edu (128.119.3.130) 6 ms 5 ms 5 ms  
4 jn1-at1-0-0-19.wor.vbns.net (204.147.132.129) 16 ms 11 ms 13 ms  
5 jn1-so7-0-0-0.wae.vbns.net (204.147.136.136) 21 ms 18 ms 18 ms  
6 abilene-vbns.abilene.ucaid.edu (198.32.11.9) 22 ms 18 ms 22 ms  
7 nycm-wash.abilene.ucaid.edu (198.32.8.46) 22 ms 22 ms 22 ms  
8 62.40.103.253 (62.40.103.253) 104 ms 109 ms 106 ms  
9 de2-1.de1.de.geant.net (62.40.96.129) 109 ms 102 ms 104 ms  
10 de.fr1.fr.geant.net (62.40.96.50) 113 ms 121 ms 114 ms  
11 renater-gw.fr1.fr.geant.net (62.40.103.54) 112 ms 114 ms 112 ms  
12 nio-n2.cssi.renater.fr (193.51.206.13) 111 ms 114 ms 116 ms  
13 nice.cssi.renater.fr (195.220.98.102) 123 ms 125 ms 124 ms  
14 r3t2-nice.cssi.renater.fr (195.220.98.110) 126 ms 126 ms 124 ms  
15 eurecom-valbonne.r3t2.ft.net (193.48.50.54) 135 ms 128 ms 133 ms  
16 194.214.211.25 (194.214.211.25) 126 ms 128 ms 126 ms  
17 \* \* \*  
18 \* \* \*  
19 fantasia.eurecom.fr (193.55.113.142) 132 ms 128 ms 136 ms

trans-oceanic link



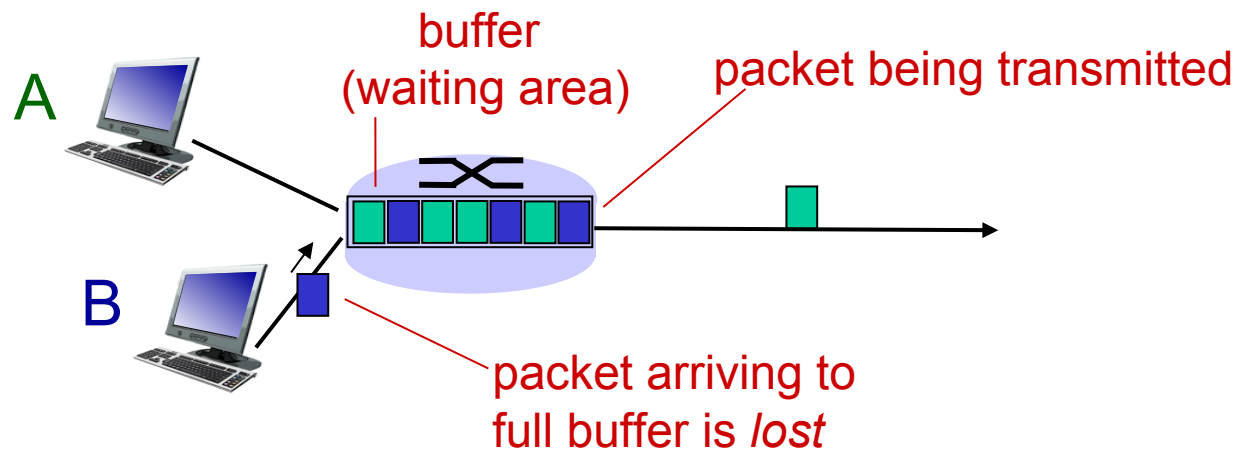
\* means no response (probe lost, router not replying)



\* Do some traceroutes from exotic countries at [www.traceroute.org](http://www.traceroute.org)

# Packet loss

- ❖ queue (aka buffer) preceding link in buffer has finite capacity
- ❖ packet arriving to full queue dropped (aka lost)
- ❖ lost packet may be retransmitted by previous node, by source end system, or not at all



\* Check out the Java applet for an interactive animation on queuing and loss

# Throughput

- ❖ *throughput*: rate (bits/time unit) at which bits transferred between sender/receiver
  - *instantaneous*: rate at given point in time
  - *average*: rate over longer period of time

