

Math/CSE 1560 Midterm test (version A)- Solutions
Winter 2011
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1. (20 points) Write 1-2 line answers for each of the following parts.

(a) (4 points) What is the response you expect to the following lines of code? Why?

```
a:= proc(n::integer)
print(n);
end proc;
```

```
a(3.1);
```

Solution: The precise error message output by Maple is *Error, invalid input: a expects its 1st argument, n, to be of type integer, but received 3.1*. If you paraphrase this you would get credit.

(b) (4 points) What is the response you expect to the following lines of code?

```
a := 2; d := 3;
evalb(a = d);
```

Solution: False, because $2 \neq 3$.

(c) (4 points) What is the response you expect to the following lines of code? Why?

```
a:= proc(n::integer)
local b;
b:=n+n;
end proc;
```

```
a(3);
```

```
b;
```

Solution: The procedure call $a(3)$ returns 6 but b is not defined (there is no error though) since the assignment of 6 to b was within a procedure, where b was a local variable.

(d) (4 points) Add a comment of the form "This procedure....." to the following procedure to make it very easy for a Maple programmer to understand.

```
a:=proc(n::float)
if frac(log2(n))=0 then return 1;
else return 0;
end if;
end proc;
```

Solution: This procedure returns 1 if the input is a positive power of 2 and 0 otherwise.

Note: Most languages would throw an exception (error) when you call $a()$ with input 0.0 but Maple does not and the procedure works as intended.

(e) (4 points) What is the value of d in the following lines of code? Why?

```
a := proc (n::integer)
local b;
b := 2*n;
print(b);
end proc;
```

```
bb := proc()
local c;
```

```

    c := a(4);
    return c
end proc;

```

```

d := bb();

```

Solution: The correct answer is that d is NULL but “ d is undefined” would get you full credit. The reason that d is not 8 is because the procedure `a` prints but does not return 8. Therefore c is not set in procedure `bb` and it follows that d is not set to 8.

Note: Some students have claimed d is 8 on their versions of Maple. I have not seen the claim being substantiated. My answer is based on Maple 12.

2. (a) (5 points) Write down a Maple command to plot a line segment joining (2,2) and (2,3). You must use `do this` by using an appropriate function and invoking it in a `plot` command.

Solution:

```

plot([2,t,t=2..3]);

```

Note:

```

plot([2,t],t=2..3)

```

produces a set of 2 curves – completely different from what the question asks.

- (b) (7 points) Use the `seq()` command to compute the set $\{2^i : 1 \leq i \leq 100\}$.

Solution:

```

{seq(2^i:i=1..100)}

```

- (c) (8 points) Use the `map()` command to compute the set $\{i^2 : 1 \leq i \leq 100\}$.

Solution:

```

map(i->i^2,{seq(i,i=1..100)})

```

3. (10 points) Write a procedure that contains two local functions. The procedure should take as input an integer n . The first function should compute the number of digits of n . The second function should compute the i^{th} digit of n . The procedure must use these functions to return the largest digit used in the decimal representation of n . For example, if $n = 1238$, the procedure should return 8.

Solution:

```

p2 := proc (n::integer)
local x, i,numdig,ithdig;

numdig := n -> 1+trunc(evalf(log10(n)));
ithdig := (n, k) -> iquo(irem(n, 10^k), 10^(k-1)) ;

x := {seq(ithdig(n, i), i = 1 .. numdig(n))};
return max(x)
end proc;

```

Note: A very minor twist on a solved practice problem for the midterm.

4. (10 points) Write a procedure that takes as input an integer n and returns a set defined by $\{2^i : i \text{ is a factor of } n\}$.

Solution:

```

expfactorlist := proc (n::integer)
local divisor,rset;
divisor := (n, i) -> piecewise(frac(n/i) = 0,2^i, frac(n/i) <> 0, -100);
rset:={seq(divisor(n, i), i = 1 .. n)} minus {-100}
return map(i->2^i,rset);
end proc;

```