

Assignment 5  
Due: November 2, 9:30 am

1. (4 points) Suppose  $f: \mathbb{R} \rightarrow \mathbb{Z}$  where  $f(x) = \lceil 2x - 1 \rceil$ . Draw the graph of  $f$ .
2. (4 points) For each of the following sequence, find a formula that generates sequence  $a_0, a_1, a_2, a_3, \dots$  that begins with the given list.
  - a. 15, 20, 25, 30, 35, ...
  - b. 2, 4, 16, 256, 65536, ...
3. (4 points) Find the value of each of these sums.
  - a. 
$$\sum_{i=2}^7 (-3 \times 2^i)$$
  - b. 
$$\sum_{i=0}^3 \sum_{j=2}^4 (2i + 3j + 1)$$
4. (2 points) Show that the union of two countable sets is countable.