#### More Data Structures (Part 2)

Queues

#### Queue



#### Queue



## **Queue Operations**

- classically, queues only support two operations
  - 1. enqueue
    - add to the back of the queue
  - 2. dequeue
    - remove from the front of the queue

## **Queue Optional Operations**

- optional operations
  - 1. size
    - number of elements in the queue
  - 2. isEmpty
    - is the queue empty?
  - 3. peek
    - get the front element (without removing it)
  - 4. search
    - find the position of the element in the queue
  - 5. isFull
    - is the queue full? (for queues with finite capacity)
  - 6. capacity
    - total number of elements the queue can hold (for queues with finite capacity)



- 5. **q.enqueue("E")**
- 4. **q.enqueue("D")**
- 3. **q.enqueue("C")**
- 2. **q.enqueue("B")**
- 1. **q.enqueue("A")**

#### Enqueue

1. String s = q.dequeue()



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- 2. s = q.dequeue()



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- 2. s = q.dequeue()
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- $4 \cdot \mathbf{s} = \mathbf{q} \cdot \mathbf{dequeue}()$
- 5. s = q.dequeue()



### FIFO

- queue is a First-In-First-Out (FIFO) data structure
  - the first element enqueued in the queue is the first element that can be accessed from the queue

## Implementation with LinkedList

- a linked list can be used to efficiently implement a queue as long as the linked list keeps a reference to the last node in the list
  - required for enqueue
- the head of the list becomes the front of the queue
  - removing (dequeue) from the head of a linked list requires
     O(1) time
  - adding (enqueue) to the end of a linked list requires O(1) time if a reference to the last node is available
- java.util.LinkedList is a doubly linked list that holds a reference to the last node

```
public class Queue<E> {
  private LinkedList<E> q;
  public Queue() {
    this.q = new LinkedList<E>();
  }
  public enqueue(E element) {
    this.q.addLast(element);
  }
  public E dequeue() {
    return this.q.removeFirst();
```

## Implementation with LinkedList

- note that there is no need to implement your own queue as there is an existing interface
  - the interface does not use the names enqueue and dequeue however

## java.util.Queue

# public interface Queue<E> extends Collection<E>

boolean	add(E e)
	Inserts the specified element into this queue
Е	remove()
	Retrieves and removes the head of this queue
Е	peek()
	Retrieves, but does not remove, the head of this queue

#### plus other methods

http://docs.oracle.com/javase/7/docs/api/java/util/Queue. html

## java.util.Queue

- LinkedList implements Queue so if you ever need a queue you can simply use:
  - e.g. for a queue of strings

Queue<String> q = new LinkedList<String>();

## Queue applications

- queues are useful whenever you need to hold elements in their order of arrival
  - serving requests of a single resource
    - printer queue
    - disk queue
    - CPU queue
    - web server

## **Robotics example**

- in robotics, the path planning problem is
  - given a map of the environment, find a path between the starting point of the robot and a goal location that does not pass through any obstacles
- one approach is to use a grid for the map

#### Grid-based map



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- the wave-front planner finds a path between a start and goal point in spaces represented as a grid where
  - free space is labeled with a o
  - obstacles are labeled with a 1
  - the goal is labeled with a 2
  - the start is known



starting with the goal cell

```
label L = 2
while start cell is unlabelled {
  for each cell C with label L {
    for each cell Z connected to C with label 0 {
      label Z with L+1
    }
  }
  L = L + 1
```







goal



D





start

to generate a path starting from the start point

```
L = start point label
while not at the goal {
  move to any connected cell with label L-1
  L = L-1
}
```



start

## Breadth-first search

- the wave-front planner is actually a classic computer science algorithm called breadth-first search
- visiting every node of a tree using breadth-first search results in visiting nodes in order of their level in the tree



#### BFS: <u>5</u>0



#### BFS: 50, 27, 73



BFS: 50, 27, 73, 8, 44, 83



BFS: 50, 27, 73, 8, 44, 83, 73, 93

#### Breadth-first search algorithm

```
Q.enqueue(root node)
while Q is not empty {
  n = Q.dequeue()
  if n.left != null {
    Q.enqueue(n.left)
  }
  if n.right != null {
    Q.enqueue(n.right)
  }
```
















dequeue 44







BFS: 50, 27, 73, 8, 44, 83, 73, 93 dequeue 93



BFS: 50, 27, 73, 8, 44, 83, 73, 93 queue empty

### Previous written exam question

Suppose that you have a **Stack** class that has only the following features:

- the elements are of type int
- a default constructor that creates an empty stack
- a method **isEmpty** that returns true if the stack is empty
- **push** and **pop** methods

Describe how you would write a (static) method that makes a copy of a stack. A postcondition of your method must be that the state of the stack when the method finishes is the same as when the method started. Try to avoid using additional data structures (such as lists and arrays) if possible. Functional Java code is not required.

### Previous written exam question

Suppose that you have a **Queue** class that has only the following features:

- the elements are of type int
- a default constructor that creates an empty queue
- a method **size** that returns the number of elements in the queue
- **enqueue** and **dequeue** methods

Describe how you would write a (static) method that makes a copy of a queue. A postcondition of your method must be that the state of the queue when the method finishes is the same as when the method started. Try to avoid using additional data structures (such as lists and arrays) if possible. Functional Java code is not required.

### Summary

# **Major Topics**

- 1. static features (utility classes)
- 2. non-static features
- 3. mixing static and non-static features
- 4. aggregation and composition
- 5. inheritance
- 6. graphical user interfaces
- 7. recursion
- 8. data structures

### Inheritance

means

#### is-a

#### or is-substitutable-for



## What is a Subclass?

- a subclass looks like a new class that has the same API as its superclass with perhaps some additional methods and attributes
- inheritance does more than copy the API of the superclass
  - the derived class contains a subobject of the parent class
  - the superclass subobject needs to be constructed (just like a regular object)
    - the mechanism to perform the construction of the superclass subobject is to call the superclass constructor

Mix mutt = new Mix(1, 10);

- 1. Mix constructor starts running
- creates new Dog subobject by invoking the Dog constructor
  - 2. Dog constructor starts running
  - creates new Object subobject
     by (silently) invoking the
     Object constructor
    - 3. Object constructor runs
  - sets size and energy
- creates a new empty ArrayList and assigns it to breeds

Mix object		
Dog object		
Object object		
size	1	
energy	10	
breeds	1000	

## Strength of a Precondition

 to strengthen a precondition means to make the precondition more restrictive



## Preconditions on Overridden Methods

- a subclass can change a precondition on a method but it must not strengthen the precondition
  - a subclass that strengthens a precondition is saying that it cannot do everything its superclass can do

```
// Dog setEnergy // Mix setEnergy
// assume non-final // bad : strengthen precond.
// @pre. none // @pre. 1 <= nrg <= 10
public
void setEnergy(int nrg) public
void setEnergy(int nrg) {
 { // ... } {
 { if (nrg < 1 || nrg > 10)
 { // throws exception }
 // ...
```

client code written for Dogs now fails when given a
 Mix

```
// client code that sets a Dog's energy to zero
public void walk(Dog d)
{
   d.setEnergy(0);
}
```

 remember: a subclass must be able to do everything its ancestor classes can do; otherwise, clients will be (unpleasantly) surprised

## Strength of a Postcondition

 to strengthen a postcondition means to make the postcondition more restrictive





## Postconditions on Overridden Methods

- a subclass can change a postcondition on a method but it must not weaken the postcondition
  - a subclass that weakens a postcondition is saying that it cannot do everything its superclass can do

Dogzilla: a made-up breed of dog that has no upper limit on its size

#### client code written for Dogs can now fail when given a Dogzilla

 remember: a subclass must be able to do everything its ancestor classes can do; otherwise, clients will be (unpleasantly) surprised

## **Exceptions and Inheritance**

- a method that claims to throw an exception of type x is allowed to throw any exception type that is a subclass of x
  - this makes sense because exceptions are objects and subclass objects are substitutable for ancestor classes

```
// in Dog
public void someDogMethod() throws DogException
{
    // can throw a DogException, BadSizeException,
    // NoFoodException, or BadDogException
}
```

- a method that overrides a superclass method that claims to throw an exception of type x must also throw an exception of type x or a subclass of x
  - remember: a subclass promises to do everything its superclass does; if the superclass method claims to throw an exception then the subclass must also

### Which are Legal?

• in Mix

@Override

public void someDogMethod() throws BadDogException

@Override

public void someDogMethod() throws Exception

@Override

public void someDogMethod()

@Override

public void someDogMethod()

throws DogException, IllegalArgumentException

technically legal, but don't do this









## Abstract Classes

- abstract classes appear when there are common attributes and methods that all subclasses share
- often, only the subclasses will have enough information to implement the methods
  - these methods are marked abstract in the parent class to indicate that subclasses are responsible for providing the implementation

### **Static Features and Inheritance**

- non-private static attributes are inherited
  - but there is still only one copy of the attribute and it is in the parent class
- non-private static methods are inherited
  - but they cannot be overridden, they can only be hidden

### Interfaces

- in Java an *interface* is a reference type (similar to a class)
- an interface says what methods an object must have and what the methods are supposed to do
  - i.e., an interface is an API
- unlike inheritance, a class may implement as many interfaces as needed

## Model-View-Controller

model

 represents state of the application and the rules that govern access to and updates of state

view

- presents the user with a sensory (visual, audio, haptic) representation of the model state
- a user interface element (the user interface for simple applications)
- controller
  - processes and responds to events (such as user actions) from the view and translates them to model method calls

🕌 Simple Calculator	
File	
Calculated Value 0	Input Add Subtract Multiply Divide Clear



### Recursion

- a method that calls itself is called a *recursive* method
- a recursive method solves a problem by repeatedly reducing the problem so that a base case can be reached

```
printIt("*", 5)
*printIt("*", 4)
**printIt("*", 3)
*the string is printed decreases
after each recursive call to printIt
****printIt("*", 1)
*****printIt("*", 0) base case
****
```

## **Proving Correctness and Termination**

- to show that a recursive method accomplishes its goal you must prove:
  - 1. that the base case(s) and the recursive calls are correct
  - 2. that the method terminates

### **Proving Correctness**

- to prove correctness:
  - 1. prove that each base case is correct
  - 2. assume that the recursive invocation is correct and then prove that each recursive case is correct

### Correctness of printltToo

- 1. (prove the base case) If n == 0 nothing is printed; thus the base case is correct.
- Assume that printItToo(s, n-1) prints the string s exactly(n - 1) times. Then the recursive case prints the string s exactly(n - 1)+1 = n times; thus the recursive case is correct.
# **Proving Termination**

- to prove that a recursive method terminates:
  - define the size of a method invocation; the size must be a non-negative integer number
  - 2. prove that each recursive invocation has a smaller size than the original invocation

## Termination of printlt

- 1. printIt(s, n) prints n copies of the string s; define the size of printIt(s, n) to be n
- 2. The size of the recursive invocation printIt(s, n-1) is n-1 (by definition) which is smaller than the original size n.

### **Recurrence Relation**

- analyzing the runtime of an algorithm often leads to a recurrence relation *T*(*n*), e.g.,
  - T(n) = 2T(n/2) + O(n)
  - ► T(n) = T(n-1) + T(n-2)
- solving the recurrence can sometimes be done by substitution

### Solving the Recurrence Relation

T(n) approaches...

- $T(n) \rightarrow 2T(n/2) + O(n)$ 
  - $\approx 2T(n/2) + n$
  - = 2[2T(n/4) + n/2] + n
  - = **4**T(n/4) + **2**n
  - = 4[2T(n/8) + n/4] + 2n
  - = 8*T*(*n*/8) + 3*n*
  - = 8[2T(n/16) + n/8] + 3n
  - = 16T(n/16) + 4n=  $2^{k}T(n/2^{k}) + kn$

#### Solving the Recurrence Relation

$$T(n) = 2^k T(n/2^k) + kn$$

- for a list of length 1 we know T(1) = 1
  - if we can substitute *T*(*i*) into the right-hand side of *T*(*n*) we might be able to solve the recurrence

$$n/\mathbf{2}^k = \mathbf{1} \implies \mathbf{2}^k = n \Longrightarrow k = \log(n)$$

#### Data Structures

- recursive
  - linked list
  - binary tree
- stack
- queue