



Path Testing and Test Coverage

Chapter 9



Structural Testing

- Also known as glass/white/open box testing
- Structural testing is based on using specific knowledge of the program source text to define test cases
 - Contrast with functional testing where the program text is not seen but only hypothesized



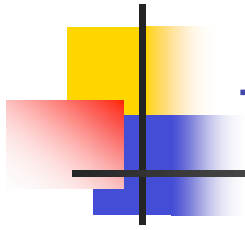
Structural Testing

- Structural testing methods are amenable to
 - Rigorous definitions
 - Control flow, data flow, coverage criteria
 - Mathematical analysis
 - Graphs, path analysis
 - Precise measurement
 - Metrics, coverage analysis



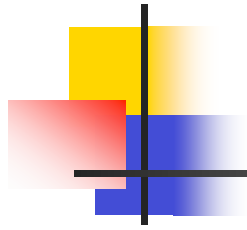
Program Graph - Definition

- Given a program written in an imperative programming language, its **program graph** is a directed graph in which nodes are statements and statement fragments, and edges represent flow of control

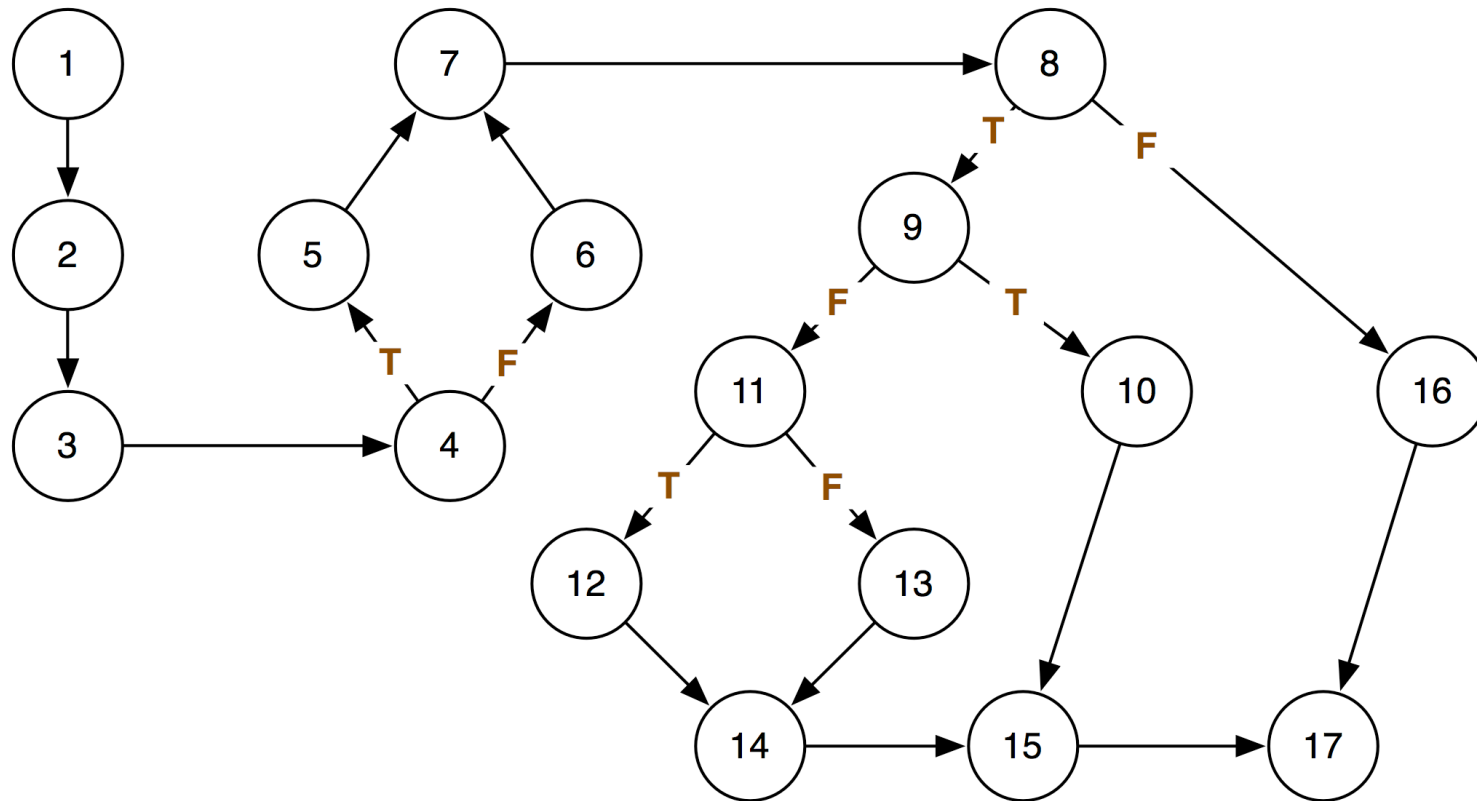


Triangle program text

```
1  output ("Enter 3 integers")
2  input (a, b, c)
3  output("Side a,b c: ", a, b, c)
4  if (a < b) and (b < a+c) and (c < a+b)
5  then isTriangle ← true
6  else isTriangle ← false
7  fi
8  if isTriangle
9  then if (a = b) and (b = c)
10         else output ("equilateral")
11         else if (a ≠ b ) and ( a ≠ c ) and ( b ≠ c)
12                 then output ("scalene")
13                 else output("isosceles")
14         fi
15     fi
16 else output ("not a triangle")
17 fi
```

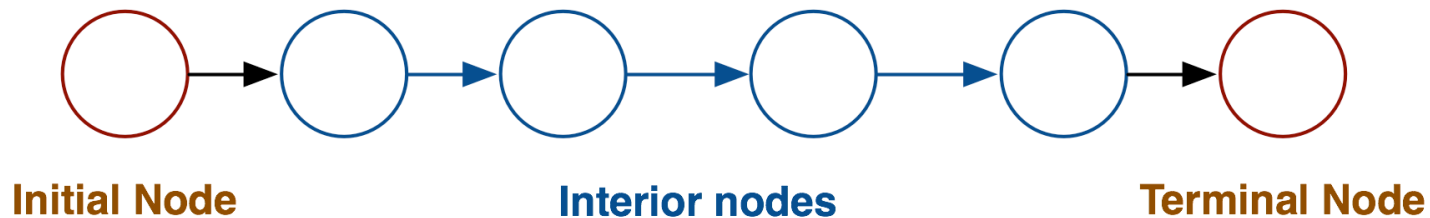


Program Graph - Example



DD-Path – informal definition

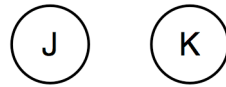
- A **decision-to-decision** path (DD-Path) is a path chain in a program graph such that
 - Initial and terminal nodes are distinct
 - Every interior node has $\text{indeg} = 1$ and $\text{outdeg} = 1$
 - The initial node is 2-connected to every other node in the path
 - No instances of 1- or 3-connected nodes occur



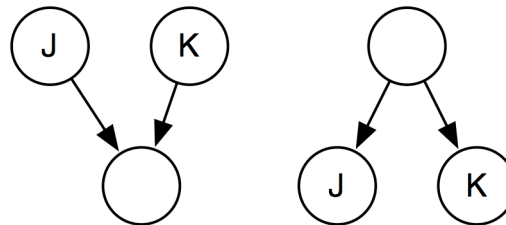


Connectedness definition

- Two nodes n_1 and n_2 in a directed graph are
 - 0-connected iff no path exists between them

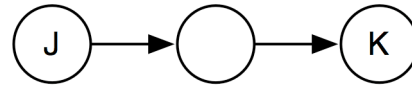


- 1-connected iff a semi-path but no path exists between them

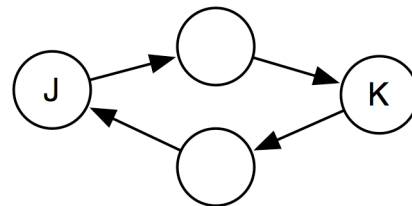


Connectedness definition – 2

- Two nodes n_1 and n_2 in a directed graph are
 - 2-connected iff a path exists between them



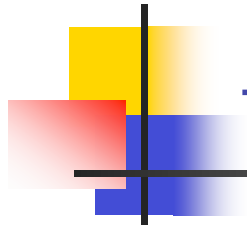
- 3-connected iff a path goes from n_1 to n_2 , and a path goes from n_2 to n_1





DD-Path – formal definition

- A **decision-to-decision** path (DD-Path) is a chain in a program graph such that:
 - Case 1: consists of a single node with $\text{indeg}=0$
 - Case 2: consists of a single node with $\text{outdeg}=0$
 - Case 3: consists of a single node with $\text{indeg} \geq 2$ or $\text{outdeg} \geq 2$
 - Case 4: consists of a single node with $\text{indeg} = 1$, and $\text{outdeg} = 1$
 - Case 5: it is a maximal chain of length ≥ 1
- DD-Paths are also known as **segments**



Triangle program DD-paths

Nodes	Path	Case
1	First	1
2,3	A	5
4	B	3
5	C	4
6	D	4
7	E	3
8	F	3
9	G	3

Nodes	Path	Case
10	H	4
11	I	3
12	J	4
13	K	4
14	L	3
15	M	3
16	N	4
17	Last	2



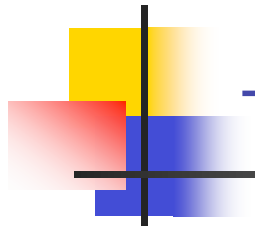
DD-Path Graph – informal definition

- Given a program written in an imperative language, its **DD-Path graph** is a directed graph, in which
 - nodes are DD-Paths of its program graph
 - edges represent control flow between successor DD-Paths.
- Also known as **Control Flow Graph**

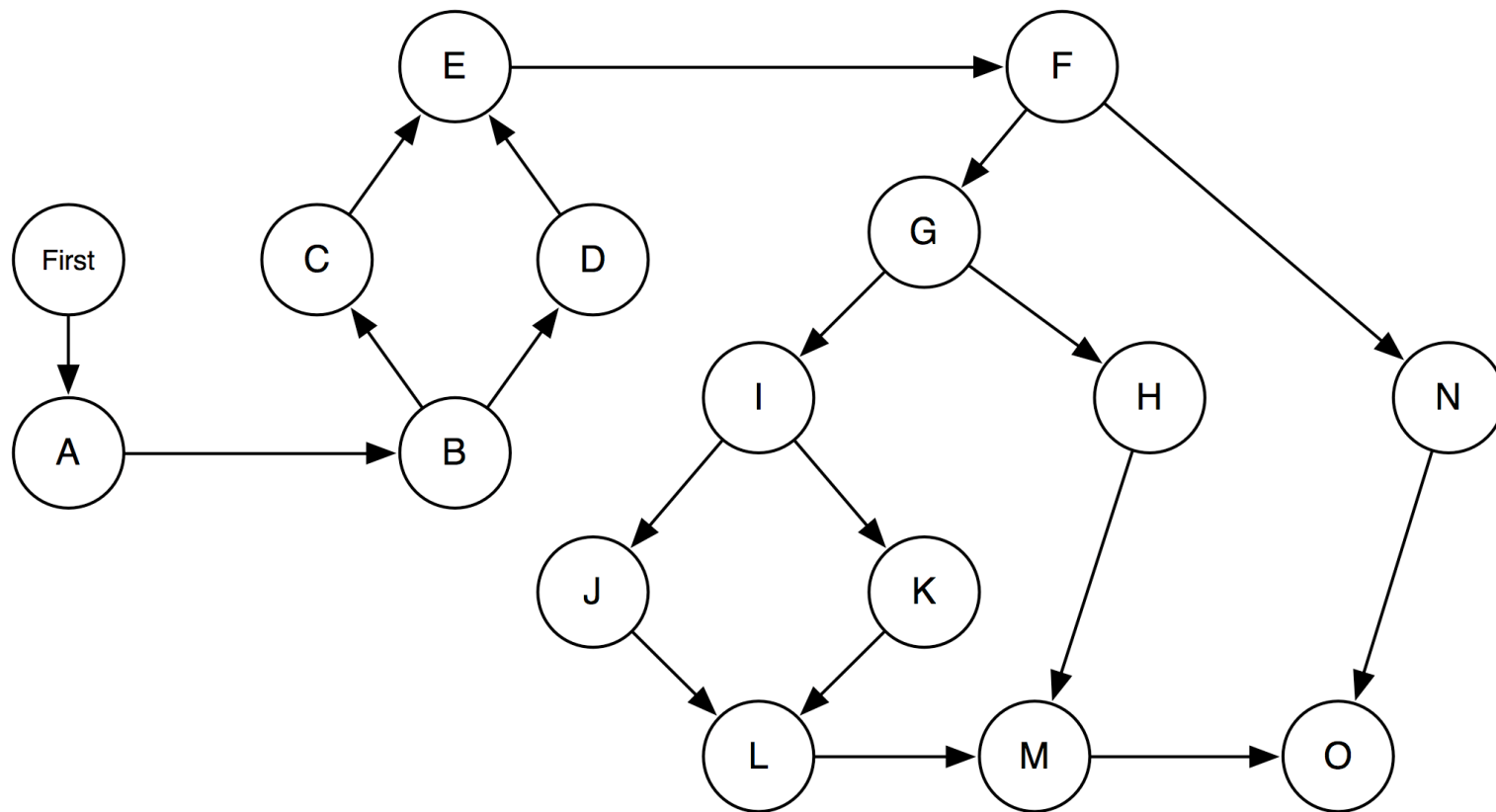


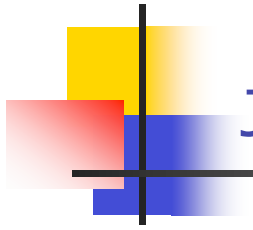
Control Flow Graph Derivation

- Straightforward process
- Some judgment is required
- The last statement in a segment must be a predicate, a loop control, a break, or a method exit



Triangle program DD-path graph





Java example program

```
public int displayLastMsg(int nToPrint) {
    np = 0;
    if ((msgCounter > 0) && (nToPrint > 0)) {
        for (int j = lastMsg; ((j != 0) && (np < nToPrint)); --j) {
            System.out.println(messageBuffer[j]);
            ++np;
        }
        if (np < nToPrint) {
            for (int j = SIZE; ((j != 0) && (np < nToPrint)); --j) {
                System.out.println(messageBuffer[j]);
                ++np;
            }
        }
    }
    return np;
}
```



Java example program – Segments part 1

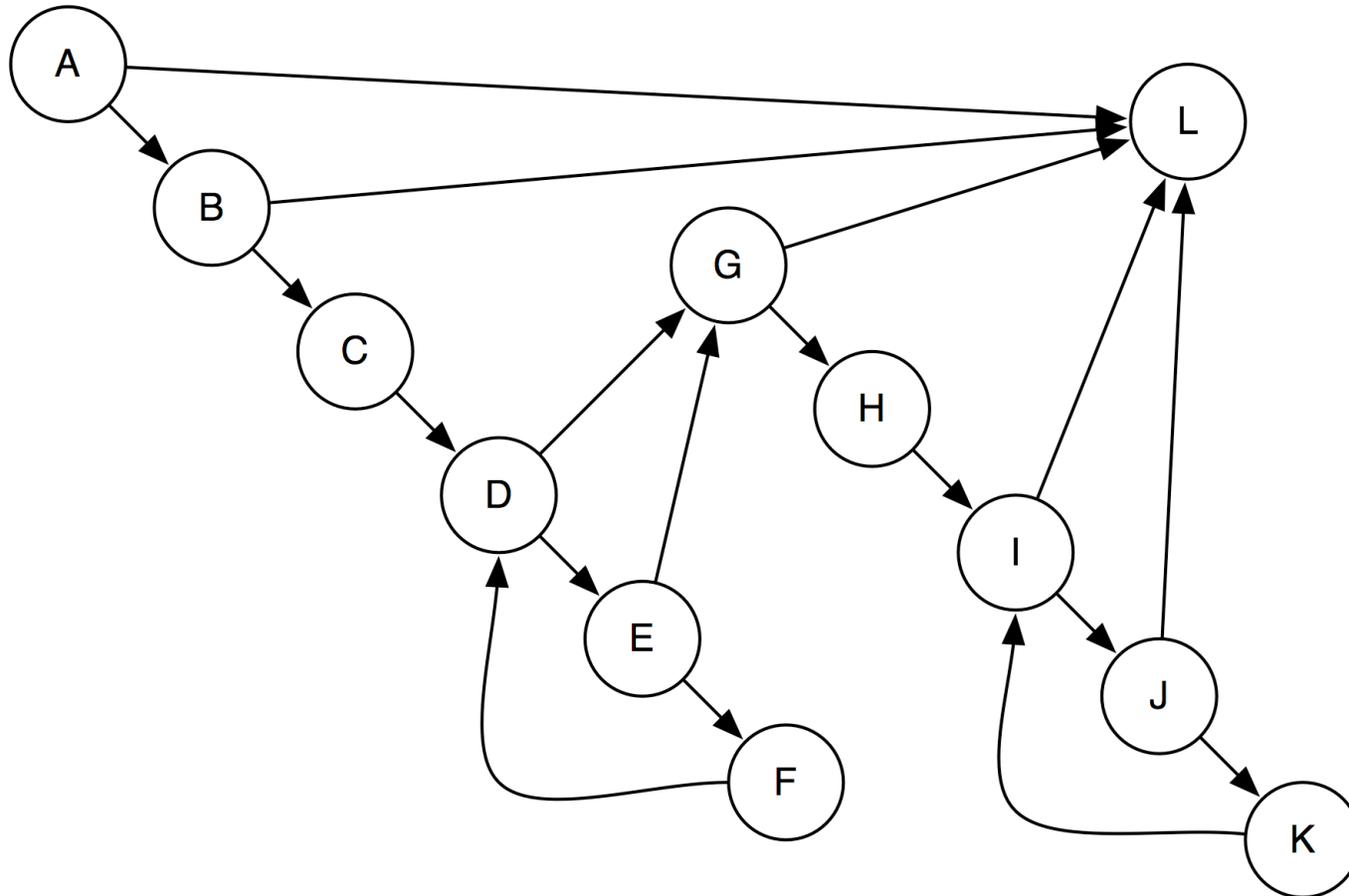
Line		Segment
1	<code>public int displayLastMsg(int nToPrint) {</code>	
2	<code>np = 0;</code>	A
3	<code>if ((msgCounter > 0)</code>	A
4	<code>&& (nToPrint > 0))</code>	B
5	<code>{ for (int j = lastMsg;</code>	C
6	<code>((j != 0)</code>	D
7	<code>&& (np < nToPrint));</code>	E
8	<code>--j)</code>	F
9	<code>{ System.out.println(messageBuffer[j]);</code>	F
10	<code>++np;</code>	F
11	<code>}</code>	F



Java example program – Segments part 2

Line		Segment
12	<code>if (np < nToPrint)</code>	G
13	<code>{ for (int j = SIZE;</code>	H
14	<code>((j != 0) &&</code>	I
15	<code>(np < nToPrint));</code>	J
16	<code>--j)</code>	K
17	<code>{ System.out.println(messageBuffer[j]);</code>	K
18	<code>++np;</code>	K
19	<code>}</code>	L
20	<code>}</code>	L
21	<code>}</code>	L
22	<code>return np;</code>	L
23	<code>}</code>	L

Java example program displayLastMsg – DD-path graph





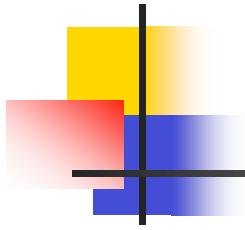
DD graphs definition – 1

- Depict which program segments may be followed by others
- A segment is a node in the CFG
- A conditional transfer of control is a **branch** represented by an edge
- An **entry node** (no inbound edges) represents the entry point to a method
- An **exit node** (no outbound edges) represents an exit point of a method



DD graphs definition – 2

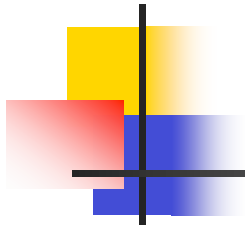
- An **entry-exit path** is a path from the entry node to the exit node
- **Path expressions** represent paths as sequences of nodes
- Loops are represented as segments within parentheses followed by an asterisk
- There are 22 different path expressions in our example



Path expressions – part 1

Entry-Exit path

1	A L
2	A B L
3	A B C D G L
4	A B C D E G L
5	A B C (D E F)* D G L
6	A B C (D E F)* D E G L
7	A B C D G H I L
8	A B C D G H I J L
9	A B C D G H (I J K)* I L
10	A B C (D E F)* D E G H (I J K)* I J L
11	A B C D E G H I L



Path expressions – part 2

Entry-Exit path

12	A B C D E G H I J L
13	A B C D E G H (I J K)* I L
14	A B C D E G H (I J K)* I J L
15	A B C (D E F)* D G H I L
16	A B C (D E F)* D G H I J L
17	A B C (D E F)* D G H (I J K)* I L
18	A B C (D E F)* D G H (I J K)* I J L
19	A B C (D E F)* D E G H I L
20	A B C (D E F)* D E G H I J L
21	A B C (D E F)* D E G H (I J K)* I L
22	A B C (D E F)* D E G H (I J K)* I J L

Paths displayLastMsg – decision table – part 1

Path condition by Segment Name

	Entry/Exit Path	A	B	D	E	G	I	J
1	A L	F	–	–	–	–	–	–
2	A B L	T	F	–	–	–	–	–
3	A B C D G L	T	T	F	–	F	–	–
4	A B C D E G L	T	T	T	F	–	–	–
5	A B C (D E F)* D G L	T	T	T/F	T/–	F	–	–
6	A B C (D E F)* D E G L	T	T	T/T	T/F	F	–	–
7	A B C D G H I L	T	T	F	–	T	F	–
8	A B C D G H I J L	T	T	F	–	T	T	F
9	A B C D G H (I J K)* I L	T	T	F	–	T/F	T/–	T
10	A B C D G H (I J K)* I J L	T	T	F	–	T/T	T/F	T
11	A B C D E G H I L	T	T	T	F	T	F	–

x/x Conditions at loop entry and exit

Branch coverage – decision table example – part 2

Path condition by Segment Name

	Entry/Exit Path	A	B	D	E	G	I	J
12	A B C D E G H I J L	T	T	T	F	T	T	F
13	A B C D E G H (I J K)* I L	T	T	T	F	T	T/F	T/-
14	A B C D E G H (I J K)* I J L	T	T	T	F	T	T/T	T/F
15	A B C (D E F)* D G H I L	T	T	T/F	T/-	T	F	-
16	A B C (D E F)* D G H I J L	T	T	T/T	T/F	T	T	F
17	A B C (D E F)* D G H (I J K)* I L	T	T	T/F	T/-	T	T/F	T/-
18	A B C (D E F)* D G H (I J K)* I J L	T	T	T/F	T/-	T	T/T	T/F
19	A B C (D E F)* D E G H I L	T	T	T/T	T/F	T	F	-
20	A B C (D E F)* D E G H I J L	T	T	T/T	T/F	T	T	F
21	A B C (D E F)* D E G H (I J K)* I L	T	T	T/T	T/F	T	T	T
22	A B C (D E F)* D E G H (I J K)* I J L	T	T	T/T	T/F	T	T	T

x/x Conditions at loop entry and exit



Program text coverage Metrics

- C_0 Every Statement
- C_1 Every DD-path
- C_{1p} Every predicate to each outcome
- C_2 C_1 coverage + loop coverage
- C_d C_1 coverage + every dependent pair of DD-paths
- C_{MCC} Multiple condition coverage
- C_{ik} Every program path that contains k loop repetitions
- C_{stat} Statistically significant faction of the paths
- C_∞ Every executable path



Program text coverage models

- Statement Coverage
- Segment Coverage
- Branch Coverage
- Multiple-Condition Coverage



Statement coverage – C_0

- Achieved when all statements in a method have been executed at least once
- A test case that will follow the path expression below will achieve statement coverage in our example

A B C (D E F)* D G H (I J K)* I L

- One test case is enough to achieve statement coverage!



Segment coverage

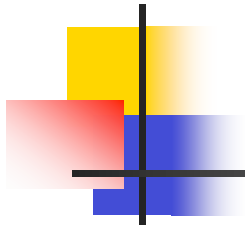
- **Segment coverage** counts segments rather than statements
- May produce drastically different numbers
 - Assume two segments P and Q
 - P has one statement, Q has nine
 - Exercising only one of the segments will give 10% or 90% statement coverage
 - Segment coverage will be 50% in both cases



Statement coverage problems

- Predicate may be tested for only one value (misses many bugs)
- Loop bodies may only be iterated once
- Statement coverage can be achieved without branch coverage. Important cases may be missed

```
String s = null;  
if (x != y) s = "Hi";  
String s2 = s.substring(1);
```

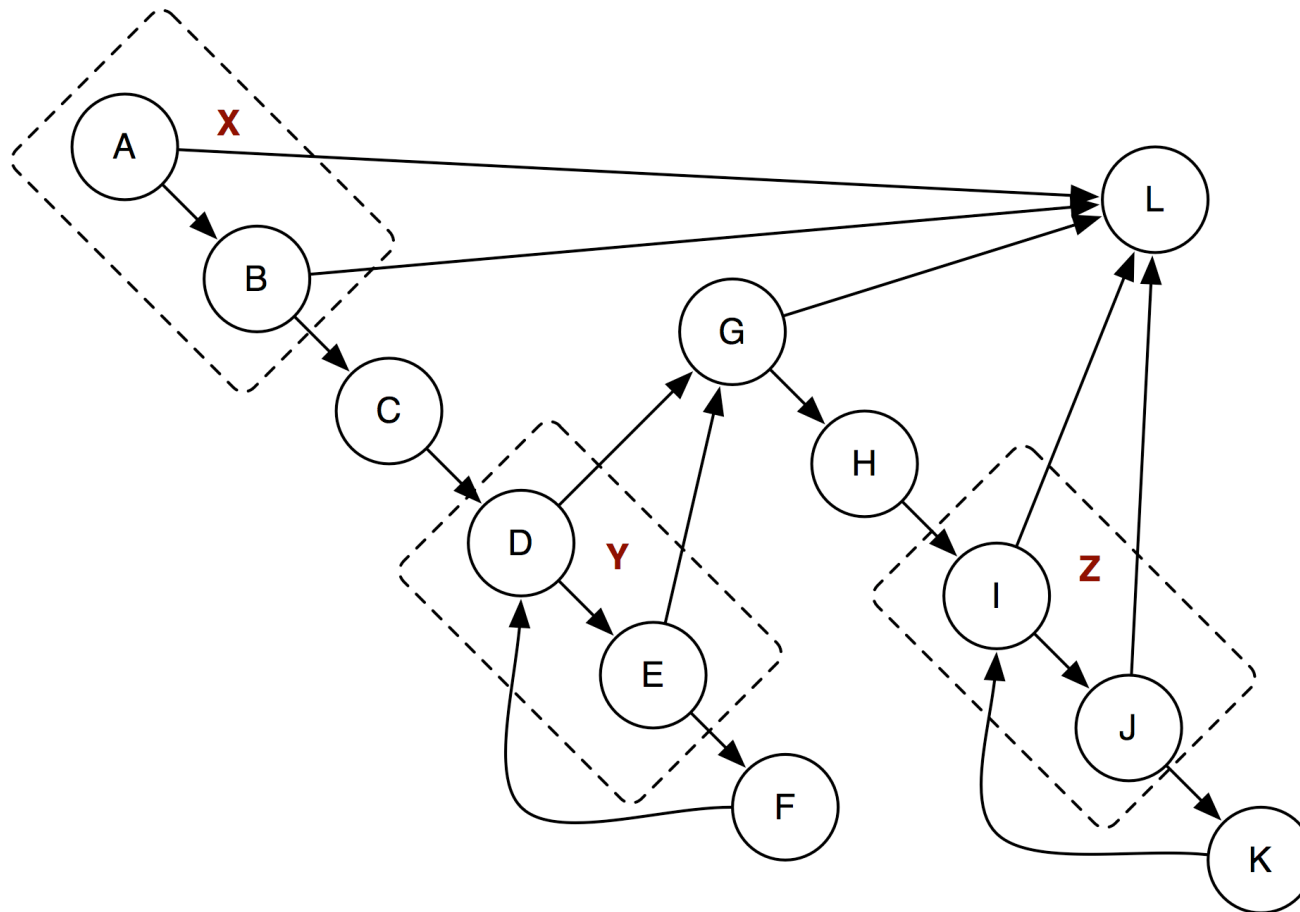


Branch coverage – C_{1p}

- Achieved when every path from a node is executed at least once
- At least one true and one false evaluation for each predicate
- Can be achieved with $D+1$ paths in a control flow graph with D 2-way branching nodes and no loops
 - Even less if there are loops
- In the Java example displayLastMsg branch coverage is achieved with three paths – see next few slides

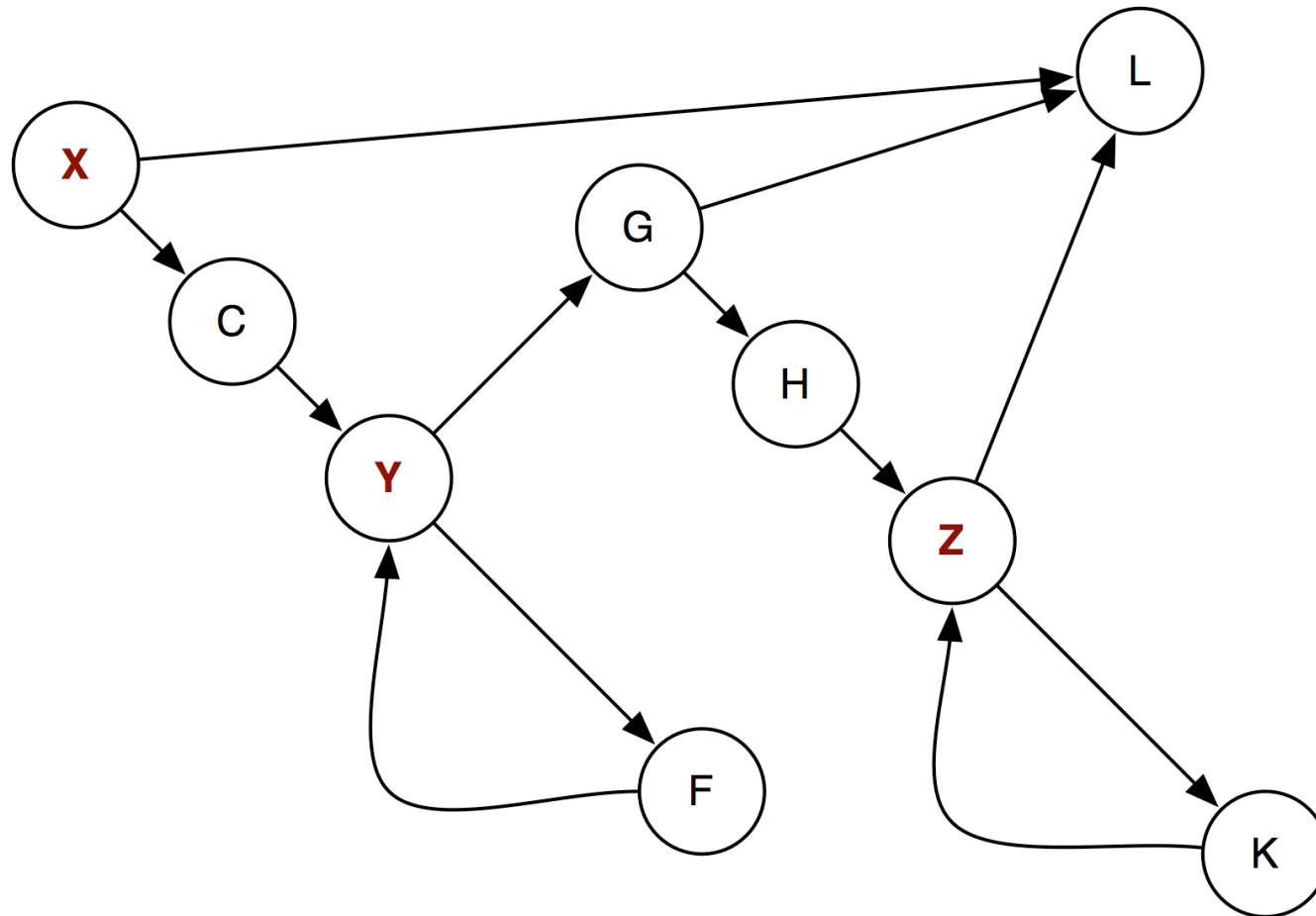
X L
X C (Y F)* Y G L
X C (Y F)* Y G H (Z K)* Z L

Java example program displayLastMsg – DD-path graph



X, Y & Z are shorthand for the nodes within the dotted boxes; used for branch testing

Java example program displastLastMsg – aggregate predicate DD-path graph



Paths aggregate – decision table – part 1

Path condition by Segment Name

	Branch Coverage	A	B	D	E	G	I	J
1	X L	F	–	–	–	–	–	–
2	X L	T	F	–	–	–	–	–
3	X C Y G L	T	T	F	–	F	–	–
4	X C Y G L	T	T	T	F	–	–	–
5	X C (Y F)* Y G L	T	T	T/F	T/–	F	–	–
6	X C (Y F)* Y G L	T	T	T/T	T/F	F	–	–
7	X C Y G H Z L	T	T	F	–	T	F	–
8	X C Y G H Z L	T	T	F	–	T	T	F
9	X C Y G H (Z K)* I L	T	T	F	–	T/F	T/–	T
10	X C Y G H (Z K)* I L	T	T	F	–	T/T	T/F	T
11	X C Y G H Z L	T	T	T	F	T	F	–

x/x Conditions at loop entry and exit

Branch coverage – decision table example – part 2

Path condition by Segment Name

	Branch Coverage	A	B	D	E	G	I	J
12	X C Y G H Z L	T	T	T	F	T	T	F
13	X C Y G H (Z K)* Z L	T	T	T	F	T	T/F	T/-
14	X C Y G H (Z K)* Z L	T	T	T	F	T	T/T	T/F
15	X C (Y F)* Y G H Z L	T	T	T/F	T/-	T	F	-
16	X C (Y F)* Y G H Z L	T	T	T/T	T/F	T	T	F
17	X C (Y F)* Y G H (Z K)* Z L	T	T	T/F	T/-	T	T/F	T/-
18	X C (Y F)* Y G H (Z K)* Z L	T	T	T/F	T/-	T	T/T	T/F
19	X C (Y F)* Y G H Z L	T	T	T/T	T/F	T	F	-
20	X C (Y F)* Y G H Z L	T	T	T/T	T/F	T	T	F
21	X C (Y F)* Y G H (Z K)* Z L	T	T	T/T	T/F	T	T	T
22	X C (Y F)* Y G H (Z K)* Z L	T	T	T/T	T/F	T	T	T

x/x Conditions at loop entry and exit



Branch coverage problems

- Ignores implicit paths from compound paths
 - 11 paths in aggregate model vs 22 in full model
- Short-circuit evaluation means that many predicates might not be evaluated
 - A compound predicate is treated as a single statement. If n clauses, 2^n combinations, but only 2 are tested
- Only a subset of all entry-exit paths is tested
 - Two tests for branch coverage vs 4 tests for path coverage
 - $a = b = x = y = 0$ and $a = x = 0 \wedge b = y = 1$

```
if (a == b) x++;  
if (x == y) x--;
```



Multiple-condition coverage

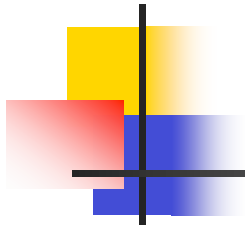
- All true-false combinations of simple conditions in compound predicates are considered at least once
 - Guarantees statement, branch and predicate coverage
 - Does not guarantee path coverage
- A truth table may be necessary
- Not necessarily achievable due to lazy evaluation or mutually exclusive conditions

```
if ((x > 0) && (x < 5)) ...
```



Dealing with Loops

- Loops are highly fault-prone, so they need to be tested carefully
- Simple view: Every loop involves a decision to traverse the loop or not
- A bit better: Boundary value analysis on the index variable
- Nested loops have to be tested separately starting with the innermost
- Once loops have been tested then can be condensed to a single node



Basis path testing

- For a vector space a basis set of vectors can be constructed
 - As a consequence every vector in the space is a linear combination of the basis vectors
- By analogy a basis set of paths can be constructed for a DD-path graph
- Problems
 - One cannot assume that testing the basis set is sufficient
 - Basis sets assume independence of members but program text paths are dependent
 - Analogous to variable dependencies causing problems for boundary value testing



Essential complexity

- The cyclomatic number for a graph is given by
 - $CN(G) = e - v + c$
 - e number of edges v number of vertices
c number of strongly connected components
 - **For strongly connected, need to add edges from every sink to every source**
- Condensation graphs are based on removing strong components or DD-paths
- For programs remove structured program constructs
 - One entry, one exit constructs for sequences, choices and loops
 - Each structured component once tested can be replaced by a single node when condensing its graph



Essential complexity – 2

- Program text that violates proper structure has
 - Branches either into or out of the middle of a loop
 - Branches either into or out of then and else phrases of if...then...else statements
 - This increases the cyclomatic number – i.e. the complexity of the program
- The higher the cyclomatic number the more tests are required.
 - If complexity is too high
 - Simplify the program rather than do more testing



Guidelines

- Functional testing is too far from the program text
- Path testing is too close to the program text
 - Obscures feasible and infeasible paths
 - Use dataflow testing to move out a bit
- Path testing
 - does not give good help in finding test cases
 - does give good measures of quality of testing through coverage analysis
 - Basis path testing gives a lower bound on the number of tests



Guidelines – 2

- Path testing
 - Provides set of metrics that cross-check functional testing
 - Use to resolve gap and redundancy questions
 - Missing DD-paths – have gaps
 - Repeated DD-paths – have redundancy
- Distinctions are made with the following types of paths
 - Feasible – infeasible
 - Specified – unspecified
 - Topologically possible – impossible

Guidelines – 3

- Re-examine the Venn diagram in the context of path testing

