

Homework Exercise #6

Due: November 10, 2009

1. The model of computation for this question is an asynchronous shared-memory system of n processes. The shared memory consists of linearizable registers. Processes may experience crash failures.

A PROD object stores a positive number (initially 1) and provides two types of operations:

- `MULT(x)` multiplies the value stored in the object by x and returns `ACK` (where x is a positive integer).
- `PRODUCT` returns the current state of the object without changing it, and

- (a) Show that the following implementation of a PROD object is *not* linearizable. It uses n shared registers, denoted R_1, \dots, R_n and the code below is for process P_i . Each register initially contains 1.

```
MULT( $x$ )
   $v \leftarrow \text{read}(R_i)$ 
  write( $v * x$ ) into  $R_i$ 
  return ACK
end MULT
```

```
PROD
   $result \leftarrow 1$ 
  for  $i = 1$  to  $n$ 
     $result \leftarrow result * \text{read}(R_i)$ 
  end for
  return result
end PROD
```

- (b) Is the implementation in part (a) linearizable if the only argument allowed for `MULT` operations is 2?
- (c) Describe how the PROD object can be implemented in a linearizable and lock-free way. The implementation should work for all possible arguments to `MULT` operations, not just 2. (“Lock-free” will be defined in the Nov 5 lecture, but it means that, even if some processes crash, whenever there are pending operations on the PROD object by non-faulty processes, one of those operations will eventually finish.)