# Register Transfer Level 

## ECE470

## RTL

- A digital system is represented at the register transfer level by these three components

1. The set of registers in the system
2. The operation that are performed on the data stored in the registers
3. The control that supervises the sequence of operations in the system.

- The operations executed on the information stored in the registers are elementary operations and performed in parallel during one clock cycle.


## RTL

- Comma is used to separate 2 or more operations that are executed in the same time If(T3=1) then ( $2 \leftarrow \leftarrow \mathrm{R} 1, \mathrm{R} 1 \leftarrow \mathrm{R} 2$ )
- That is possible with registers that have edge triggered flip-flop


## RTL in HDL



## HDL Operations

- Arithmetic: + - */ \%
- Logic (bit wise): ~\&|^
- Logical ! \&\& ||
- Shift $\gg \ll\{$,
- Relational > < == != >= <=
- In shifting, the vacant bits are filled with zeros


## Loop Statements

- 

| integer count initial | initial begin |
| :---: | :---: |
| begin | clock = 1'b0; |
| count $=0$; | end |
| while (count <0) | repeat (16) |
| \#5 count = count+1; | \#5 clock $=\sim$ clock; |
| end | end |

## Loop Statements

module decoder
input [1:0] IN;
output [3:0]Y;
reg [3:0]Y;
integer I;
always @(IN)

for ( $I=0 ; 1<=3 ; \quad I=I+1$ ) if (IN == I) $\quad Y[1\}=1 ;$
else $Y[1\}=0$;
endmodule


Fig. 8-1 Process of HDL Simulation and Synthesis

## Algorithmic State Machine (ASM)



Fig. 8-2 Control and Datapath Interaction

## ASM

- ASM is similar to flowchart in the sense that it specifies a sequence of procedural steps and decision paths for an algorithm.
- However, ASM is interpreted differently than a flowchart. While the flow chart is interpreted as a sequence of operations, ASM describes the sequence of events as well as the timing relationship between the states (as we will see shortly).


## State Box



Fig. 8-3 State Box
The state is given a symbolic name (T3)
Binary code for the assigned state (011)
The operations that are performed in this state $R \leftarrow 0$; and START could be an output signal is generated to start some operation
The operation is performed when we leave $T_{3}$ to the next state

## Decision Box



Fig. 8-4 Decision Box

## Conditional Box



Input to the conditional box must come from one of the exit paths of a decision box.

The register operation or outputs listed inside the conditional box are generated during a given state, if the input condition is satisfied of course

Fig. 8-5 Conditional Box

## ASM

- The operation in the state box or conditional box are nott executed in the current state.
- Rather, a control signal is asserted in the current state if Q0 is 1 and the operation is done at the transition from this state to the next one (with the next clock cycle)



## ASM Block



Fig. 8-6 ASM Block
If flow chart, $A$ is incremented, then $E$ is tested


Fig. 8-7 State Diagram Equivalent to the ASM Chart of Fig. 8-6 ASM block is a structure consisting of one state box and all the decision and conditional boxes connected to its exit path.
Each block in the ASM describes the state of the system during one clock-pulse interval.

The operations within the state and conditional boxes are executed at the clock pulse when the system is leaving $T_{1}$ to $T_{2}$, $\mathrm{T}_{3}$, or $\mathrm{T}_{4}$

## Timing Consideration



Fig. 8-8 Transition Between States

## Design Example

- Design a system with 2 flip-flops $E$ and $F$, and one 4 bit binary counter $\left(A_{4}, A_{3}, A_{2}, A_{1}\right)$.
- A start signal initiates the operation by clearing $A$ and F.
- Then the counter is incremented by one starting from the next clock pulse and continues to increment until the operation stops. $A_{3}$ and $A_{4}$ determine the operations.
- If $A_{3}=0, E$ is cleared and continue
- If $A 3=1, E$ is set; then if $A 4=0$ continue, if $A 4=1 F$ is set to 1 on the next clock cycle and the system stops.


| Counter | Flip-Flops |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{A}_{4} \mathrm{~A}_{3}$ | $\mathrm{~A}_{2}$ | $\mathrm{~A}_{1}$ | E | F | Condition | State |
| 0 | 0 | 0 | 0 | 1 | 0 | $\mathrm{~A}_{3}=0, \mathrm{~A}_{4}=0$ |
| 0 | 0 | 0 | 1 | 0 | 0 |  |
| 0 | 0 | 1 | 0 | 0 | 0 |  |
| 0 | 0 | 1 | 1 | 0 | 0 |  |
| 0 | 1 | 0 | 0 | 0 | 0 | $\mathrm{~T}_{1}=1, \mathrm{~A}_{4}=0$ |
| 0 | 1 | 0 | 1 | 1 | 0 |  |
| 0 | 1 | 1 | 0 | 1 | 0 |  |
| 0 | 1 | 1 | 1 | 1 | 0 |  |
| 1 | 0 | 0 | 0 | 1 | 0 | $\mathrm{~A}_{3}=0, \mathrm{~A}_{4}=1$ |
| 1 | 0 | 0 | 1 | 0 | 0 |  |
| 1 | 0 | 1 | 0 | 0 | 0 |  |
| 1 | 0 | 1 | 1 | 0 | 0 |  |
| 1 | 1 | 0 | 0 | 0 | 0 | $\mathrm{~A}_{3}=1, \mathrm{~A}_{4}=1$ |
| 1 | 1 | 0 | 1 | 1 | 0 |  |
| 1 | 1 | 0 | 1 | 1 | 1 |  |

## Timing Sequence

- That illustrates the difference between ASM and flowchart.
- When the system is in state 1011 , It checks $A_{3}$ is 0 , so it sets E to 0 and increment counter to 1100, the next cycle will start with 1100 and $E$ set to 0 .
- Then checks $A_{3}$ and $A_{4}$ (both are 1), it sets $E$ to 1 , and increments counter.
- Next cycle counter is 1101, and $\mathrm{E}=1$ and now it is in state 2
- Then it set F to 1 and goes to state 0


## Datapath Design

- The requirements for the design of the datapath are specified in the state and conditional boxes.
- The control logic is determined from the decision and the required state transition.
- A look at the datapath design of the previous example.


## Datapath design

- In state $\mathrm{T}_{0}$, clear the counter and the F flipflop (the and gate and $f$ inputs).
- In state $T_{1}$, if $A_{3}=0$, set $E \leftarrow 0$ ( will generate 01 on the $J K$ inputs of $E$ if the state is T1).
- In state $T_{1}$, if $A_{3} A_{4}=10 ; E \leftarrow 0$ (note the inputs of E ).
- In state $\mathrm{T}_{2}$, if $\mathrm{A}_{3} \mathrm{~A}_{4}=11, \mathrm{~F} \leftarrow 1$, and (the F F is set).


Fig. 8-10 Datapath for Design Example


## State Table

- The state diagram can be converted into a state table.
- Three states ( $T_{0}, T_{1}$, and $T_{2}$ ), represents as the output of two registers $\left(\mathrm{G}_{1} \mathrm{G}_{0}\right)$ as 00, 01, and 11.
- The following table shows the state table for the previous example.

| Present (symbol) | Present State |  | Inputs |  |  | next State |  | Outputs |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | G1 | G0 | s | A3 | 4 | G1 | 0 | то | T1 |  |
| T0 | 0 |  | 0 | X | X | 0 | 0 | 1 | 0 | 0 |
| то | 0 | 0 | 1 | X | x | 0 | 1 | 1 | 0 | 0 |
| T1 | 0 | 1 | X | 0 | X | 0 | 1 | 0 | 1 | 0 |
| T1 | 0 | 1 | X | 1 | 0 | 0 | 1 | 0 | 1 | 0 |
| T1 | 0 | 1 | X | 1 | 1 | 1 | 1 | 0 | 1 |  |
| T2 | 1 | 1 | X | x | x | 0 | 0 | 0 | 0 | 1 |
| $\mathrm{T}_{0}=\mathrm{G}^{\prime}$ | $\mathrm{D}_{61}=\mathrm{T}_{1} \mathrm{~A}_{3} \mathrm{~A}_{4}$ |  |  |  |  |  |  |  |  |  |
| $\mathrm{T}_{1}=\mathrm{G}_{1} \mathrm{G}_{0}$ | $\mathrm{D}_{62}=\mathrm{T}_{0} \mathrm{~S}+\mathrm{T}_{1}$ |  |  |  |  |  |  |  |  |  |
| $\mathrm{T}_{2}=\mathrm{G}_{1}$ |  |  |  |  |  |  |  |  |  |  |



## HDL Description

- The description could be one three different levels
- Behavioral description on the RTL level
- Behavior description on the algorithmic level
- Structural description
- Note that the algorithmic level, is used only to verify the design ideas in the early stages. Some of the constructs might not be synthesizable
- Following RTL behavior description
- //RTL description of design example module Example_RTL (S,CLK,Clr,E,F,A);
- //Specify inputs and outputs
- //See block diagram Fig. 8-10
- input S,CLK,Clr;
- output E,F:
- output [4:1] A;
- //Specify system registers
- reg [4:1] A; //A register
- reg E, F; //E and F flip-flops
- reg [1:0] pstate, nstate; //control register
- //Encode the states
- parameter $\mathrm{T} 0=2$ 'b00, $\mathrm{T} 1=2$ 'b01, $\mathrm{T} 2=$ 2'b11;
- //State transition for control logic
- //See state diagram Fig. 8-11(a)
- always @(posedge CLK or negedge CIr)
- $\quad$ if $(\sim \mathrm{Clr})$ pstate $=\mathrm{TO} ; \quad / /$ Initial state
- else pstate <= nstate; //Clocked operations

```
- always @ (S or A or pstate)
- case (pstate)
\bullet
//See list of operations Fig.8-11(b)
- always @(posedge CLK)
- case (pstate)
- TO: if(S)
- begin
endmodule
```


## Testing

- Note that because we used non-blocking assignment we did not have to worry about the order of the statements in every state.
- Had we used a blocking assignment, we have to worry about the order.


## Testing

- //HDL Example 8-3
- //---------------------------
- //Test bench for design example
- module test_design_example;
- reg S, CLK, Clr;
- wire [4:1] A;
- wire E, F;
- //Instantiate design example
- endmodule
- Example_RTL dsexp
(S,CLK,CIr,E,F,A);
- initial
- begin
- $\quad \mathrm{Clr}=0$;
- $\quad S=0$;
- CLK = 0;
- \#5 Clr = 1; S = 1;
- repeat (32)
- begin
- \#5 CLK $=\sim$ CLK;
- end
- end
- initial
- \$monitor("A = \%b E = \%b F = \%b time = \%0d", A,E,F,\$time);


## Structural Description

## Structural Description

- //HDL Example 8-4
- //--
//Structural description of design example
- //See block diagram Fig. 8-10
- module Example Structure (S,CLK,CIr,E,F,A);
- input S,CLK,Clr;
- output E,F;
- output [4:1] A;
- I/Instantiate control circuit
- control ctl (S,A[3],A[4],CLK,CIr,T2,T1,Clear);
- //Instantiate E and F flip-flips
- E_F EF (T1,T2,Clear,CLK,A[3],E,F);
- //Instantiate counter
- counter ctr (T1,Clear,CLK,A);
- endmodule
- //Control circuit (Fig. 8-12)
- module control
(Start,A3,A4,CLK,Clr,T2,T1,Clear);
- input Start,A3,A4,CLK,Clr;
- output T2,T1,Clear;
- wire G1,G0,DG1,DG0;
- //Combinational circuit
- assign DG1 = A3 \& A4 \& T1,
- $\quad \mathrm{DGO}=($ Start \& $\sim \mathrm{G} 0) \mid \mathrm{T} 1$,
- $\quad \mathrm{T} 2=\mathrm{G} 1$,
- $\quad \mathrm{T} 1=\mathrm{G} 0 \& \sim \mathrm{G} 1$,
- Clear $=$ Start \& $\sim$ G0;
- //Instantiate D flip-flop
- DFF G1F (G1,DG1,CLK,Clr),
- GOF (G0,DG0,CLK,Clr);
- endmodule


## Structural Description

- //D flip-flop
- module DFF (Q,D,CLK,Clr);
- input D,CLK,Clr;
- output Q;
- reg Q;
- always @ (posedge CLK or negedge Clr)
- if ( $\sim \mathrm{Clr}) \mathrm{Q}=1$ 'b0;
- else Q = D;
- endmodule
- //E and F flipf-lops
- module E_F (T1,T2,Clear,CLK,A3,E,F);
- input T1,T2,Clear,CLK,A3;
- output E,F;
- wire E,F,JE,KE,JF,KF;
- //Combinational circuit
- assign JE = T1 \& A3,
- $K E=T 1 \& \sim A 3$,
- JF = T2,
- KF = Clear;
- //Instantiate JK flipflop
- JKFF EF (E,JE,KE,CLK),
- FF (F,JF,KF,CLK);
- endmodule


## Structural Description

- //JK flip-flop
- module JKFF (Q,J,K,CLK);
- input J,K,CLK;
- output Q;
- reg Q;
- always @ (posedge CLK)
- case (\{J, K\})
- 2'b00: Q = Q;
- 2'b01: Q = 1'b0;
- 2'b10: Q = 1'b1;
- 2'b11: Q = ~Q;
- endcase
- endmodule
- //counter with synchronous clear
- module counter
(Count, Clear,CLK,A);
- input Count,Clear,CLK;
- output [4:1] A;
- $\quad$ reg [4:1] A;
- always @ (posedge CLK)
- if (Clear) A<= 4'b0000;
- else if (Count) $A<=A+$ 1'b1;
- else $A<=A$;
- endmodule


## Binary Multiplier

- We did this before using combinational circuit (adders, gaters, ..).
- Use one adder and shift registers.
- Instead of shifting multiplicand to the

| 23 | 10111 |
| :---: | :---: |
|  | 10011 |
|  | 10111 |
| 10111 |  |
|  | 00000 |
|  | 00000 | left, shift the partial product to the right.



Fig. 8-13 Block Diagram of Binary Multiplier

## Binary Multiplier

- Assume that the multiplicand in B, and the multiplier in Q.
- $P$ contains $n$ the length of the multiplier


Fig. 8-14 ASM Chart for Binary Multiplier


## State Table

| Present State |  | Inputs |  | next State |  | Outputs |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| G1 | G0 | s | z | G1 | G0 | то | T1 | T2 | T3 |
| 0 | 0 | 0 | $x$ | 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | X | 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | X | $x$ | 1 | 0 | 0 | 1 | 0 | 0 |
| 1 | 0 | $x$ | x | 1 | 1 | 0 | 0 | 1 | 0 |
| 1 | 1 | $x$ | 0 | 1 | 0 | 0 | 0 | 0 | 1 |
| 1 | 1 | X | 1 | 0 | 0 | 0 | 0 | 0 | 1 |

## Controller Design

- We can use conventional sequential circuit design for the controller, if we did using 2 D type Flip-Flops
$\mathrm{D}_{\mathrm{G} 1}=\mathrm{G}_{1} \mathrm{G}^{\prime}{ }_{0}+\mathrm{G}_{0} \mathrm{G}_{1}^{\prime}+\mathrm{G}_{1} \mathrm{Z}^{\prime}$
$\mathrm{D}_{\mathrm{G} 0}=\mathrm{SG}^{\prime}{ }_{0}+\mathrm{G}_{1} \mathrm{G}^{\prime}{ }_{0}$

$\mathrm{G}_{1} \quad$|  | $?$ | 1 | 1 |
| :--- | :--- | :--- | :--- |
|  | $?$ | 1 | 1 |
| $1 ?$ | $? 1$ |  |  |
| $1 ?$ | $? 1$ | 1 | 1 |

$Z$ is a status signal that
checks P for 0 .

(a) State diagram
$T_{0}$ : Initial state
$T_{1}: A \leftarrow 0, C \leftarrow 0, P \leftarrow n$
$T_{2}: P \leftarrow P-1$
if $\left(Q_{0}\right)=1$ then $\left(A \leftarrow A+B, C \leftarrow C_{\text {out }}\right)$
$T_{3}$ : shift right $C A Q, C \leftarrow 0$
(b) Register transfer operations

Fig. 8-15 Control Specifications for Binary Multiplier


## Sequence Register and Decoder

- If the number of variables is large, conventional design is difficult.
- Need specialized methods for the control design.
- Uses a register to control the states, and a decoder to provide an output corresponding to each of the states.
- A register with $n$ flip-flops can have up to $2^{n}$ states, and $n$-to- $2^{n}$ line decoder has up to $2^{n}$ outputs.


## Sequence Register and Decoder

- The circuit could be obtained directly from the table by inspection (keep in mind that the states are available as inputs).
- Directly from the table, there are three 1 's for $G_{1}$, which means


Fig. 8-17 Logic Diagram of Control for Binary Multiplier Using a Sequence Register and Decoder

## One Flip-Flop per State

- We need n flip-flops for every state
- In this case, we need 4 flip-flops.
- The circuits are very simple to implement and can be obtained directly from the state diagram.
- For example, we move from state 0 to 1 if $\mathrm{S}=1$ which means $\mathrm{D}_{\mathrm{T} 1}=\mathrm{T}_{0} \mathrm{~S}$


## One Flip-Flop per State




Fig. 8-18 One Flip-Flop Per State Controller

## Design with multiplexers

- The previous design consists of flip-flops, decoder, and gates.
- Replacing gates with multiplexers results in a regular pattern of the design.
- First level contains multiplexers (possibly added gates, but only one level.
- The second level is the registers to hold the present state information
- The last stage has a decoder that provides a separate output for every state


Fig. 8-19 Example of ASM Chart with Four Control Inputs

## Multiplexer input condition

| Present State |  | next State |  | I/P | inputs |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| G1 | G0 | G1 | G0 | cond. | MUX1 | MUX2 |
| 0 | 0 | 0 | 0 | w' |  |  |
| 0 | 0 | 0 | 1 | w | 0 | W |
| 0 | 1 | 1 | 0 | x |  |  |
| 0 | 1 | 1 | 1 | $x^{\prime}$ | 1 | x' |
| 1 | 0 | 0 | 0 | y' |  |  |
| 1 | 0 | 1 | 0 | $y z^{\prime}$ | $y z^{\prime}+y z=y$ | yz |
| 1 | 0 | 1 | 1 | yz |  |  |
| 1 | 1 | 0 | 1 | y'z |  |  |
| 1 | 1 | 1 | 0 | y | $y+y^{\prime} z=y+z$ | $y^{\prime} z+y^{\prime} z y=y^{\prime}$ |
| 1 | 1 | 1 | 1 | $y^{\prime} z^{\prime}$ |  |  |



Fig. 8-20 Control Implementation with Multiplexers

## Counting the number of 1's

- The system counts the number of 1's in R1, and set R2 accordingly.
- The bits in R1 are shifted one at a time, checking if the shifted out bit is 1 or 0 , and incrementing R2
- $Z$ is a signal to indicate if R1 contains all 0's or not.
- $E$ is the output of the flip-flop (the shifted out bit).


Fig. 8-21 ASM Chart for Count-of-Ones Circuit

E could not be checked
in the same block as T2
since the shift to E will
not happen unstill the
end of the cucle.


Fig. 8-21 ASM Chart for Count-of-Ones Circuit


Fig. 8-22 Block Diagram for Count-of-Ones

## Control (counting of 1's)

| Present |  | Next |  | Conditions | MUX inputs |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| State |  | State |  |  |  |  |
| G1 | G0 | G1 | G0 |  | MUX1 | MUX2 |
| 0 | 0 | 0 | 0 | $S^{\prime}$ |  |  |
| 0 | 0 | 0 | 1 | S | 0 | S |
| 0 | 1 | 0 | 0 | Z |  |  |
| 0 | 1 | 1 | 0 | $Z^{\prime}$ | $Z^{\prime}$ | 0 |
| 1 | 0 | 1 | 1 |  | 1 | 1 |
| 1 | 1 | 1 | 0 | $E^{\prime}$ |  |  |
| 1 | 1 | 0 | 1 | $E$ | $E^{\prime}$ | $E$ |



Fig. 8-23 Control Implementation for Count-of-Ones Circuit


Fig. P8-10 Control State Diagram for Problems 8-10 and 8-11


