

# Recursive Objects

# Recursive Objects

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- ▶ an object that holds a reference to its own type is a recursive object
  - ▶ linked lists and trees are classic examples in computer science of objects that can be implemented recursively

# Data Structures

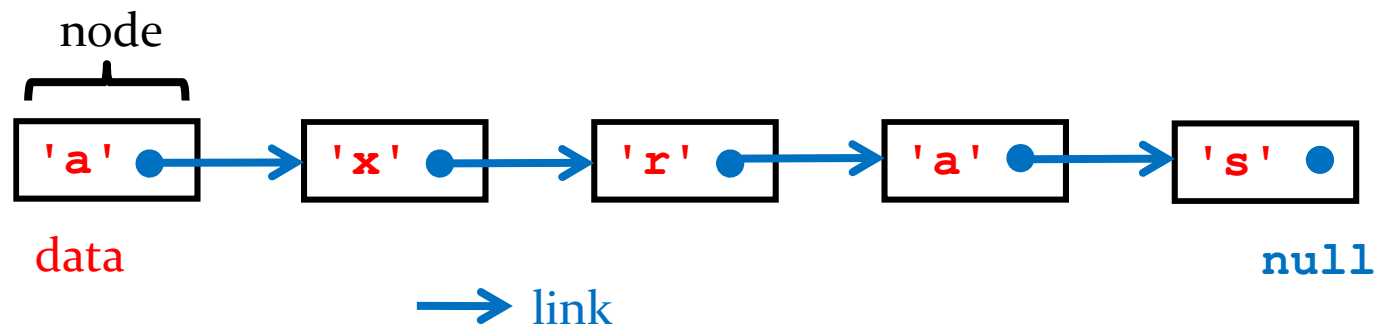
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- ▶ data structures (and algorithms) are one of the foundational elements of computer science
- ▶ a data structure is a way to organize and store data so that it can be used efficiently
  - ▶ list – sequence of elements
  - ▶ set – a group of unique elements
  - ▶ map – access elements using a key
  - ▶ many more...

# Linked Lists

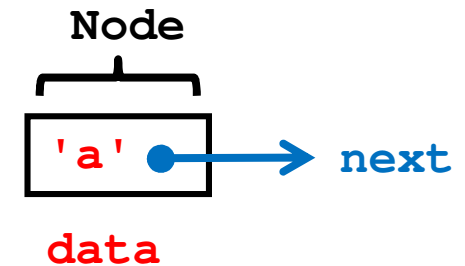
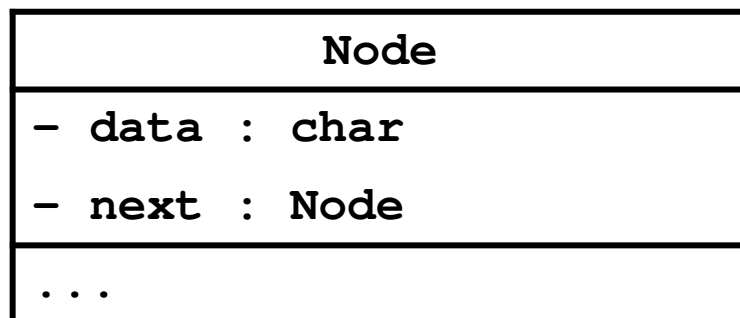
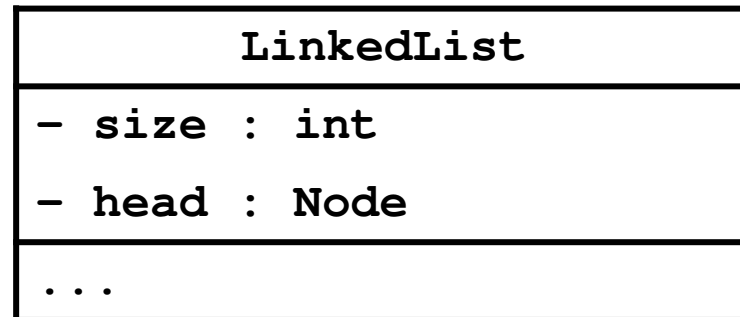
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- ▶ a data structure made up of a sequence of nodes
- ▶ each node has
  - ▶ some data
  - ▶ a field that contains a reference (a *link*) to the **next** node in the sequence
- ▶ suppose we have a linked list that holds characters; a picture of our linked list would be:



# UML Class Diagram

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# Node

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- ▶ nodes are implementation details that the client does not need to know about
  - ▶ can be private inner classes

```
public class LinkedList {  
  
    private static class Node {  
        private char data;  
        private Node next;  
  
        public Node(char c) {  
            this.data = c;  
            this.next = null;  
        }  
    }  
  
    // ...  
}
```

# LinkedList constructor

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```
/**
 * Create a linked list of size 0.
 *
 */
public LinkedList() {
    this.size = 0;
    this.head = null;
}
```



# Node constructor

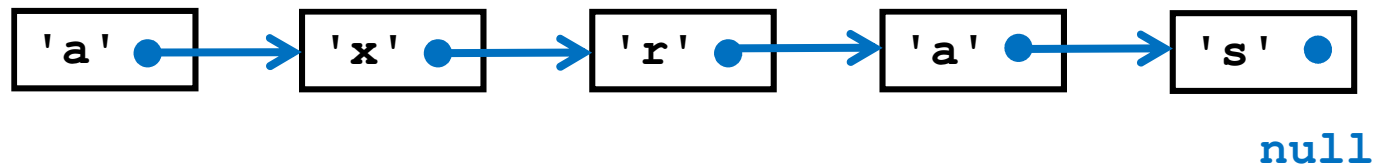
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```
/**
 * Create a node with the given character.
 *
 */
public Node(char c) {
    this.data = c;
    this.next = null;
}
```

# Creating a Linked List

---

- ▶ to create the following linked list:



```
LinkedList t = new LinkedList();  
t.add('a');  
t.add('x');  
t.add('r');  
t.add('a');  
t.add('s');
```

# Add to end of list

---

- ▶ methods of recursive objects can often be implemented with a recursive algorithm
  - ▶ notice the word "can"; the recursive implementation is not necessarily the most efficient implementation
- ▶ adding to the end of the list can be done recursively
  - ▶ base case: at the end of the list
    - ▶ i.e., **next** is **null**
    - ▶ create new node and append it to this link
  - ▶ recursive case: current link is not the last link
    - ▶ add to the end of **next**

```
/**
 * Adds the given character to the end of the list.
 *
 * @param c The character to add
 */
public void add(char c) {
    if (this.size == 0) {
        this.head = new Node(c);
    }
    else {
        LinkedList.add(c, this.head);
    }
    this.size++;
}
```

recursive method

```
/**
 * Adds the given character to the end of the list.
 *
 * @param c The character to add
 * @param node The node at the head of the current sublist
 */
private static void add(char c, Node node) {
    if (node.next == null) {
        node.next = new Node(c);
    }
    else {
        LinkedList.add(c, node.next);
    }
}
```

# Getting an Element in the List

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- ▶ a client may wish to retrieve the  $i$ th element from a list
  - ▶ the ability to access arbitrary elements of a sequence in the same amount of time is called *random access*
  - ▶ arrays support random access; linked lists do not
- ▶ to access the  $i$ th element in a linked list we need to sequentially follow the first  $(i - 1)$  links



`t.get(3)`            **link 0**      **link 1**      **link 2**

- ▶ takes  $O(n)$  time versus  $O(1)$  for arrays

# Getting an Element in the List

---

- ▶ validation?
- ▶ getting the *i*th element can be done recursively
  - ▶ base case: **index == 0**
    - ▶ return the value held by the current link
  - ▶ recursive case: current link is not the last link
    - ▶ get the element at **index - 1** starting from **next**

```
/**
 * Returns the item at the specified position
 * in the list.
 *
 * @param index index of the element to return
 * @return the element at the specified position
 * @throws IndexOutOfBoundsException if the index
 *         is out of the range
 *         {@code (index < 0 || index >= list size)}
 */
public char get(int index) {
    if (index < 0 || index >= this.size) {
        throw new IndexOutOfBoundsException("Index: " + index +
                                           ", Size: " + this.size);
    }
    return LinkedList.get(index, this.head);
}
```

recursive method



```
/**
 * Returns the item at the specified position
 * in the list.
 *
 * @param index index of the element to return
 * @param node The node at the head of the current sublist
 * @return the element at the specified position
 */
private static char get(int index, Node node) {
    if (index == 0) {
        return node.data;
    }
    return LinkedList.get(index - 1, node.next);
}
```

# Setting an Element in the List

---

- ▶ setting the  $i$ th element is almost exactly the same as getting the  $i$ th element

```
/**
 * Sets the element at the specified position
 * in the list.
 *
 * @param index index of the element to set
 * @param c new value of element
 * @throws IndexOutOfBoundsException if the index
 *         is out of the range
 *         {@code (index < 0 || index >= list size)}
 */
public void set(int index, char c) {
    if (index < 0 || index >= this.size) {
        throw new IndexOutOfBoundsException("Index: " + index +
                                           ", Size: " + this.size);
    }
    LinkedList.set(index, c, this.head);
}

```

recursive method

```
/**
 * Sets the element at the specified position
 * in the list.
 *
 * @param index index of the element to set
 * @param c new value of the element
 * @param node The node at the head of the current sublist
 */
private static void set(int index, char c, Node node) {
    if (index == 0) {
        node.data = c;
        return;
    }
    LinkedList.set(index - 1, c, node.next);
}
```

# toString

---

- ▶ finding the string representation of a list can be done recursively



- ▶ the string is  
`"[a, x, r, a, s]"`
- ▶ the string is  
`"[" + "a, " + toString(the list['x', 'r', 'a', 's'])`

# toString

---

- ▶ base case: **next** is **null**
  - ▶ return the value of the link as a string + "]"
- ▶ recursive case: current link is not the last link
  - ▶ return the value of the link as a string + ", " + the rest of the list as a string

```
public String toString() {  
    if (this.size == 0) {  
        return "[]";  
    }  
    return "[" + LinkedList.toString(this.head);  
}
```

recursive method

```
private static String toString(Node n) {  
    if (n.next == null) {  
        return n.data + "];";  
    }  
    String s = n.data + ", ";  
    return s + LinkedList.toString(n.next);  
}
```

# Finding an element in the list

---

- ▶ often useful to ask if a list contains a particular element
- ▶ worst case: must visit every element of the list



- ▶ e.g., `t.contains('z')`



# Finding an element in the list

---

- ▶ contains can be solved recursively
  - ▶ base case: found the character we are looking for
    - ▶ i.e., node **data** is equal to the character we are searching for
      - return true
  - ▶ base case: at the end of the list
    - ▶ i.e., node **next** is **null**
      - return false
  - ▶ recursive case: have not found the character we are searching for and not at the end of the list
    - ▶ search the sublist starting at **node.next**
      - return result

```
/**
 * Returns true if this list contains the specified
 * element.
 *
 * @param c element to search for
 * @return true if this list contains the
 * specified element
 */
public boolean contains(char c) {
    if (this.size == 0) {
        return false;
    }
    return LinkedList.contains(c, this.head);
}
```

recursive method

```
/**
 * Returns true if this list contains the specified
 * element.
 *
 * @param c element to search for
 * @param node the node at the head of the current sublist
 * @return true if this list contains the
 * specified element
 */
private static boolean contains(char c, Node node) {
    if (node.data == c) {
        return true;
    }
    if (node.next == null) {
        return false;
    }
    return LinkedList.contains(c, node.next);
}
```

# Finding an element in the list

---

- ▶ closely related to `contains` is finding the index of an element in the list
- ▶ worst case: must visit every element of the list



- ▶ e.g., `t.indexOf('s')`

# Finding an element in the list

---

- ▶ **indexOf** can be solved recursively
  - ▶ base case: found the character we are looking for
    - ▶ i.e., node **data** is equal to the character we are searching for
      - return 0
  - ▶ base case: at the end of the list
    - ▶ i.e., node **next** is **null**
      - return -1
  - ▶ recursive case: have not found the character we are searching for and not at the end of the list
    - ▶ search the sublist starting at **node.next**
      - return 1 + result

```
/**
 * Returns the index of the first occurrence of the
 * specified element in this list, or -1 if this list
 * does not contain the element.
 *
 * @param c
 *         element to search for
 * @return the index of the first occurrence of the
 *         specified element in this list, or -1 if this
 *         list does not contain the element
 */
public int indexOf(char c) {
    if (this.size == 0) {
        return -1;
    }
    return LinkedList.indexOf(c, this.head);
}
```

recursive method

```
private static int indexOf(char c, Node n) {
    if (n.data == c) {
        return 0;
    }
    if (n.next == null) {
        return -1;
    }
    int i = LinkedList.indexOf(c, n.next);
    if (i == -1) {
        return -1;
    }
    return 1 + i;
}
```

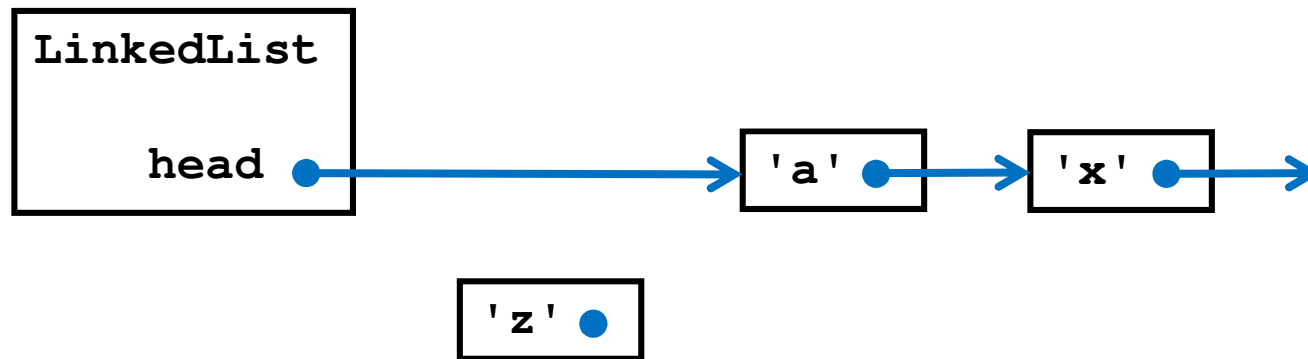
# Recursive Objects (Part 2)



# Adding to the front of the list

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- ▶ adding to the front of the list

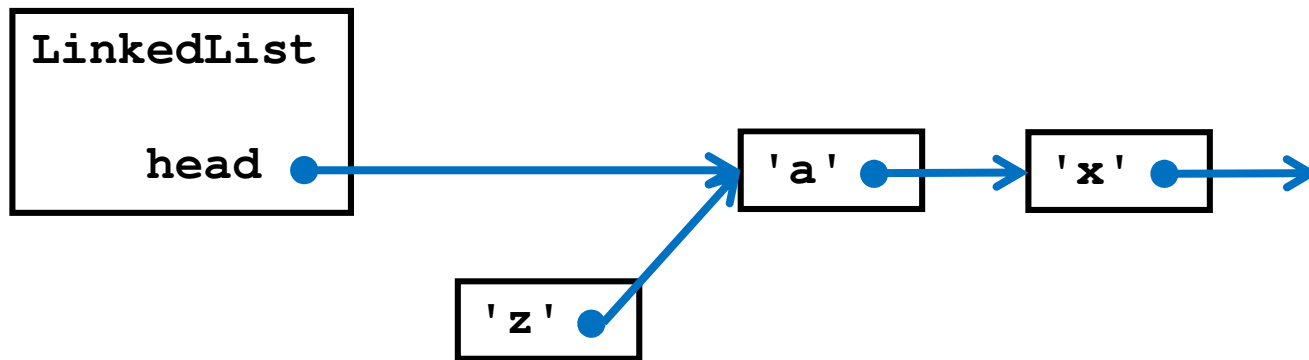


- ▶ `t.addFirst('z')` or `t.add(0, 'z')`

# Adding to the front of the list

---

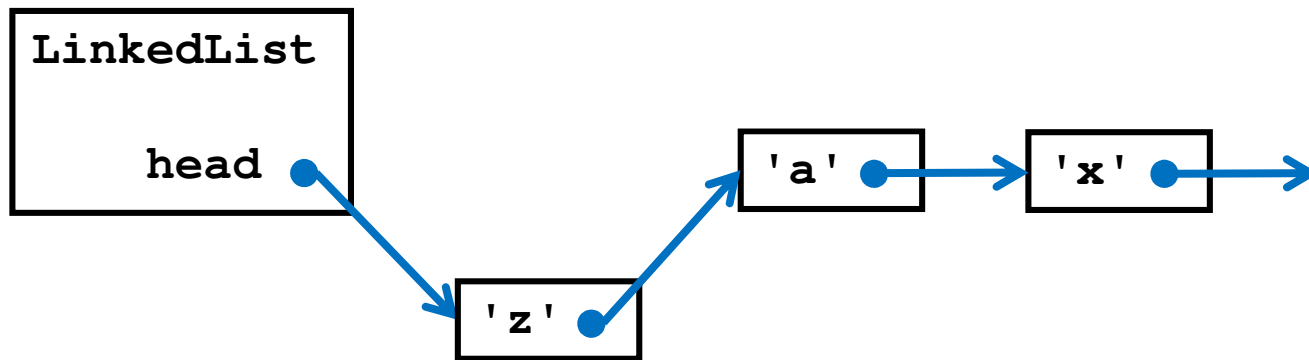
- ▶ must connect to the rest of the list



# Adding to the front of the list

---

- ▶ then re-assign head of linked list

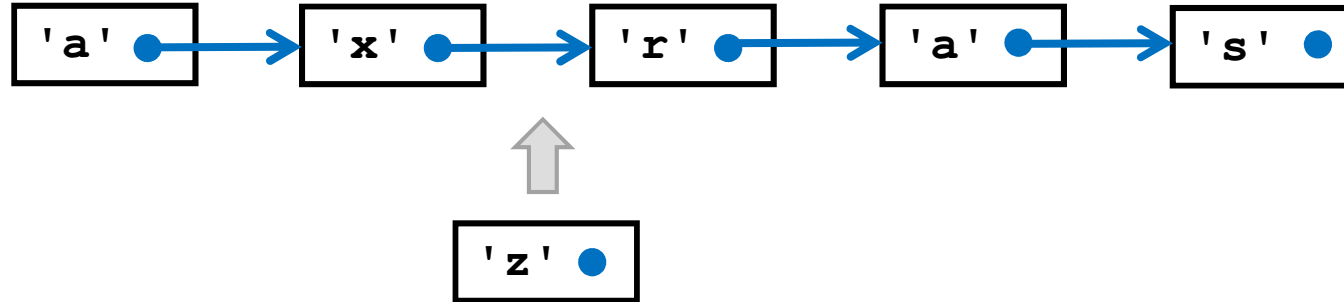


```
/**
 * Inserts the specified element at the beginning of this list.
 *
 * @param c the character to add to the beginning of this list.
 */
public void addFirst(char c) {
    Node newNode = new Node(c);
    newNode.next = this.head;
    this.head = newNode;
    this.size++;
}
```

# Adding to the middle of the list

---

- ▶ adding to the middle of the list

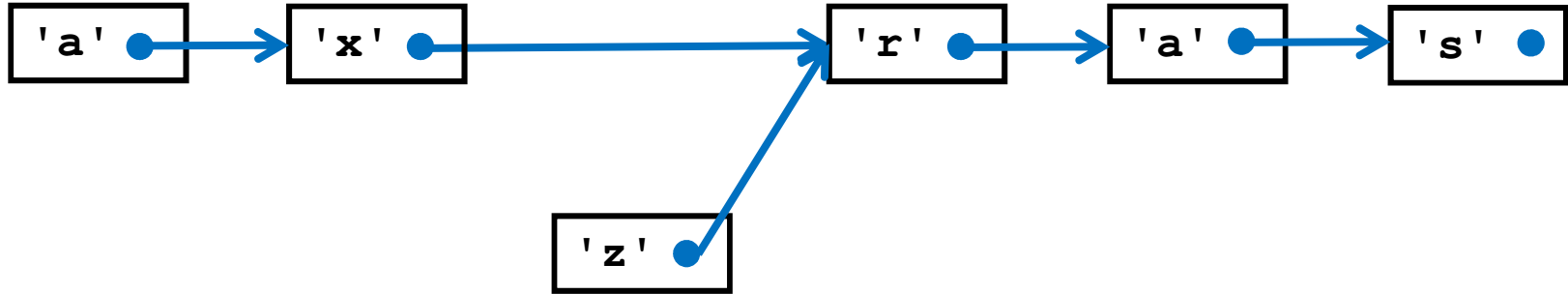


- ▶ `t.add(2, 'z')`

# Adding to the middle of the list

---

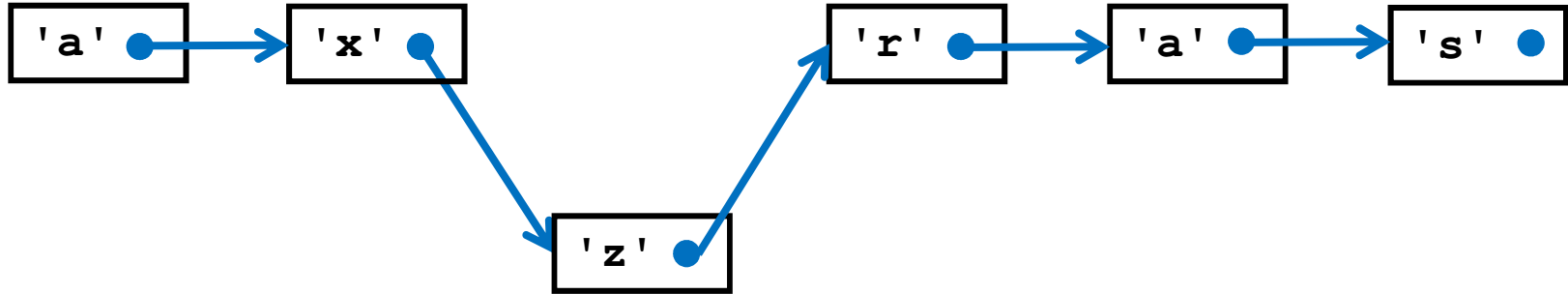
- ▶ must connect to the rest of the list



# Adding to the middle of the list

---

- ▶ then re-assign the link from the previous node



- ▶ notice that we to know the node previous to the inserted node

```
/**
 * Insert an element at the specified index in the list.
 *
 * @param index the index to insert at
 * @param c the character to insert
 */
public void add(int index, char c) {
    if (index < 0 || index > this.size) {
        throw new IndexOutOfBoundsException("Index: " + index + ", Size: "
            + this.size);
    }
    if (index == 0) {
        this.addFirst(c);
    }
    else {
        LinkedList.add(index - 1, c, this.head);
        this.size++;
    }
}
```

recursive method

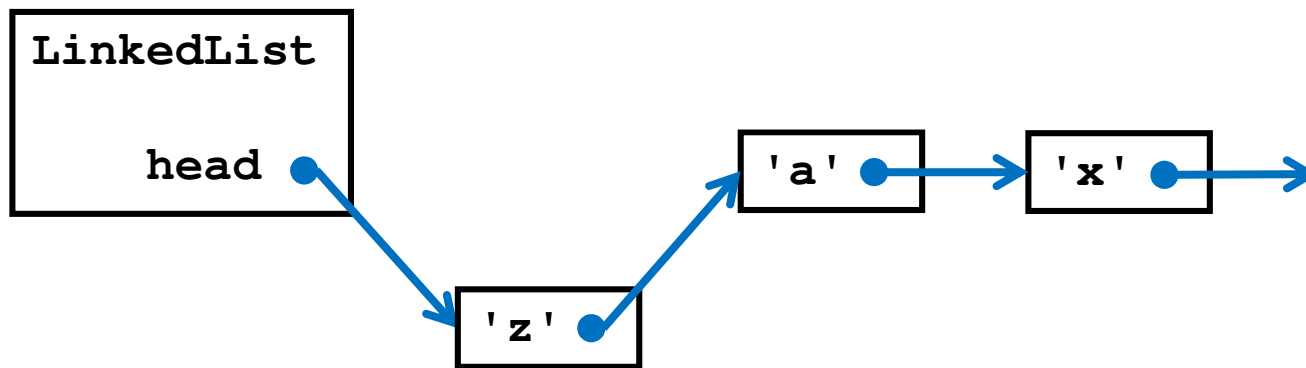


```
/**
 * Insert an element at the specified index after the
 * specified node.
 *
 * @param index the index after prev to insert at
 * @param c the character to insert
 * @param prev the node to insert after
 */
private static void add(int index, char c, Node prev) {
    if (index == 0) {
        Node newNode = new Node(c);
        newNode.next = prev.next;
        prev.next = newNode;
        return;
    }
    LinkedList.add(index - 1, c, prev.next);
}
```

# Removing from the front of the list

---

- ▶ removing from the front of the list

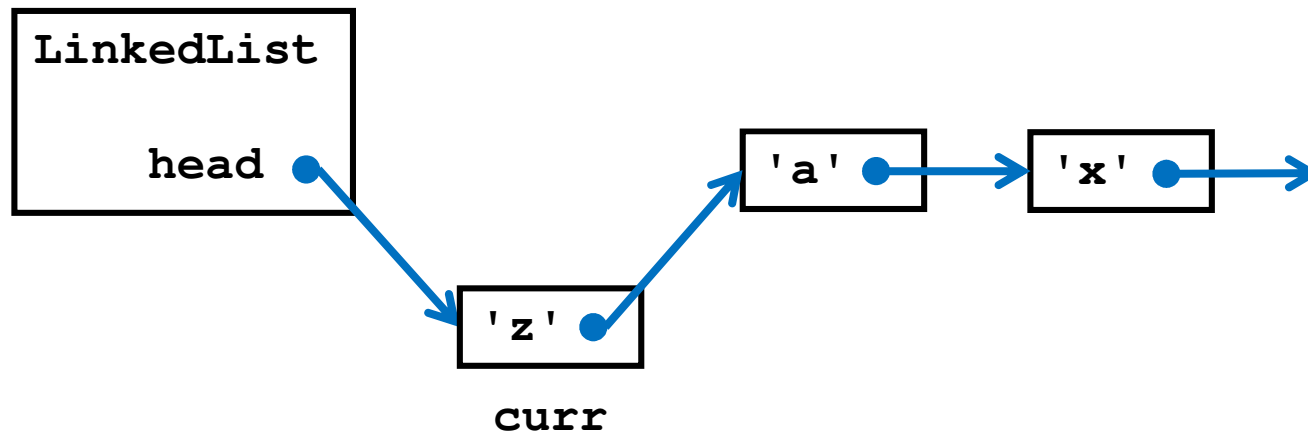


- ▶ `t.removeFirst()` or `t.remove(0)`
- ▶ also returns the element removed

# Removing from the front of the list

---

- ▶ create a reference to the node we want to remove

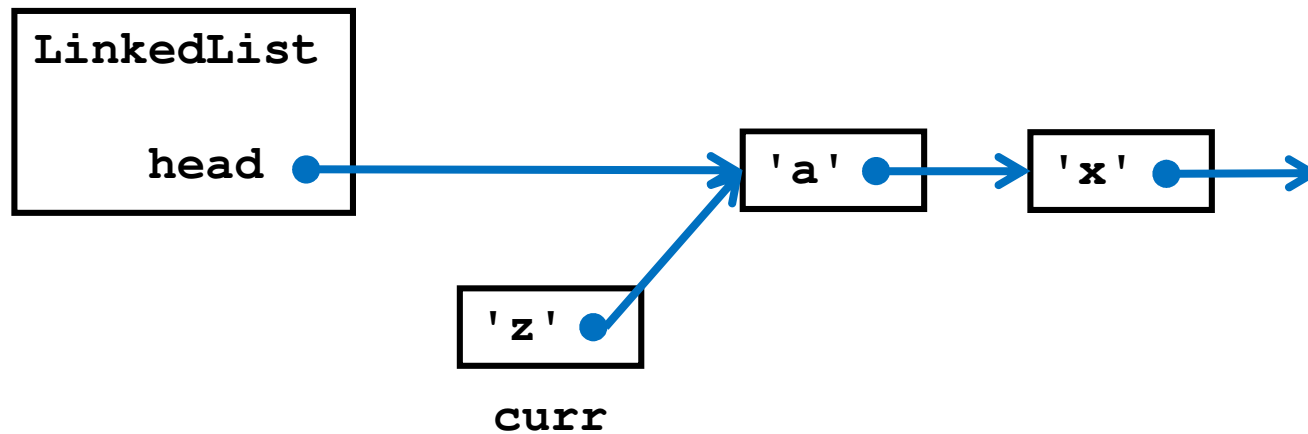


```
Node curr = this.head;
```

# Removing from the front of the list

---

- ▶ re-assign the head node

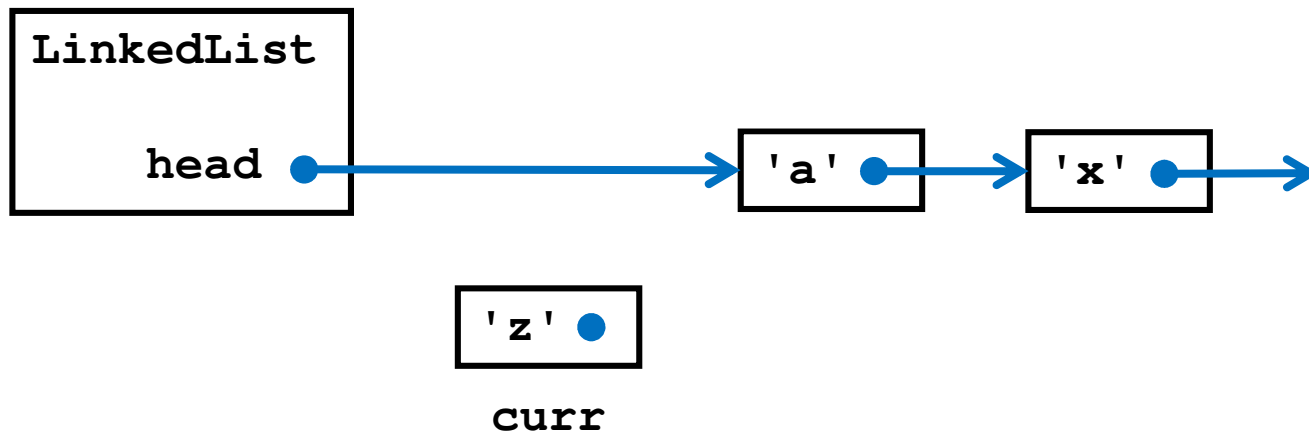


```
this.head = curr.next;
```

# Removing from the front of the list

---

- ▶ then remove the link from the old head node



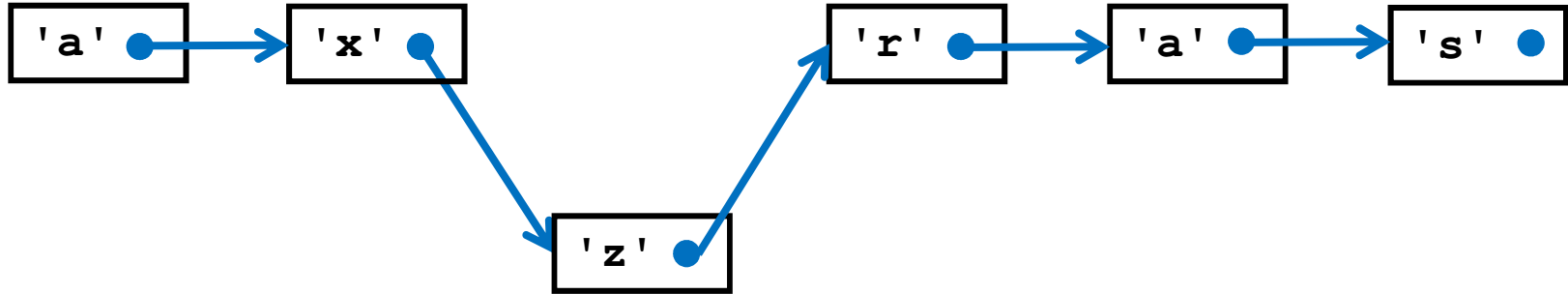
```
curr.next = null;
```

```
/**
 * Removes and returns the first element from this list.
 *
 * @return the first element from this list
 */
public char removeFirst() {
    if (this.size == 0) {
        throw new NoSuchElementException();
    }
    Node curr = this.head;
    this.head = curr.next;
    curr.next = null;
    this.size--;
    return curr.data;
}
```

# Removing from the middle of the list

---

- ▶ removing from the middle of the list

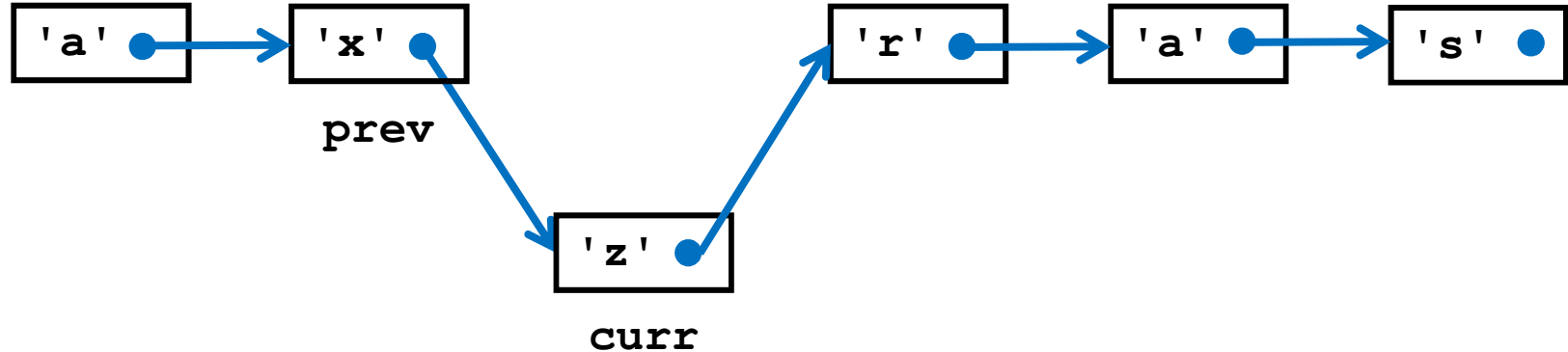


- ▶ `t.remove(2)`

# Removing from the middle of the list

---

- ▶ assume that we have references to the node we want to remove and its previous node

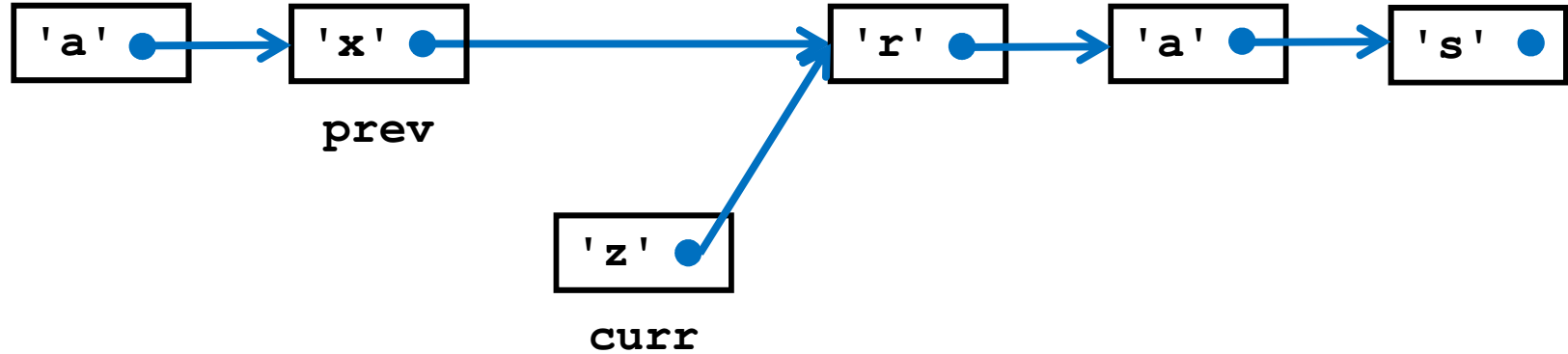




# Removing from the middle of the list

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- ▶ re-assign the link from the previous node

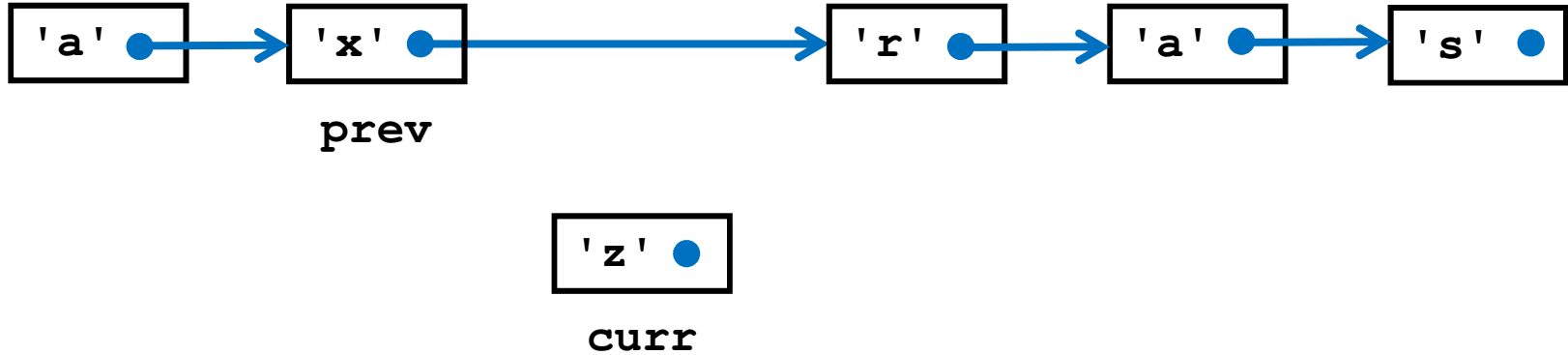


```
prev.next = curr.next;
```

# Removing from the middle of the list

---

- ▶ then remove the link from the current node



```
curr.next = null;
```

```
/**
 * Removes the element at the specified position in this list
 *
 * @param index the index of the element to be removed
 * @return the element previously at the specified position
 */
public char remove(int index) {
    if (index < 0 || index >= this.size) {
        throw new IndexOutOfBoundsException("Index: " + index +
                                           ", Size: " + this.size);
    }
    if (index == 0) {
        return this.removeFirst();
    }
    else {
        char result = LinkedList.remove(index - 1, this.head, this.head.next);
        this.size--;
        return result;
    }
}
```

**recursive method**

```

/**
 * Removes the element at the specified position relative to the
 * current node.
 *
 * @param index
 *         the index relative to the current node of the
 *         element to be removed
 * @param prev
 *         the node previous to the current node
 * @param curr
 *         the current node
 * @return the element previously at the specified position
 */
private static char remove(int index, Node prev, Node curr) {
    if (index == 0) {
        prev.next = curr.next;
        curr.next = null;
        return curr.data;
    }
    return LinkedList.remove(index - 1, curr, curr.next);
}

```

# Implementing Iterable

---

- ▶ having our linked list implement **Iterable** would be very convenient for clients

```
// for some LinkedList t

for (Character c : t) {
    // do something with c
}
```

# Iterable Interface

---

```
public interface Iterable<T>
```

Implementing this interface allows an object to be the target of the "foreach" statement.

```
Iterator<T>
```

```
iterator ()
```

Returns an iterator over a set of elements of type **T**.

# Iterator

---

- ▶ to implement **Iterable** we need to provide an iterator object that can iterate over the elements in the list

```
public interface Iterator<E>
```

An iterator over a collection.

```
boolean
```

```
hasNext ()
```

Returns true if the iteration has more elements.

```
E
```

```
next ()
```

Returns the next element in the iteration.

```
void
```

```
remove ()
```

Removes from the underlying collection the last element returned by this iterator (optional operation).

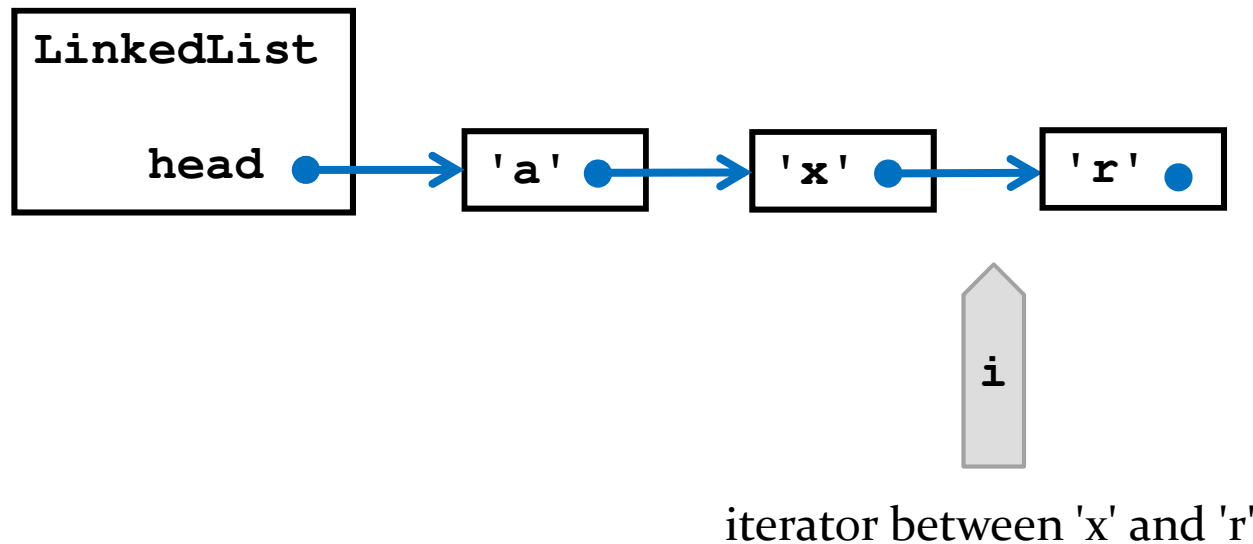
# Recursive Objects (Part 3)



# LinkedList Iterator

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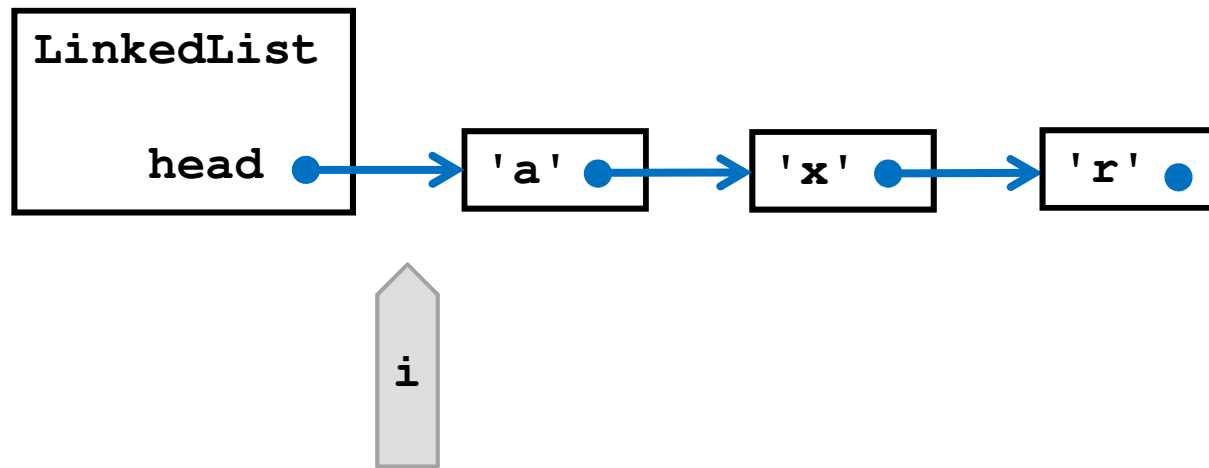
- ▶ think of the iterator as lying between elements in the list (like a cursor)



# LinkedList Iterator

---

- ▶ think of the iterator as lying between elements in the list (like a cursor)

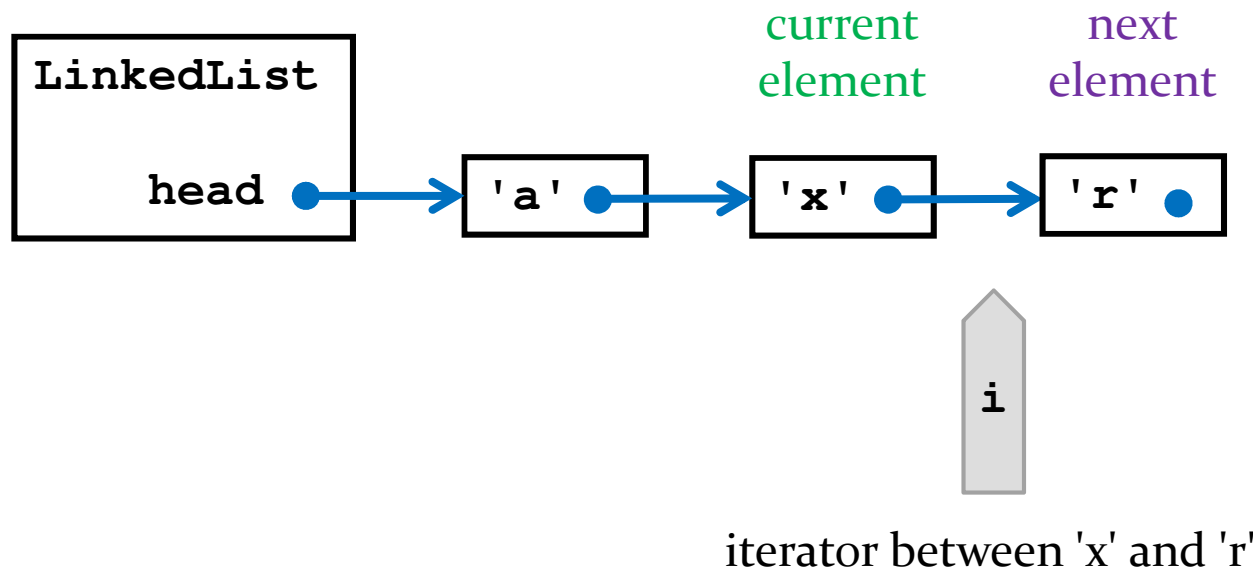


iterator at the start of the iteration  
(between nothing and 'a')

# LinkedList Iterator

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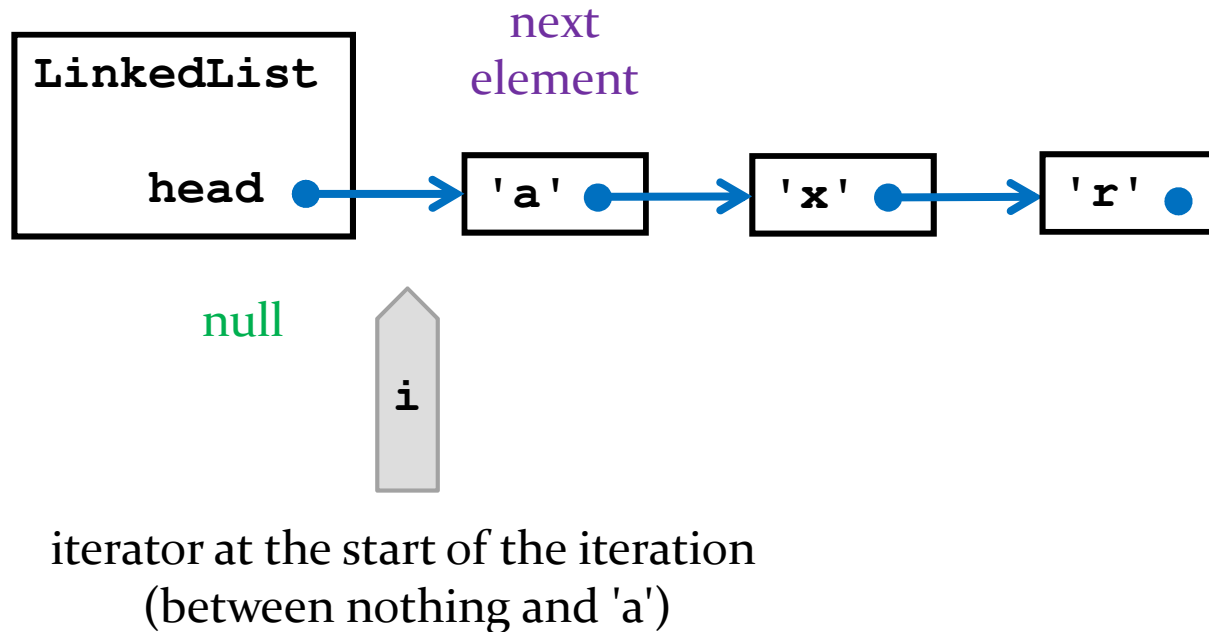
- ▶ because the iterator is between elements, there is a current element and next element of the iteration



# LinkedList Iterator

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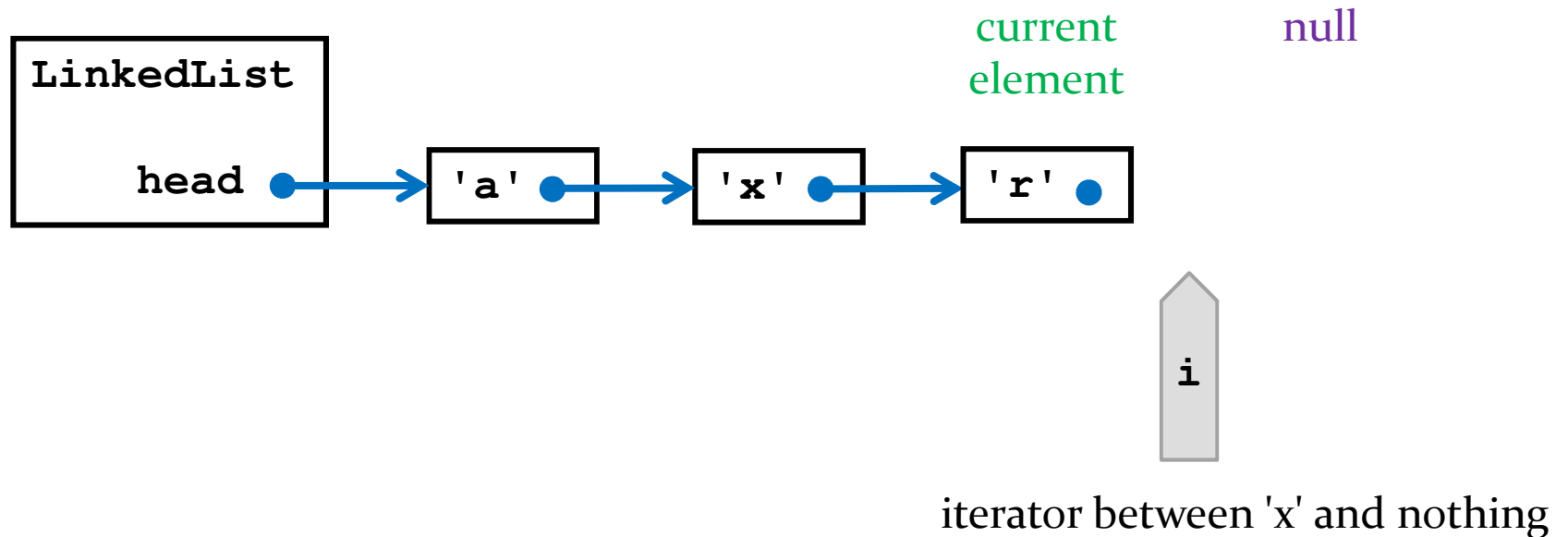
- ▶ the current element is `null` at the start of the iteration



# LinkedList Iterator

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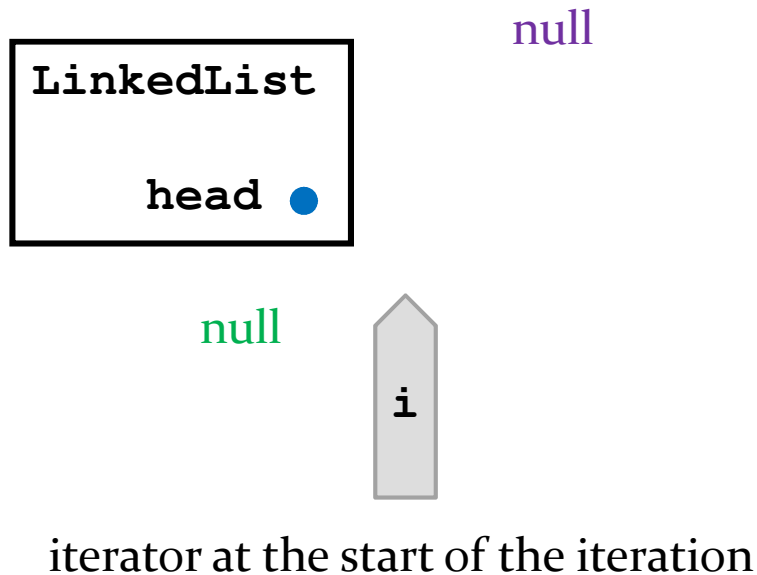
- ▶ the next element is `null` at the end of the iteration



# LinkedList Iterator

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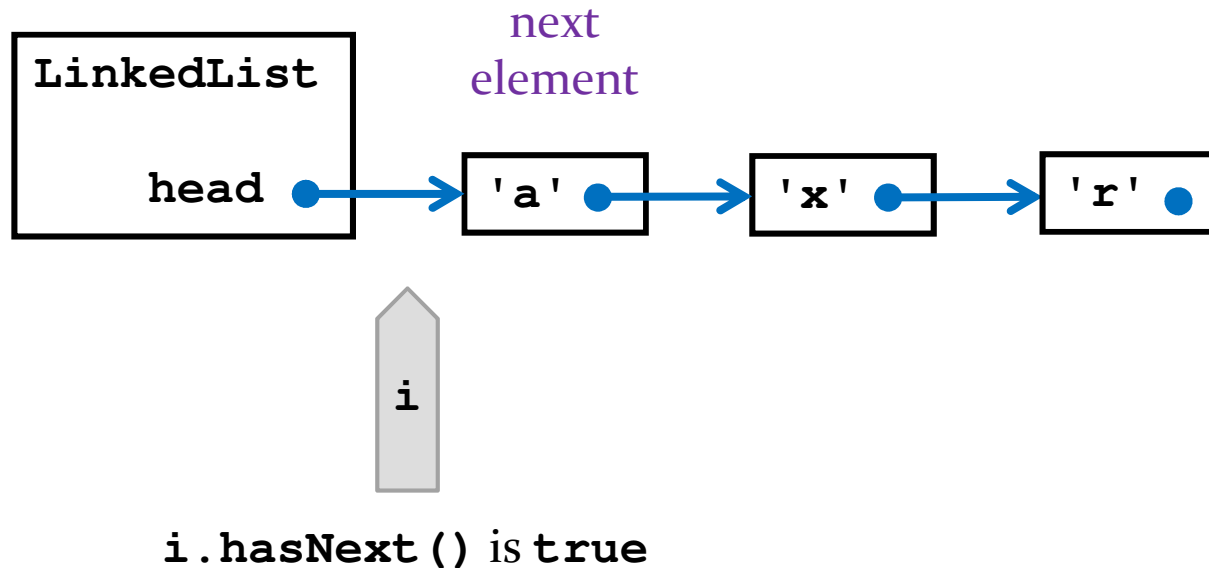
- ▶ both the current and next elements are **null** if the list is empty



# LinkedList Iterator: hasNext

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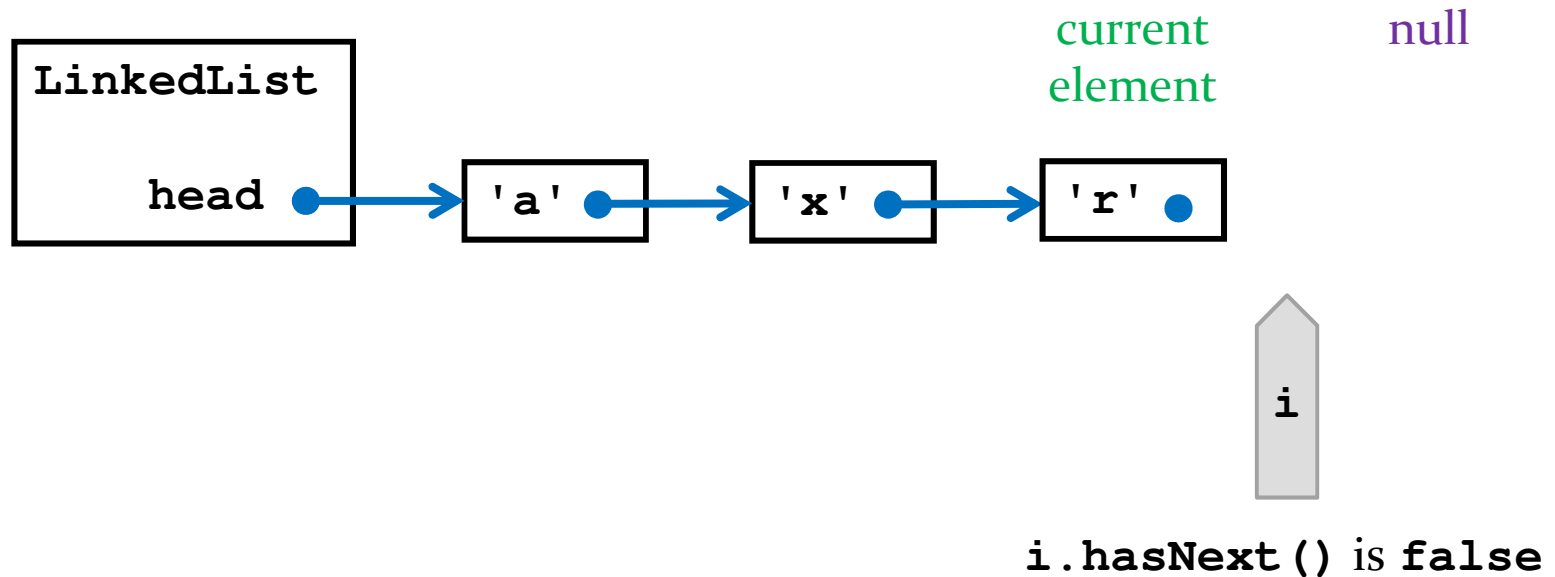
- ▶ **hasNext ()** returns true if there is at least one more element in the iteration



# LinkedList Iterator: hasNext

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- ▶ `hasNext ()` returns false at the end of the iteration

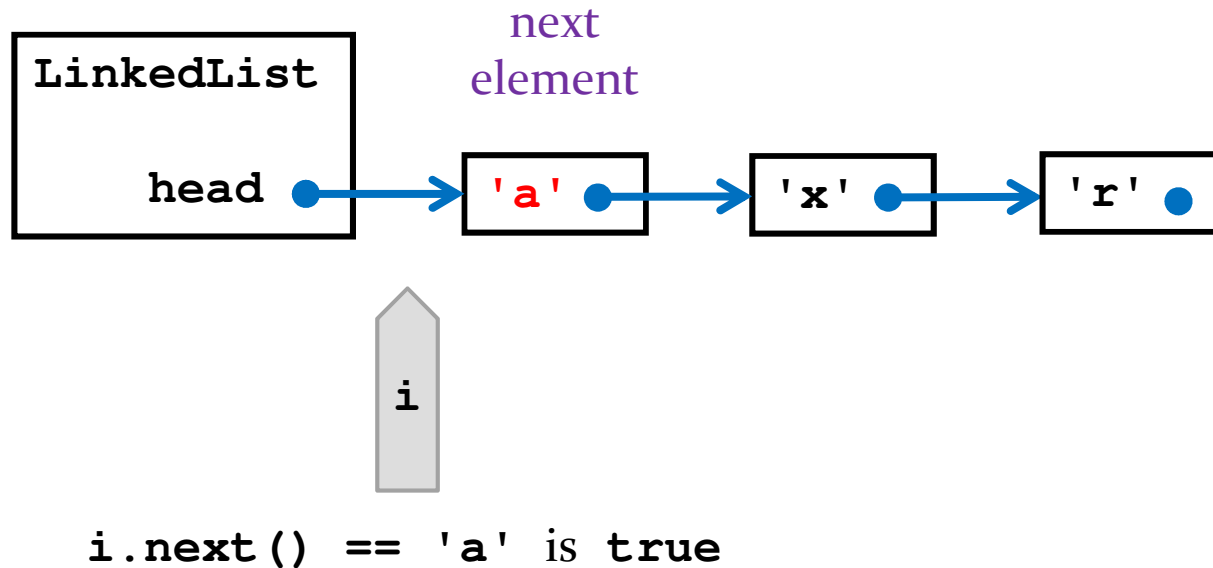




# LinkedList Iterator: next

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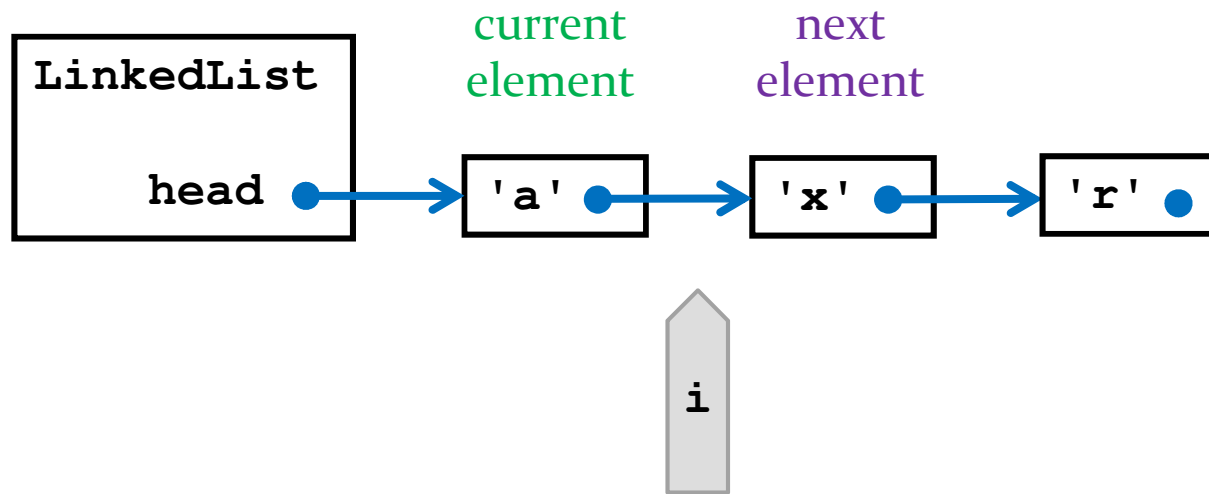
- ▶ invoking `next ()` returns the next element...



# LinkedList Iterator: next

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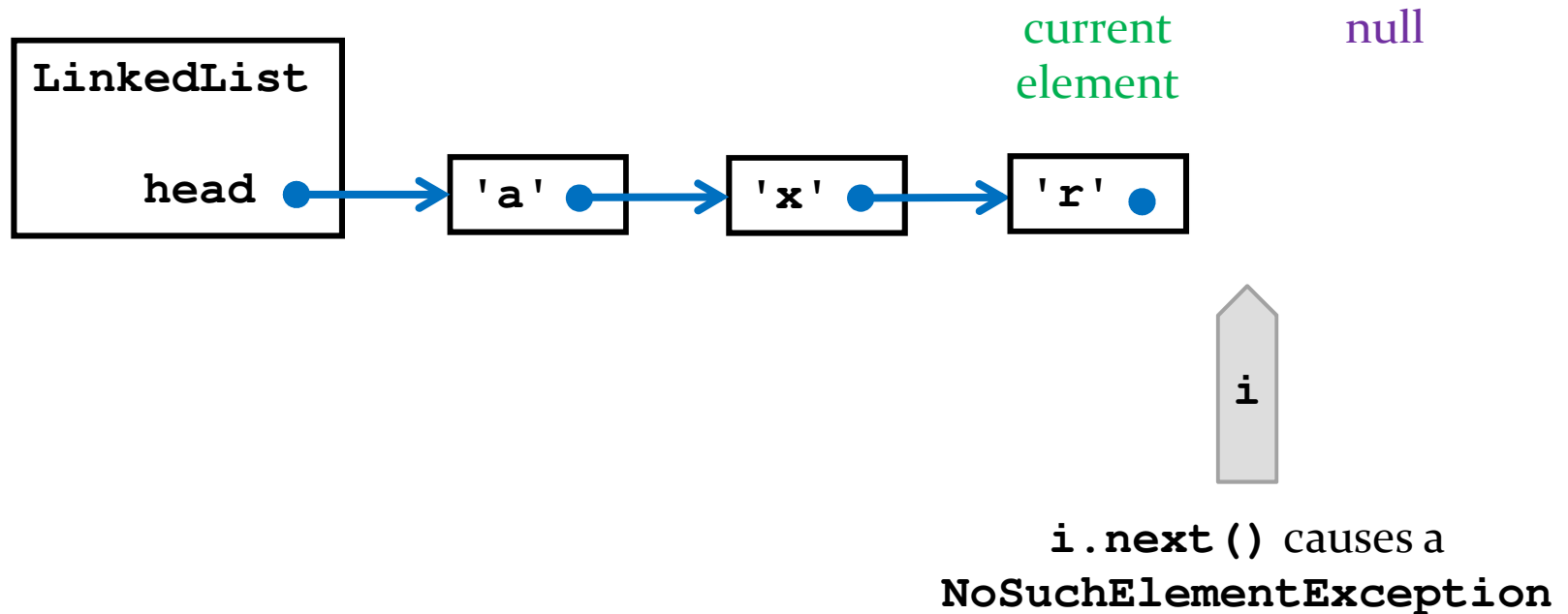
- ▶ and causes the iterator to move to its next position in the iteration



# LinkedList Iterator: next

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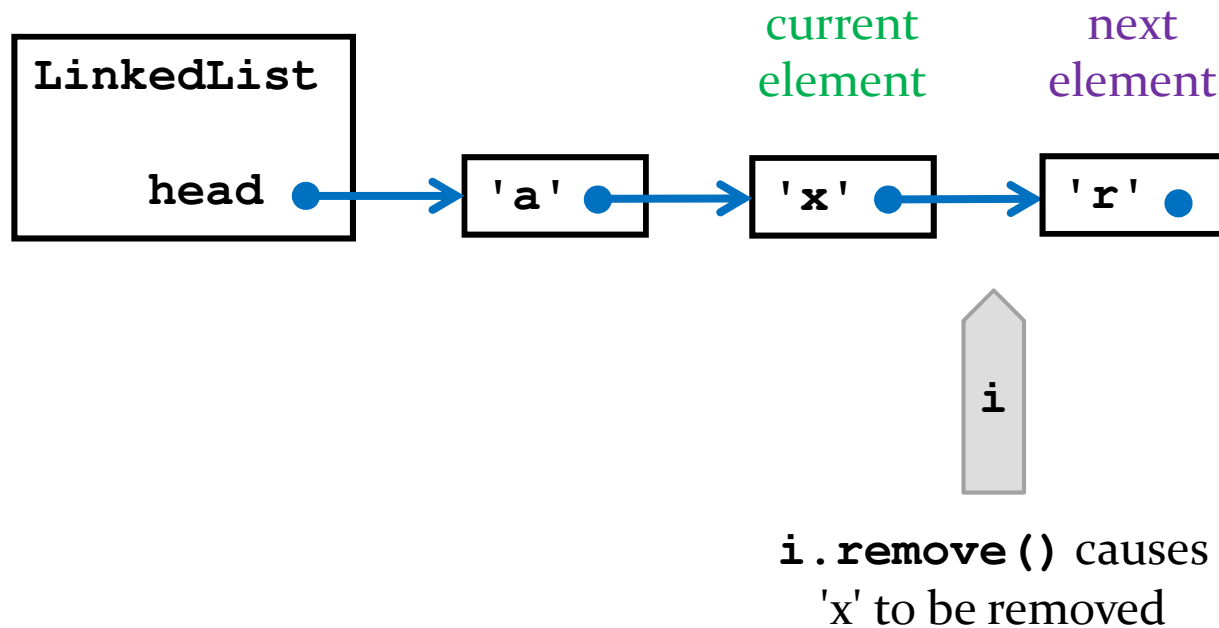
- ▶ invoking `next ()` at the end of the iteration causes a `NoSuchElementException` to be thrown



# LinkedList Iterator: remove

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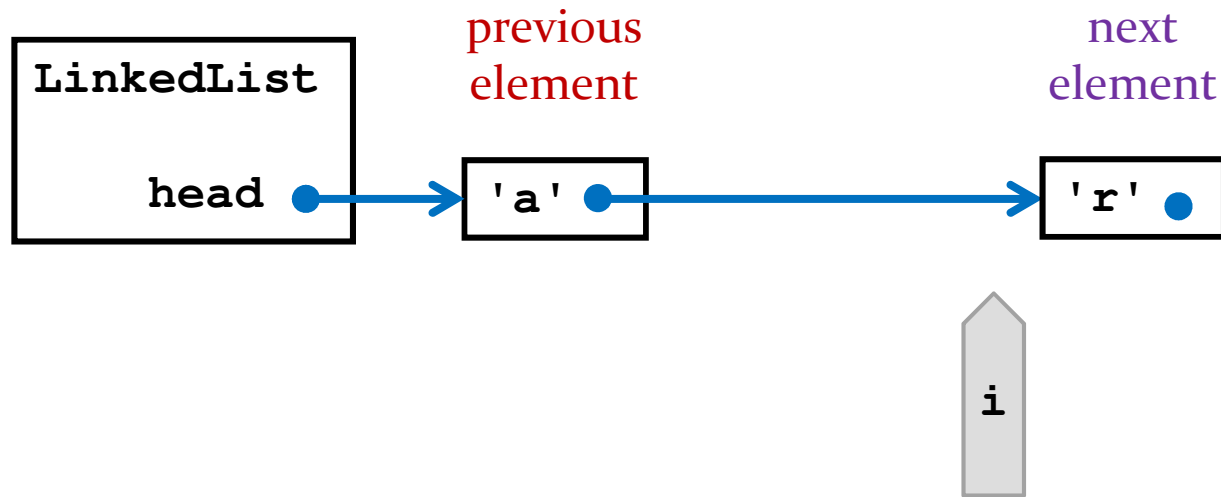
- ▶ **remove ()** causes the element most recently returned by **next ()** to be removed from the linked list



# LinkedList Iterator: remove

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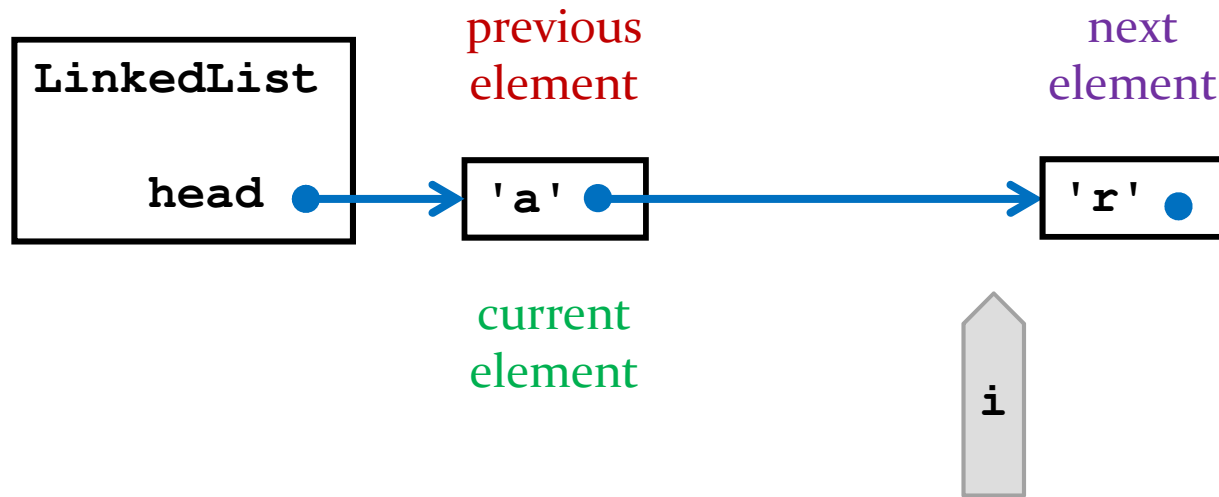
- ▶ notice that the iterator needs to know what was the previous element of the iteration



# LinkedList Iterator: remove

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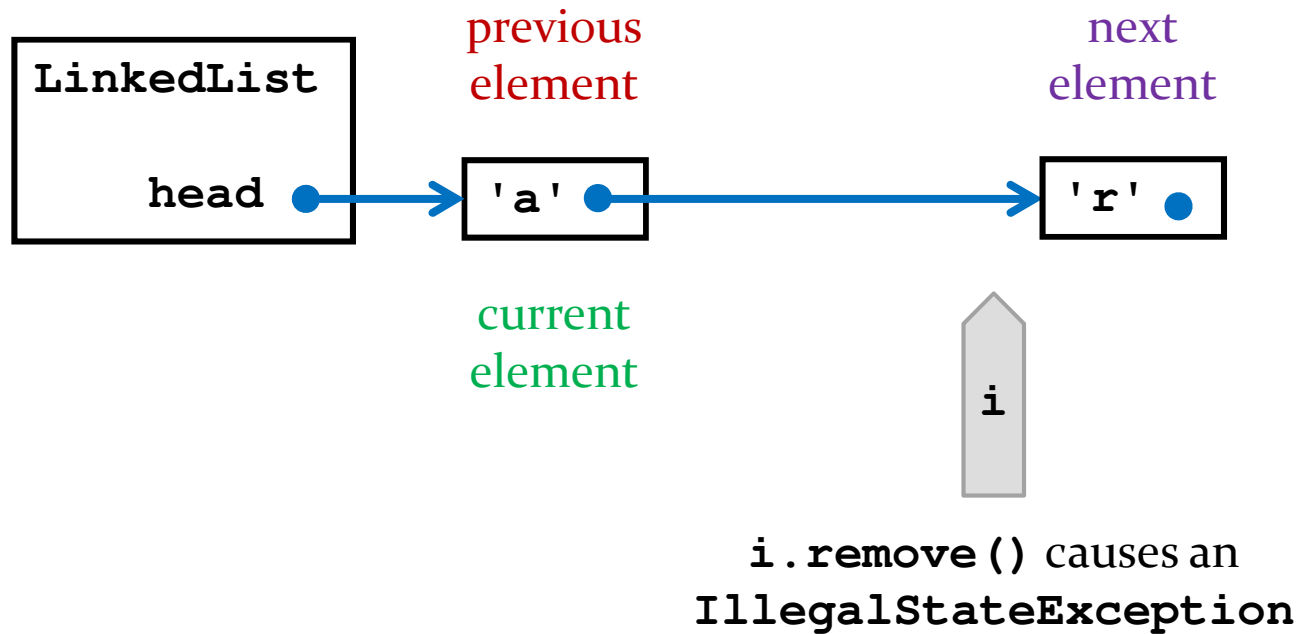
- ▶ after removing the element the current element and previous element are the same



# LinkedList Iterator: remove

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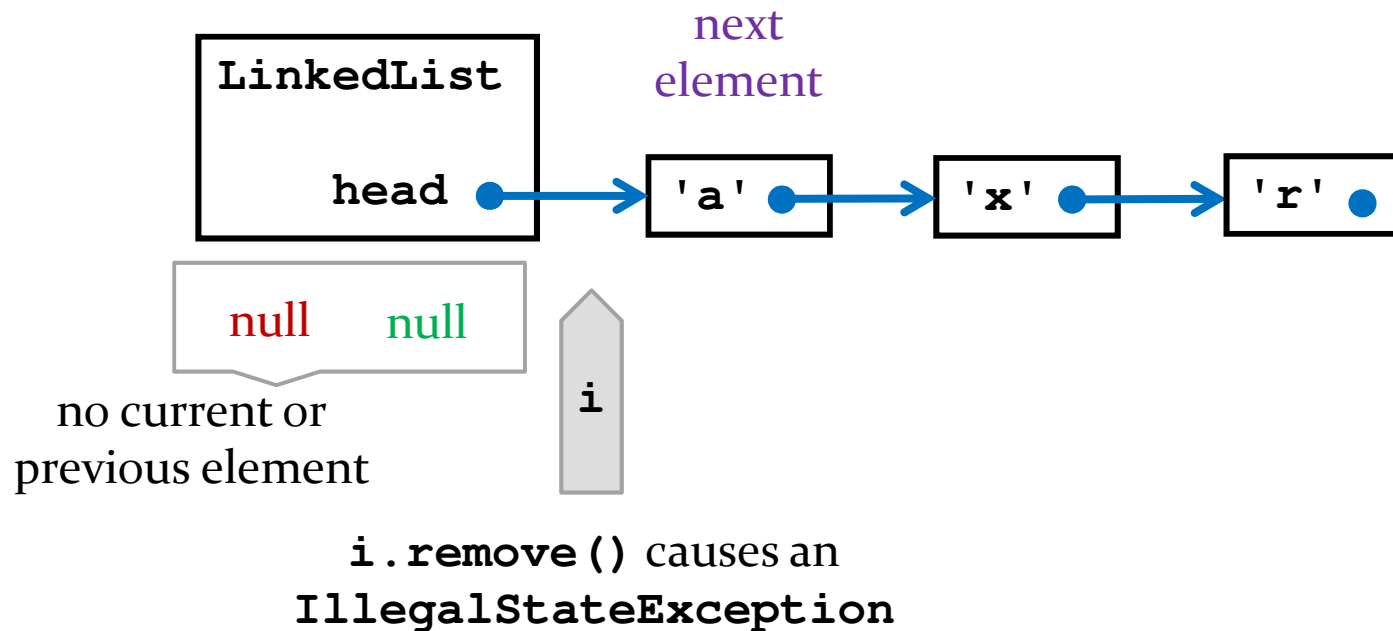
- ▶ invoking `remove ()` a second time causes an `IllegalStateException` to be thrown



# LinkedList Iterator: remove

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- ▶ invoking `remove ()` before calling `next ()` also causes and `IllegalStateException` to be thrown





# LinkedList Iterator: remove

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- ▶ note that using an iterator and **remove ()** is the safest way to iterate over a collection and selectively remove elements from the collection
  - ▶ called filtering

# LinkedList Iterator: remove

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```
// removes vowels from our LinkedList t

for (Iterator<Character> i = t.iterator();
     i.hasNext(); ) {
    char c = i.next();
    if (String.valueOf(c).matches("[aeiou]")) {
        System.out.println("removing " + c);
        i.remove();
    }
}
```

# Implementation

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- ▶ **currNode**

- ▶ reference to the node most recently returned by **next ()**
  - ▶ this means that **currNode** is **null** at the start of the iteration
    - requires special treatment in methods

- ▶ **prevNode**

- ▶ reference to the node previous to **currNode**
  - ▶ needed for **remove ()**

# Implementation: Attributes and Ctor

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```
private class LinkedListIterator implements
    Iterator<Character> {

    private Node currNode;
    private Node prevNode;

    public LinkedListIterator() {
        this.currNode = null;
        this.prevNode = null;
    }
}
```

# Implementation: hasNext

---

```
@Override
public boolean hasNext() {
    if (this.currNode == null) {
        return head != null;
    }
    return this.currNode.next != null;
}
```

# Implementation: next

---

```
@Override
public Character next() {
    if (!this.hasNext()) {
        throw new NoSuchElementException();
    }
    this.prevNode = this.currNode;
    if (this.currNode == null) {
        this.currNode = head;
    }
    else {
        this.currNode = this.currNode.next;
    }
    return this.currNode.data;
}
```

# Implementation: remove

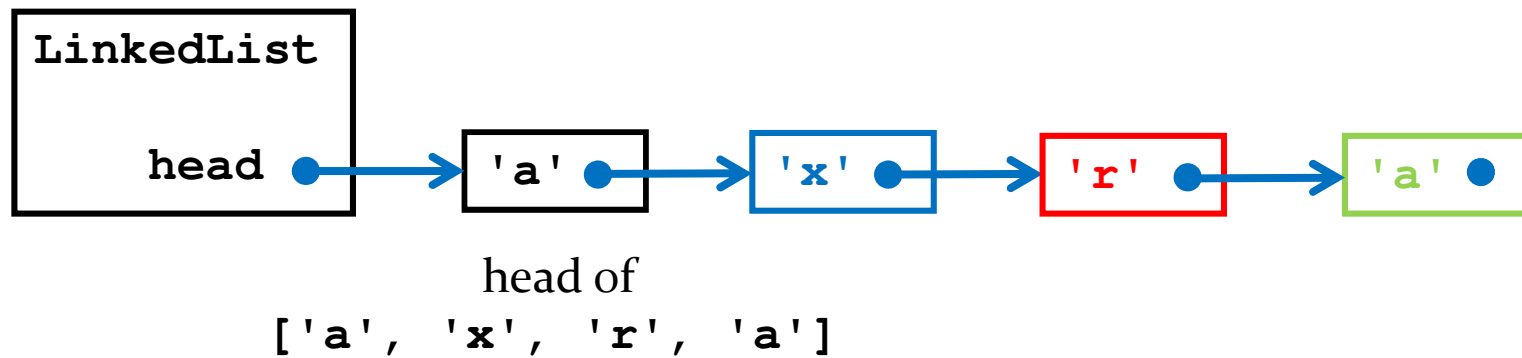
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```
@Override
public void remove() {
    if (this.prevNode == this.currNode) {
        throw new IllegalStateException();
    }
    if (this.currNode == head) {
        head = this.currNode.next;
    }
    else {
        this.prevNode.next = this.currNode.next;
    }
    this.currNode = this.prevNode;
    size--;
}
```

# LinkedList Summary

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- ▶ each node can be thought of as the head of a smaller list

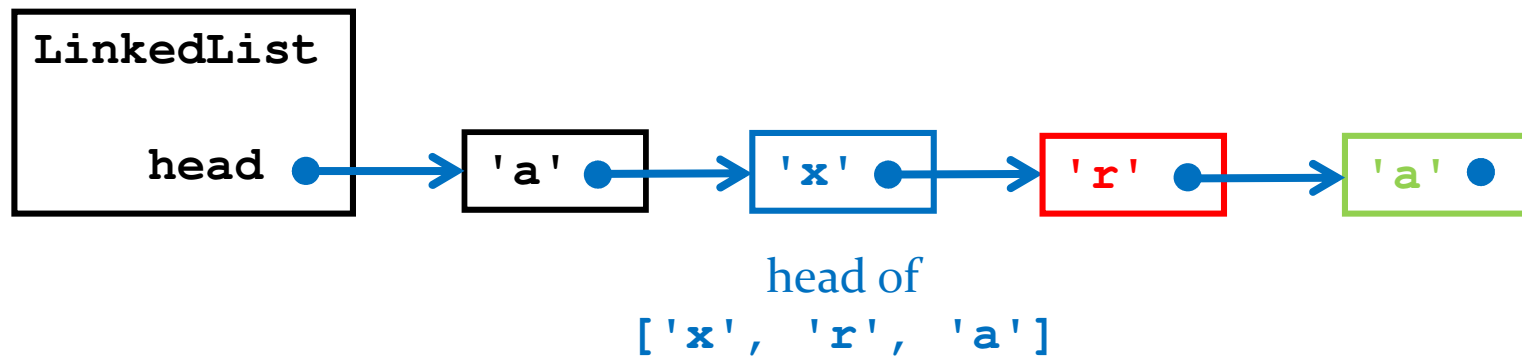




# LinkedList Summary

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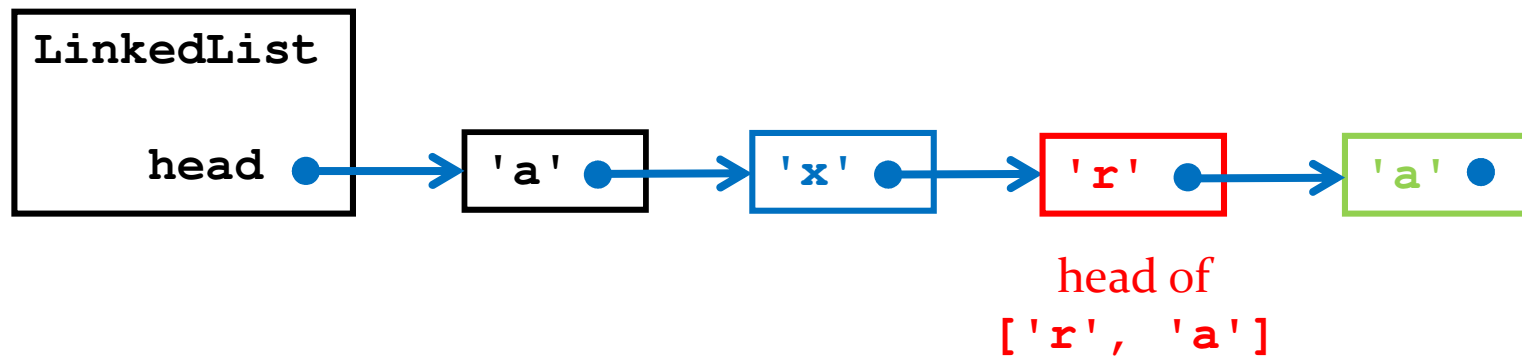
- ▶ each node can be thought of as the head of a smaller list



# LinkedList Summary

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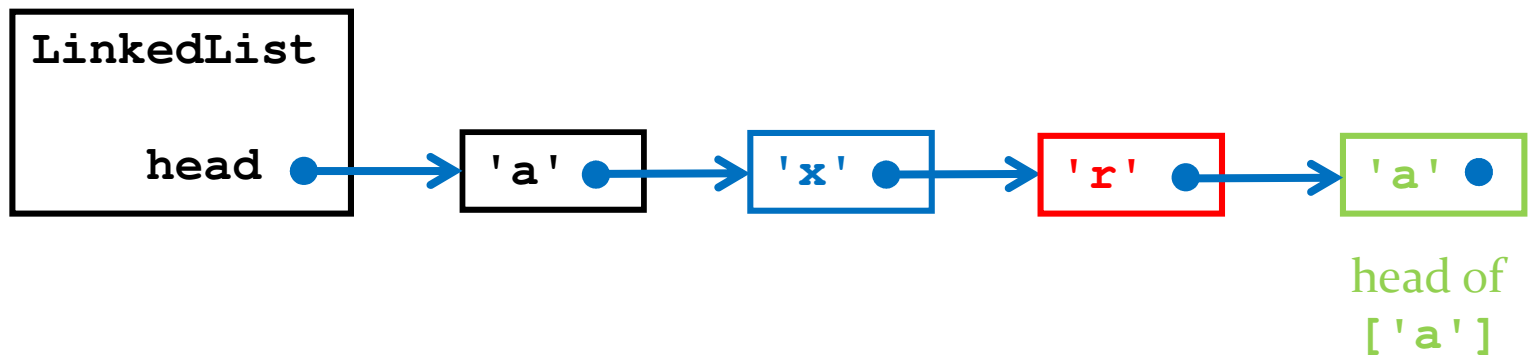
- ▶ each node can be thought of as the head of a smaller list



# LinkedList Summary

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- ▶ each node can be thought of as the head of a smaller list



# LinkedList Summary

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- ▶ the recursive structure of the linked list leads to recursive algorithms that operate on the list

```
private static boolean contains(char c, Node node) {
    if (node.data == c) {
        return true;
    }
    if (node.next == null) {
        return false;
    }
    return LinkedList.contains(c, node.next);
}
```

# LinkedList Summary

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- ▶ nodes are an implementation detail
  - ▶ the client only cares about the elements (characters) in the list
- ▶ **Node** is implemented as a private static inner class
  - ▶ private so that only **LinkedList** can use it
  - ▶ static because **Node** does not need access to any non-static attribute of **LinkedList**

# LinkedList Summary

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- ▶ by implementing the **Iterable** interface we give clients the ability to iterate over the elements of the list
- ▶ clients expect to be able to do this for most collections

```
// for some LinkedList t

for (Character c : t) {
    // do something with c
}
```

# LinkedList Summary

---

- ▶ to implement **Iterable** we need to provide an iterator object that can iterate over the elements in the list

```
public interface Iterator<E>
```

An iterator over a collection.

```
boolean
```

```
hasNext ()
```

Returns true if the iteration has more elements.

```
E
```

```
next ()
```

Returns the next element in the iteration.

```
void
```

```
remove ()
```

Removes from the underlying collection the last element returned by this iterator (optional operation).