

Example programs

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Overview

- Classifying terms
 - Weight Conversion
- Working with Lists
- Working with Structures
 - Board Example
- Linked Lists
- Binary Trees

[ref.: Clocksin, Chap 6 & 7]

[also Prof. Zbigniew Stachniak's notes]

Weight conversion

- Problem:
 - Convert Pounds to Kilos and vice versa
 - Show an error message and fail if no inputs given
 - Show an error message and fail if given input is not a number

Some useful built-in predicates:

<i>var(X)</i>	succeeds if X is a variable and is not instantiated
<i>nonvar(X)</i>	succeeds if var(X) fails
<i>atom(X)</i>	succeeds if X stands for an atom e.g. adam, 'George', ...
<i>number(X)</i>	succeeds if X stands for a number
<i>atomic(X)</i>	succeeds if X stands for a number or an atom
<i>integer(X)</i>	Succeeds if X stands for an integer.

Weight Conversion- code

```
convert(Pounds, Kilos):-          % If no inputs given
    var(Pounds), var(Kilos), !,
    write('No inputs!'), nl, fail.

convert(Pounds, _):-              % If Pounds is known,
                                   but not a number
    nonvar(Pounds), \+number(Pounds), !,
    write('Inputs must be numbers!'), nl, fail.

convert(_, Kilos):-              % If Kilos is known,
                                   but not a number
    nonvar(Kilos), \+number(Kilos), !,
    write('Inputs must be numbers!'), nl, fail.

convert(Pounds, Kilos):- % If Pounds is known
    number(Pounds), !,
    Kilos is Pounds * 0.45359.

convert(Pounds, Kilos):-          % Otherwise
    Pounds is Kilos/0.45359.
```

Weight conversion- queries

```
?- convert(X,Y).
```

```
No inputs!  
false.
```

```
?- convert(20,Y).
```

```
Y = 9.0718.
```

```
?- convert(X,9).
```

```
X = 19.8417.
```

```
?- convert(20,9.0718).
```

```
true.
```

```
?- X=5, convert(X,Y).
```

```
X = 5,  
Y = 2.26795.
```

```
?- convert(X,a).
```

```
Inputs must be numbers!  
false.
```

Working with Lists

- Find the first element of a list.

```
first(X, [X|_]).
```

- Find the last element of a list.

```
last(X, [X]).
```

```
last(X, [H|T]) :- last(X, T).
```

- Shift the elements of a list to left.

```
lshift([H|T], L) :- append(T, [H], L).
```

```
?- lshift([1, 2, 3, 4, 5], L).
```

```
L = [2, 3, 4, 5, 1].
```

Working with Lists (2)

- Note:

```
?- lshift(L, [1, 2, 3, 4, 5]).
```

```
L = [5, 1, 2, 3, 4].
```

- Shift the elements of a list to the right.

```
rshift(L, R):- lshift(R, L).
```

- Shift the elements of a list to the right N times.

```
good(N):- integer(N), N >= 0.
```

```
rshift(L, N, R):-  
    \+good(N), !,  
    write('N must be a known positive integer.'),  
    nl, fail.
```

```
rshift(L, 0, L).
```

```
rshift(L, N, R):-  
    N>0,  
    rshift(L, R1), N1 is N-1, rshift(R1, N1, R).
```

Working with Lists (3)

- Change the N^{th} element of a list
 - Assuming we already checked for the possible errors (e.g. $N < 1$ or $N > \text{length of list}$)
 - *setPosition* ($L1, N, X, L2$) returns list $L2$ which is the same as list $L1$, except that its N^{th} element is changed to X .

?- setPosition([1, 2, 3, 4], 2, z, L).

$L = [1, z, 3, 4]$

setPosition([_|L], 1, X, [X|L]).

setPosition([H|L1], N, X, [H|L2]):-

$N > 1,$

$N1$ is $N-1,$

setPosition(L1, N1, X, L2).

See more examples of list processing in Clocksin, Section 7.5.

Board example:

Input a board position number

- Get an **integer** from 1 to 9 from user, set the corresponding board position to 'x'.

getXPosition(N):-

```
write('Enter a position (1-9): '),  
read(N),  
integer(N), N > 0, N <10, !.
```

getXPosition(N):- getXPosition(N).

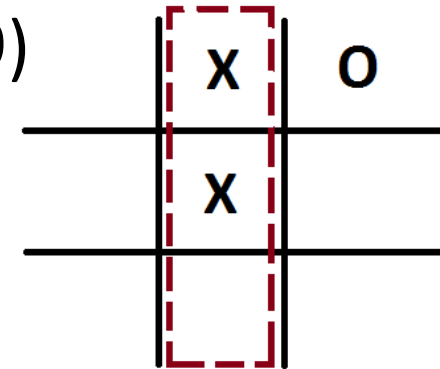
- or use **repeat**

getXPosition(N):-

```
repeat,  
write('Enter a position (1-9): '),  
read(N),  
integer(N), N > 0, N <10, !.
```

Working with structures

- The board is a structure $b(B1, B2, \dots, B9)$
For example, this board is shown as
 $b(e,x,o, e,x,e, e,e,e)$



- How can we access the components, especially if we don't know anything about the structure.
- Useful built-in predicates:

<i>functor(T, F, N)</i>	means "T is a structure with functor F and arity N".
<i>arg(N, T, A)</i>	Returns/ matches the N th argument of T in/ with A.
<i>T =.. L</i>	means "L is a list of functor of T and its arguments"

Working with structures- examples

```
?- functor(s(a,b,c), F, N).
```

```
F = s, N = 3.
```

```
?- functor(c, F, N).
```

```
F = c, N = 0.
```

```
?- functor(T, book, 2).
```

```
T = book(_G48, _G49).
```

```
?- arg(2, s(a,b,c), X).
```

```
X = b.
```

```
?- arg(2, [a, b, c], X).
```

```
X = [b, c].
```

```
?- s(a,b,c) =.. L.
```

```
L = [s, a, b, c].
```

```
?- s(a,b,c) =.. [H|L].
```

```
H = s, L = [a, b, c].
```

```
?- T =.. [g,1].
```

```
T = g(1).
```

```
?- [a, b, c] =.. [H|T].
```

```
H = `.', T = [a, [b,c]].
```

Board example: Set a board position

- Set a board position to X

```
setPosBoard(OldB, N, X, NewB) :-  
    OldB =.. [H|L1],  
    setPosition(L1, N, X, L2),  
    NewB =.. [H|L2].
```

- Ask the position from user and set that position to 'x'

```
nextX(OldB, NewB) :-  
    getXPosition(N),  
    setPosBoard(OldB, N, x, NewB).
```

Board example: Set a board position if available

- But we also have to make sure the board position is available

```
nextX(OldB, NewB):-  
    getXPosition(N),                % ask where to play  
    checkPosition(OldB, N),!,      % is it available  
    setPosBoard(OldB, N, x, NewB).  
                                     % set the board to x  
  
nextX(OldB, NewB):-                % else error message  
    write('Not an empty board position!'),  
    nl,  
    nextX(OldB, NewB).
```

Board example: Checking a position on board

- Is the board position containing an 'e'?
 - Reminder: we decided to have e in any empty position.

```
checkPosition(B, N) :-  
    arg(N, B, X),      % get position N on board  
    X = e.             % check if it is e
```

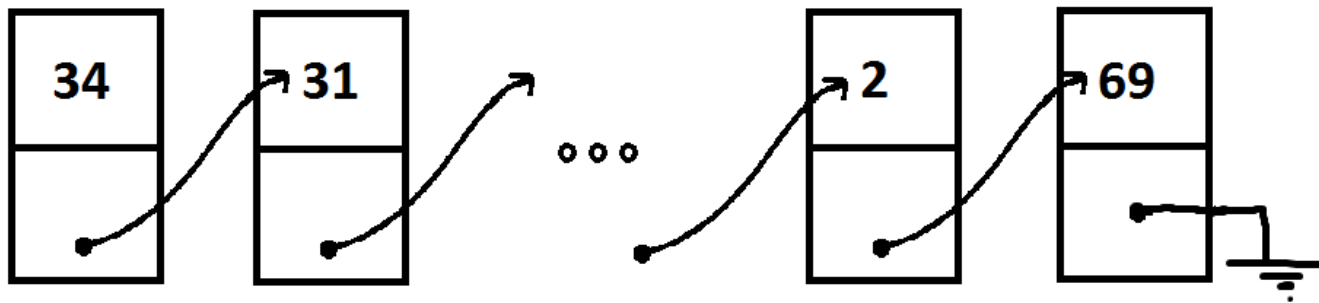
Linked Lists

- We can define linked lists as a structure with two arguments: data and link

```
l1ist(Data, Link)
```

```
l1ist(34, l1ist(31, ..., l1ist(2, l1ist(69, end)) ...))
```

- Used the constant 'end' to mark the end of the linked list.
- It is possible to have a more complicated Data, or more arguments for l1ist.



Linked Lists- search & insert

- Write *search(X, LL)* which succeeds if X is a data in a linked list LL.

```
search(_, end):- fail.
```

```
search(X, llist(X, _)).
```

```
search(X, llist(_,Rest)) :- search(X, Rest).
```

- Write *insert(X, LL1, LL2)* which inserts X in front of LL1 to get LL2.

```
insert(X, LL1, llist(X, LL1)).
```

- Exercise:
 - write *delete(X, LL1, LL2)* which deletes all occurrence of X in LL1 to get LL2.

Ordered Linked Lists

- Write $add(X, LL1, LL2)$ which inserts X in an ordered link list $LL1$ to get $LL2$.

```
add(X, end, llist(X, end)).
```

```
add(X, llist(Y, Rest), llist(X, llist(Y, Rest))):-  
    X =< Y.
```

```
add(X, llist(Y, Rest), llist(Y, Rest2)) :-  
    X>Y,  
    add(X, Rest, Rest2).
```

```
?- add(34,end, R1), add(31, R1, R2),  
    add(2, R2, R3), add(69, R3, Result).
```

```
R1 = llist(34, end),
```

```
R2 = llist(31, llist(34, end)),
```

```
R3 = llist(2, llist(31, llist(34, end))),
```

```
Result= llist(2,llist(31,llist(34,llist(69,end))));
```

```
false
```

Ordered Linked Lists (cont.)

- Exercise:
 1. Modify `add` to skip adding an element if it is already in the linked list.
 2. Modify `add` to work with terms, use $X@=<Y$, $X@>Y$, etc
- Write $del(X, L1, L2)$ to delete X from an ordered linked list:

```
del(X, Old, New) :- add(X, New, Old).
```

```
?- add(5, llist(1, llist(2, end)), R),  
del(2, R, Final).
```

```
R = llist(1, llist(2, llist(5, end))),  
Final = llist(1, llist(5, end)) ;  
false.
```

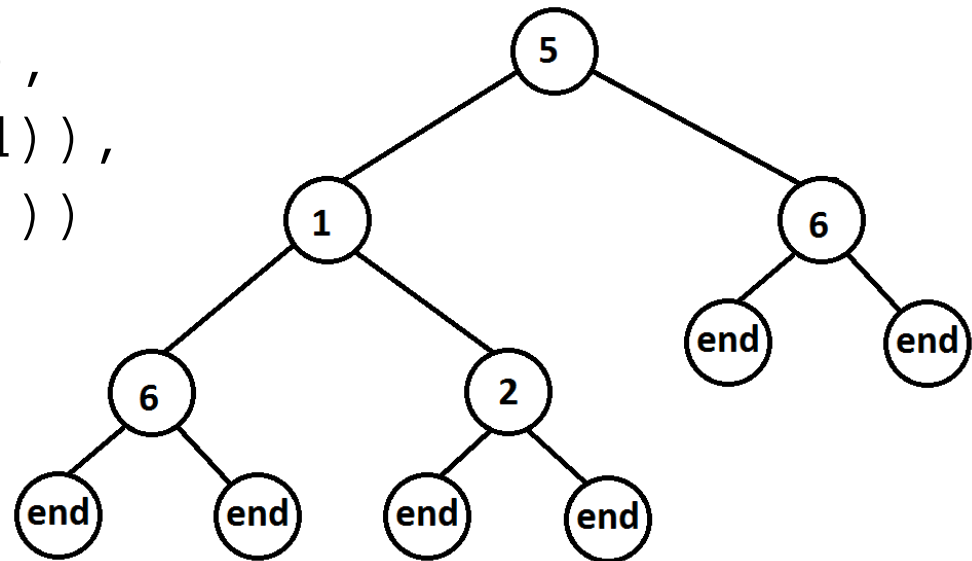
Binary Trees

- Each node **Root** in a binary tree has two children, **Left** and **Right**.

`t(Left, Root, Right)`

- Unless it is a leaf, which can be denoted as 'end'.

```
t(t(t(end, 6, end),
    1, t(end, 2, end)),
  5, t(end, 6, end))
```



Binary Trees- counting elements

- Counting the elements in a binary tree

```
count(end,0).
```

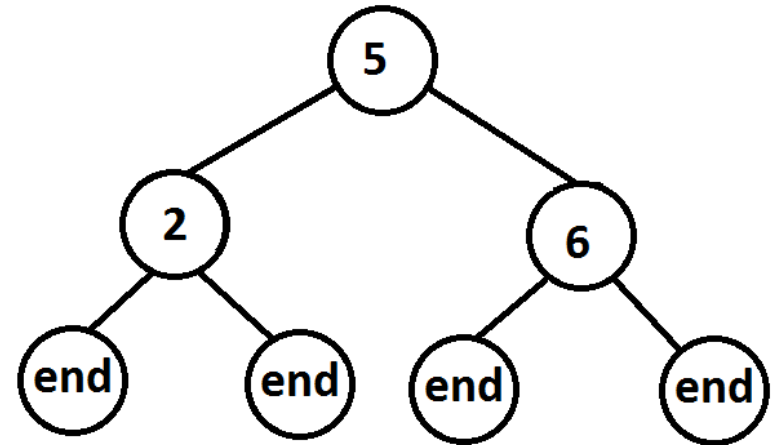
```
count(t(Left, Root, Right), N) :-  
    count(Left, N1),  
    count(Right, N2),  
    N is N1 + N2 +1.
```

```
?- count(t( t( t(end, 6,end),1,  
    t(end,2,end)), 5, t(end,6,end)),  
    N).
```

N = 5.

Sorted Binary Trees

- A binary tree is sorted if
 $Left < Root \leq Right$
- Searching for an item in a sorted binary tree:



```
lookup(Item, t(Left, Item, Right)).  
lookup(Item, t(Left, Root, Right)):-  
    Item < Root,  
    lookup(Item, Left).  
lookup(Item, t(Left, Root, Right)):-  
    Item > Root,  
    lookup(Item, Right).
```

Sorted Binary Trees- add items

- Adding an item in a sorted binary tree

```
addT(X, end, t(end, X, end)).           % if empty tree
```

```
addT(X, t(L, Root, R), t(L1, Root, R)):-  
    X < Root,  
    addT(X, L, L1).
```

```
addT(X, t(L, Root, R), t(L, Root, R1)):-  
    X >= Root,  
    addT(X, R, R1).
```

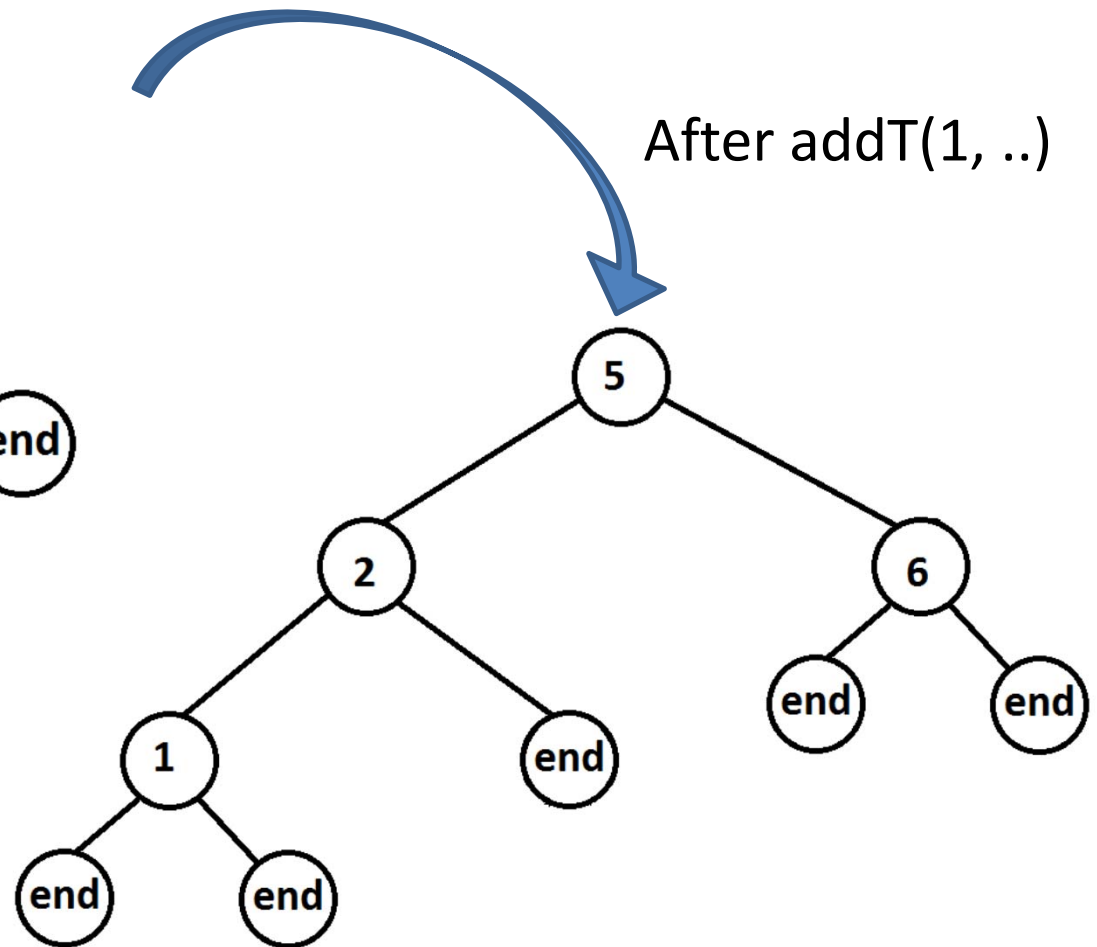
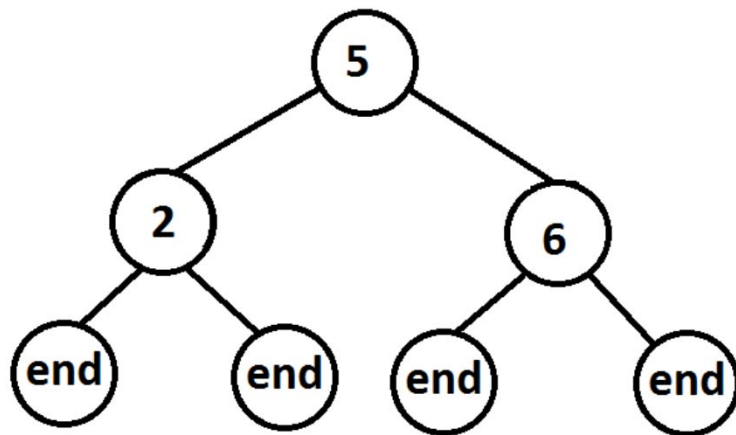
```
?- addT(1, t(t(end,2,end),5,t(end,6,end)), L).
```

```
L = t( ? ,5,t(end,6,end))
```

```
L = t(t( ? ,2,end),5,t(end,6,end))
```

```
L = t(t( t(end,1,end),2,end),5,t(end,6,end))
```

Sorted Binary Trees- add items



Sorted Binary Trees- delete items

- Deleting an item from a sorted binary tree

```
delT(X, t(end, X, R), R).
```

```
delT(X, t(L, X, end), L).
```

```
delT(X, t(L, X, R), t(L, Y, R1)):- delMin(R, Y, R1).
```

```
delT(X, t(L, A, R), t(L1, A, R)):- X < A,  
delT(X, L, L1).
```

```
delT(X, t(L, A, R), t(L, A, R1)):- X > A,  
delT(X, R, R1).
```

```
delMin(t(end, Y, R), Y, R).
```

```
delMin(t(L, Root, R), Y, t(L1, Root, R)):-  
delMin(L, Y, L1).
```

- Exercise: What is the property of node Y in `delMin(T1, Y, T2)`?