## CSE4421: Lab 3

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Note: I will check your answers for steps 1 and 3 if you ask.

- 1. Derive the table of Denavit-Hartenberg (DH) parameters for the A150 robot using the frame placements shown in Figure 1. Links 1–3 all have a length of 10 inches. Link 4 can be treated as a link of length 0 inches. The distance between  $o_4$  and  $o_5$  is 2 inches.
- 2. Implement a Matlab function that computes the Denavit-Hartenberg transformation matrix given vectors of DH values a,  $\alpha$ , d, and  $\theta$ . The function signature should be:

function T = dh(a, alpha, d, theta)

You can check that your function gives results that are consistent with the A150 simulator by plugging in appropriate DH values for the A150 arm.

- 3. Derive the analytic form of the matrix  $T_5^3$ ; i.e., derive the elements of the  $4 \times 4$  matrix.
- 4. Solve the inverse kinematics problem for the wrist; i.e., given  $T_5^3$  solve for the values of  $\theta_4$  and  $\theta_5$ . Implement a Matlab function that computes the inverse kinematics of the wrist. The function signature should be:

function theta45 = invwrist(T35)

where theta45 is the vector  $[\theta_4 \ \theta_5]$  and T35 is the matrix  $T_5^3$ .

5. Implement a Matlab function that finds the location of  $o_c^0$ , the wrist center relative to frame  $\{0\}$ , given  $T_5^0$ , the pose of frame  $\{5\}$  relative to frame  $\{0\}$ . The function signature should be:

function oc = wristcenter(T05)

where oc is the wrist center location  $o_c^0$  and T05 is the matrix  $T_5^0$ .

Submit your Matlab files using the command

submit 4421 L3 dh.m invwrist.m wristcenter.m



Figure 1: Denavit-Hartenberg frame placement for the A150 and A255 robots.

Joint variable	Range
$ heta_1$	$-175^\circ$ to $175^\circ$
$ heta_2$	$0^{\circ}$ to $110^{\circ}$
$ heta_3$	$-130^\circ$ to $0^\circ$
$ heta_4$	$-110^{\circ}$ to $110^{\circ}$
$ heta_5$	$-180^\circ$ to $180^\circ$

Table 1: The joint variable ranges in the Denavit-Hartenberg convention.