

# Summary of last lecture

- Some facts on logic
- Representing functions as input/output lists/tables, decision problems and languages
- Computing devices solving problems by accepting (recognizing) languages

# Comparison of computation models

- We would like to claim “Model A can compute function every function B can, and further it can compute a function  $f$ , but model B cannot” which would imply model A is strictly more powerful than B.
- What we will (typically) prove is “Model A accepts every language model B accepts and in addition a language  $L$  that model B cannot accept”

# Proof by contradiction - 2

## The Pigeonhole Principle

- If  $n+1$  or more objects are placed into  $n$  boxes, then there is at least one box containing two or more of the objects

In a set of any 27 English words, at least two words must start with the same letter

- If  $n$  objects are placed into  $k$  boxes, then there is at least one box containing  $\lceil n/k \rceil$  objects

# Recursively defined sets

Close relationship to induction

Example: set of all palindromes

- $\varepsilon \in P; \forall a \in \Sigma, a \in P;$
- $\forall a \in \Sigma \forall x \in P, axa \in P$
- No other strings are in  $P$

# More definitions

Definition of  $\Sigma^*$ :

- $\varepsilon \in \Sigma^*$ ;
- $\forall a \in \Sigma, \forall x \in \Sigma^*, xa \in \Sigma^*$ ;
- No other strings are in  $\Sigma^*$ .

# Exercise

Suppose  $\Sigma = \{a,b\}$ . Define  $L$  as

- $a \in L$ ;
  - $\forall x \in L, ax \in L$
  - $\forall x, y \in L, bxy, xby$  and  $xyb$  are in  $L$
  - No other strings are in  $P$
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- Prove that this is the language of strings with more a's than b's.