



# Path Testing and Test Coverage

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## Chapter 9



## Structural Testing

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- Also known as glass/white/open box testing
- Structural testing is based on using specific knowledge of the program source text to define test cases
  - Contrast with functional testing where the program text is not seen but only hypothesized



# Structural Testing

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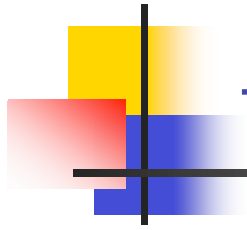
- Structural testing methods are amenable to
  - Rigorous definitions
    - Control flow, data flow, coverage criteria
  - Mathematical analysis
    - Graphs, path analysis
  - Precise measurement
    - Metrics, coverage analysis



## Program Graph - Definition

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- Given a program written in an imperative programming language, its **program graph** is a directed graph in which nodes are statements and statement fragments, and edges represent flow of control

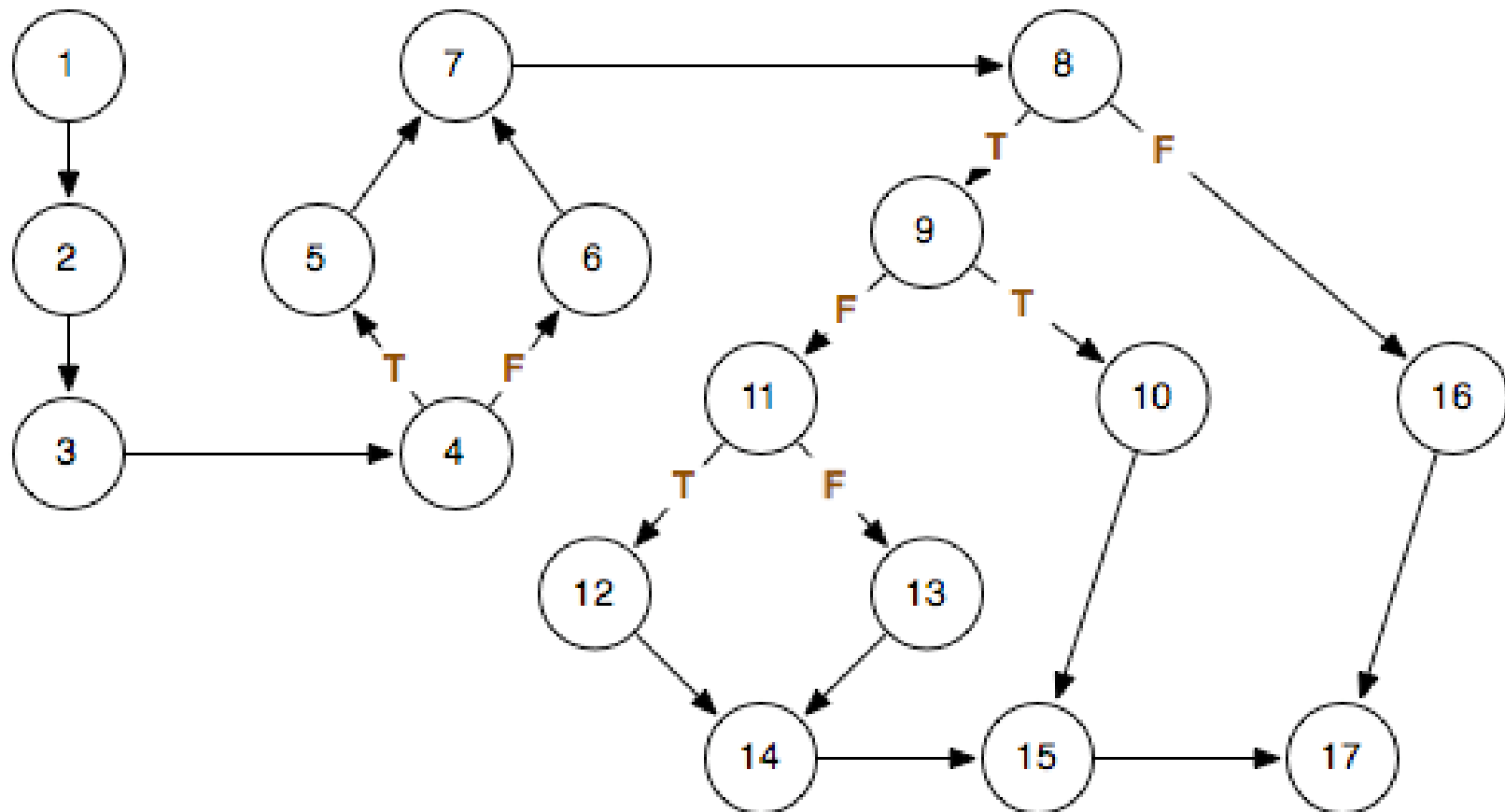


## Triangle program text

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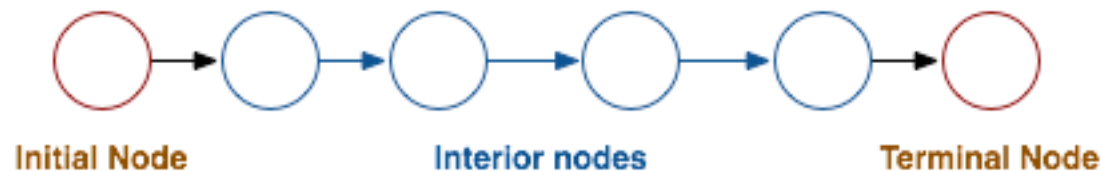
```
1  output ("Enter 3 integers")
2  input (a, b, c)
3  output("Side a,b c: ", a, b, c)
4  if (a < b) and (b < a+c) and (c < a+b)
5  then isTriangle ← true
6  else isTriangle ← false
7  fi
8  if isTriangle
9  then if (a = b) and (b = c)
10         else output ("equilateral")
11         else if (a ≠ b ) and ( a ≠ c ) and ( b ≠ c)
12             then output ("scalene")
13             else output("isosceles")
14         fi
15     fi
16 else output ("not a triangle")
17 fi
```

## Program Graph - Example



## DD-Path – informal definition

- A **decision-to-decision** path (DD-Path) is a path chain in a program graph such that
  - Initial and terminal nodes are distinct
  - Every interior node has  $\text{indeg} = 1$  and  $\text{outdeg} = 1$ 
    - The initial node is 2-connected to every other node in the path
    - No instances of 1- or 3-connected nodes occur





## Connectedness definition

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- Two nodes  $n_1$  and  $n_2$  in a directed graph are
  - 0-connected iff no path exists between them
  - 1-connected iff a semi-path but not path exists between them
  - 2-connected iff a path exists between between them
  - 3-connected iff a path goes from  $n_1$  to  $n_2$  , and a path goes from  $n_2$  to  $n_1$

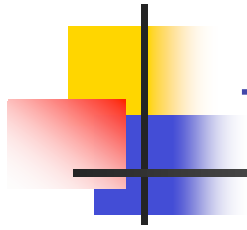




## DD-Path – formal definition

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- A **decision-to-decision** path (DD-Path) is a chain in a program graph such that:
  - Case 1: consists of a single node with  $\text{indeg}=0$
  - Case 2: consists of a single node with  $\text{outdeg}=0$
  - Case 3: consists of a single node with  $\text{indeg} \geq 2$  or  $\text{outdeg} \geq 2$
  - Case 4: consists of a single node with  $\text{indeg} = 1$ , and  $\text{outdeg} = 1$
  - Case 5: it is a maximal chain of length  $\geq 1$
- DD-Paths are also known as **segments**



## Triangle program DD-paths

| Nodes | Path  | Case |
|-------|-------|------|
| 1     | First | 1    |
| 2,3   | A     | 5    |
| 4     | B     | 3    |
| 5     | C     | 4    |
| 6     | D     | 4    |
| 7     | E     | 3    |
| 8     | F     | 3    |
| 9     | G     | 3    |

| Nodes | Path | Case |
|-------|------|------|
| 10    | H    | 4    |
| 11    | I    | 3    |
| 12    | J    | 4    |
| 13    | K    | 4    |
| 14    | L    | 3    |
| 15    | M    | 3    |
| 16    | N    | 4    |
| 17    | Last | 2    |



## DD-Path Graph – informal definition

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- Given a program written in an imperative language, its **DD-Path graph** is a directed graph, in which
  - nodes are DD-Paths of its program graph
  - edges represent control flow between successor DD-Paths.
- Also known as **Control Flow Graph**

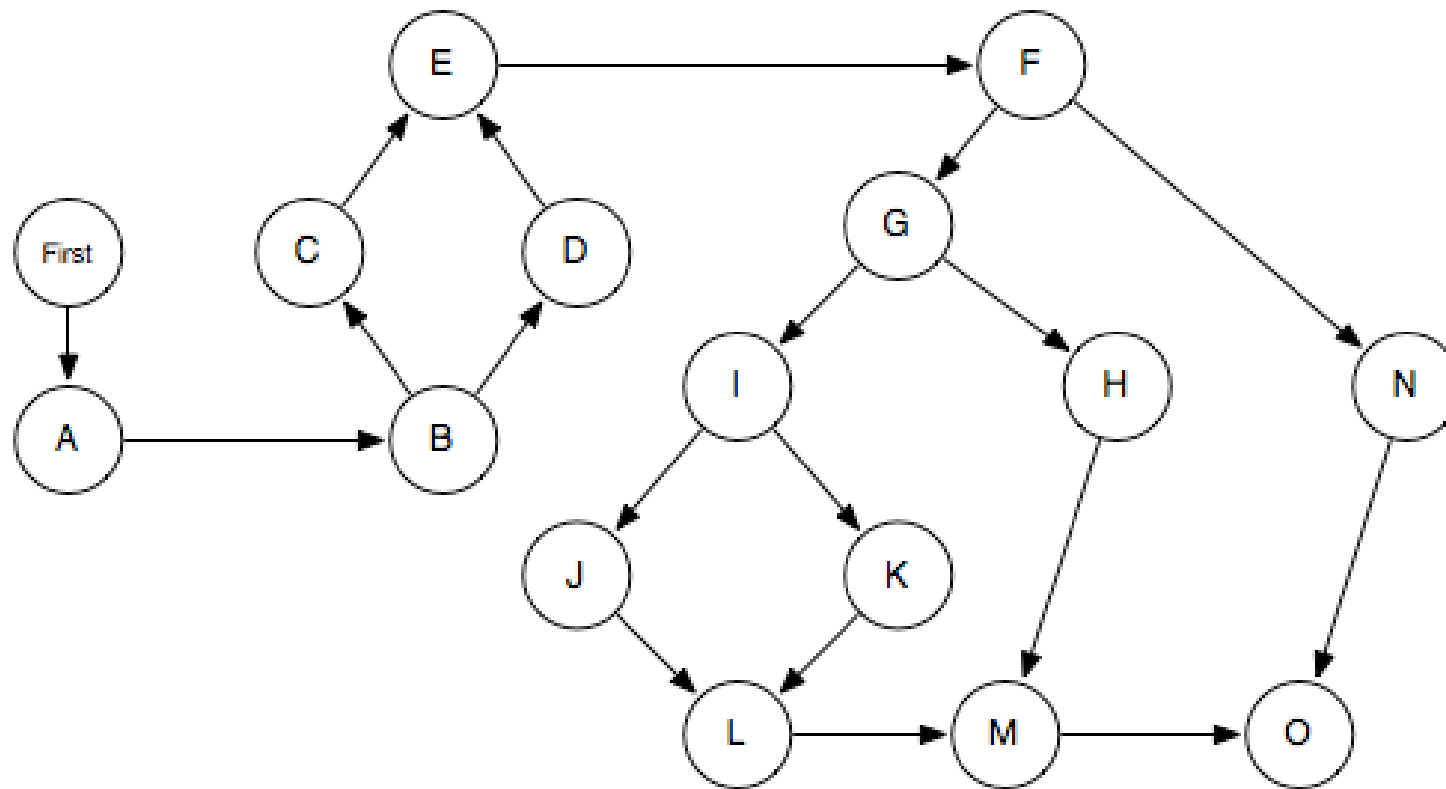


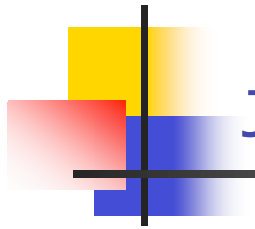
## Control Flow Graph Derivation

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- Straightforward process
- Some judgment is required
- The last statement in a segment must be a predicate, a loop control, a break, or a method exit
- Let's try a couple of examples

## Triangle program DD-path graph





## Java example program

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```
public int displayLastMsg(int nToPrint) {
    np = 0;
    if ((msgCounter > 0) && (nToPrint > 0)) {
        for (int j = lastMsg; ((j != 0) && (np < nToPrint)); --j) {
            System.out.println(messageBuffer[j]);
            ++np;
        }
        if (np < nToPrint) {
            for (int j = SIZE; ((j != 0) && (np < nToPrint)); --j) {
                System.out.println(messageBuffer[j]);
                ++np;
            }
        }
    }
    return np;
}
```



## Java example program – Segments part 1

| Line |   | Segment |
|------|---|---------|
| 1    | public int displayLastMsg(int nToPrint) { |         |
| 2    | np = 0;                                   | A       |
| 3    | if ( (msgCounter > 0)                     | A       |
| 4    | && (nToPrint > 0))                        | B       |
| 5    | { for (int j = lastMsg;                   | C       |
| 6    | ( ( j != 0)                               | D       |
| 7    | && (np < nToPrint));                      | E       |
| 8    | --j)                                      | F       |
| 9    | { System.out.println(messageBuffer[j]);   | F       |
| 10   | ++np;                                     | F       |
| 11   | }   | F       |

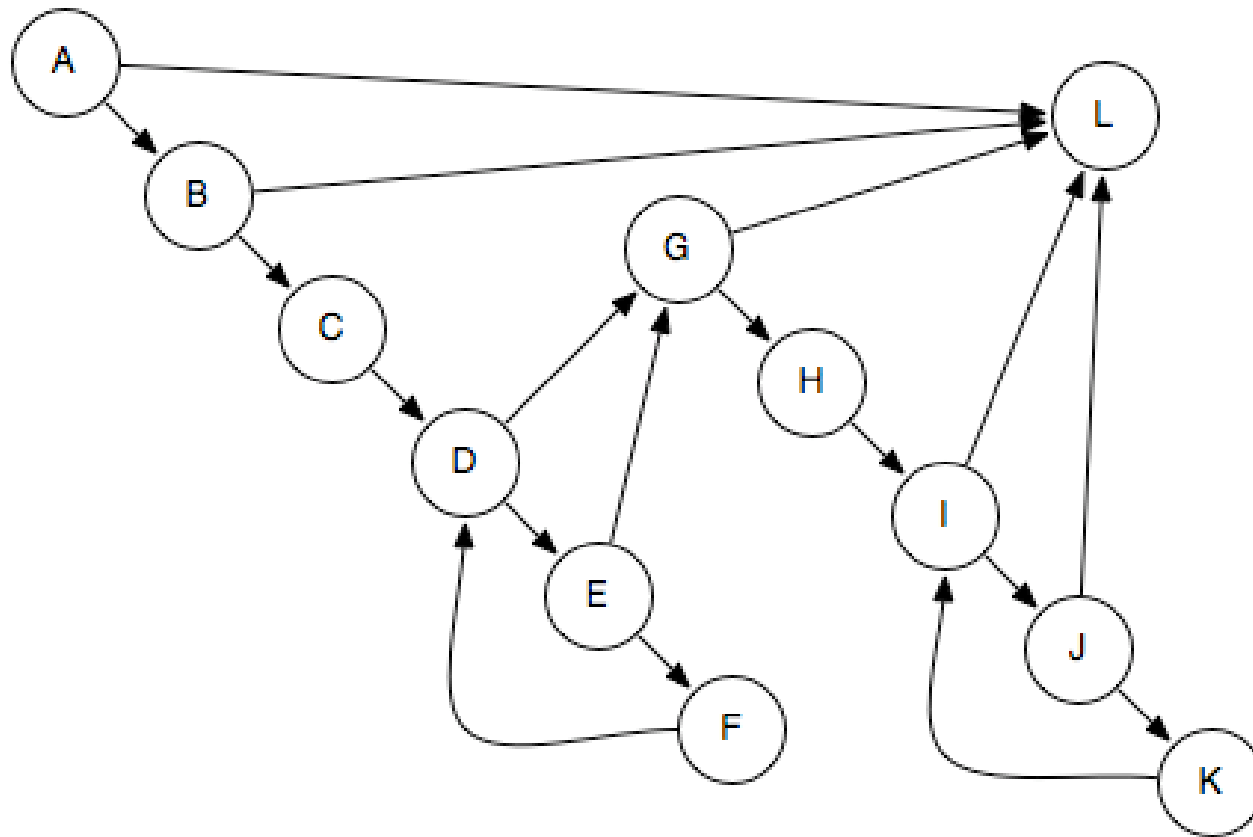


## Java example program – Segments part 2

| Line |  | Segment |
|------|--|---------|
| 12   | <code>if (np &lt; nToPrint)</code>                   | G       |
| 13   | <code>{ for (int j = SIZE;</code>                    | H       |
| 14   | <code>((j != 0) &amp;&amp;</code>                    | I       |
| 15   | <code>(np &lt; nToPrint));</code>                    | J       |
| 16   | <code>--j)</code>                                    | K       |
| 17   | <code>{ System.out.println(messageBuffer[j]);</code> | K       |
| 18   | <code>++np;</code>                                   | K       |
| 19   | <code>}</code>                                       | L       |
| 20   | <code>}</code>                                       | L       |
| 21   | <code>}</code>                                       | L       |
| 22   | <code>return np;</code>                              | L       |
| 23   | <code>}</code>                                       | L       |



## Java example program displayLastMsg – DD-path graph





## DD graphs definition – 1

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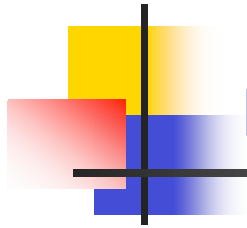
- Depict which program segments may be followed by others
- A segment is a node in the CFG
- A conditional transfer of control is a **branch** represented by an edge
- An **entry node** (no inbound edges) represents the entry point to a method
- An **exit node** (no outbound edges) represents an exit point of a method



## DD graphs definition – 2

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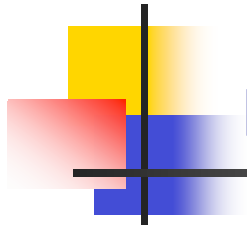
- An **entry-exit path** is a path from the entry node to the exit node
- **Path expressions** represent paths as sequences of nodes
- Loops are represented as segments within parentheses followed by an asterisk
- There are 22 different path expressions in our example



## Path expressions – part 1

### Entry-Exit path

|    |                                       |
|----|---------------------------------------|
| 1  | A L                                   |
| 2  | A B L                                 |
| 3  | A B C D G L                           |
| 4  | A B C D E G L                         |
| 5  | A B C (D E F)* D G L                  |
| 6  | A B C (D E F)* D E G L                |
| 7  | A B C D G H I L                       |
| 8  | A B C D G H I J L                     |
| 9  | A B C D G H (I J K)* I L              |
| 10 | A B C (D E F)* D E G H (I J K)* I J L |
| 11 | A B C D E G H I L                     |



## Path expressions – part 2

### Entry-Exit path

|    |                                       |
|----|---------------------------------------|
| 12 | A B C D E G H I J L                   |
| 13 | A B C D E G H (I J K)* I L            |
| 14 | A B C D E G H (I J K)* I J L          |
| 15 | A B C (D E F)* D G H I L              |
| 16 | A B C (D E F)* D G H I J L            |
| 17 | A B C (D E F)* D G H (I J K)* I L     |
| 18 | A B C (D E F)* D G H (I J K)* I J L   |
| 19 | A B C (D E F)* D E G H I L            |
| 20 | A B C (D E F)* D E G H I J L          |
| 21 | A B C (D E F)* D E G H (I J K)* I L   |
| 22 | A B C (D E F)* D E G H (I J K)* I J L |

## Paths displayLastMsg – decision table – part 1

### Path condition by Segment Name

|    | Branch Coverage            | A | B | D   | E   | G   | I   | J |
|----|----------------------------|---|---|-----|-----|-----|-----|---|
| 1  | A L                        | F | – | –   | –   | –   | –   | – |
| 2  | A B L                      | T | F | –   | –   | –   | –   | – |
| 3  | A B C D G L                | T | T | F   | –   | F   | –   | – |
| 4  | A B C D E G L              | T | T | T   | F   | –   | –   | – |
| 5  | A B C (D E F)* D G L       | T | T | T/F | T/– | F   | –   | – |
| 6  | A B C (D E F)* D E G L     | T | T | T/T | T/F | F   | –   | – |
| 7  | A B C D G H I L            | T | T | F   | –   | T   | F   | – |
| 8  | A B C D G H I J L          | T | T | F   | –   | T   | T   | F |
| 9  | A B C D G H (I J K)* I L   | T | T | F   | –   | T/F | T/– | T |
| 10 | A B C D G H (I J K)* I J L | T | T | F   | –   | T/T | T/F | T |
| 11 | A B C D E G H I L          | T | T | T   | F   | T   | F   | – |

x/x Conditions at loop entry and exit

## Branch coverage – decision table example – part 2

### Path condition by Segment Name

|    | Branch Coverage                       | A | B | D   | E   | G | I   | J   |
|----|---------------------------------------|---|---|-----|-----|---|-----|-----|
| 12 | A B C D E G H I J L                   | T | T | T   | F   | T | T   | F   |
| 13 | A B C D E G H (I J K)* I L            | T | T | T   | F   | T | T/F | T/- |
| 14 | A B C D E G H (I J K)* I J L          | T | T | T   | F   | T | T/T | T/F |
| 15 | A B C (D E F)* D G H I L              | T | T | T/F | T/- | T | F   | -   |
| 16 | A B C (D E F)* D G H I J L            | T | T | T/T | T/F | T | T   | F   |
| 17 | A B C (D E F)* D G H (I J K)* I L     | T | T | T/F | T/- | T | T/F | T/- |
| 18 | A B C (D E F)* D G H (I J K)* I J L   | T | T | T/F | T/- | T | T/T | T/F |
| 19 | A B C (D E F)* D E G H I L            | T | T | T/T | T/F | T | F   | -   |
| 20 | A B C (D E F)* D E G H I J L          | T | T | T/T | T/F | T | T   | F   |
| 21 | A B C (D E F)* D E G H (I J K)* I L   | T | T | T/T | T/F | T | T   | T   |
| 22 | A B C (D E F)* D E G H (I J K)* I J L | T | T | T/T | T/F | T | T   | T   |

x/x Conditions at loop entry and exit



## Program text coverage Metrics

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- $C_0$  Every Statement
- $C_1$  Every DD-path
- $C_{1p}$  Every predicate to each outcome
- $C_2$   $C_1$  coverage + loop coverage
- $C_d$   $C_1$  coverage + every dependent pair of DD-paths
- $C_{MCC}$  Multiple condition coverage
- $C_{ik}$  Every program path that contains k loop repetitions
- $C_{stat}$  Statistically significant faction of the paths
- $C_\infty$  Every executable path





## Program text coverage models

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- Statement Coverage
- Segment Coverage
- Branch Coverage
- Multiple-Condition Coverage



## Statement coverage – $C_0$

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- Achieved when all statements in a method have been executed at least once
- A test case that will follow the path expression below will achieve statement coverage in our example

**A B C (D E F)\* D G H (I J K)\* I L**

- One test case is enough to achieve statement coverage!



## Segment coverage

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- **Segment coverage** counts segments rather than statements
- May produce drastically different numbers
  - Assume two segments P and Q
  - P has one statement, Q has nine
  - Exercising only one of the segments will give 10% or 90% statement coverage
  - Segment coverage will be 50% in both cases



## Statement coverage problems

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- Predicate may be tested for only one value (misses many bugs)
- Loop bodies may only be iterated once
- Statement coverage can be achieved without branch coverage. Important cases may be missed

```
String s = null;  
if (x != y) s = "Hi";  
String s2 = s.substring(1);
```



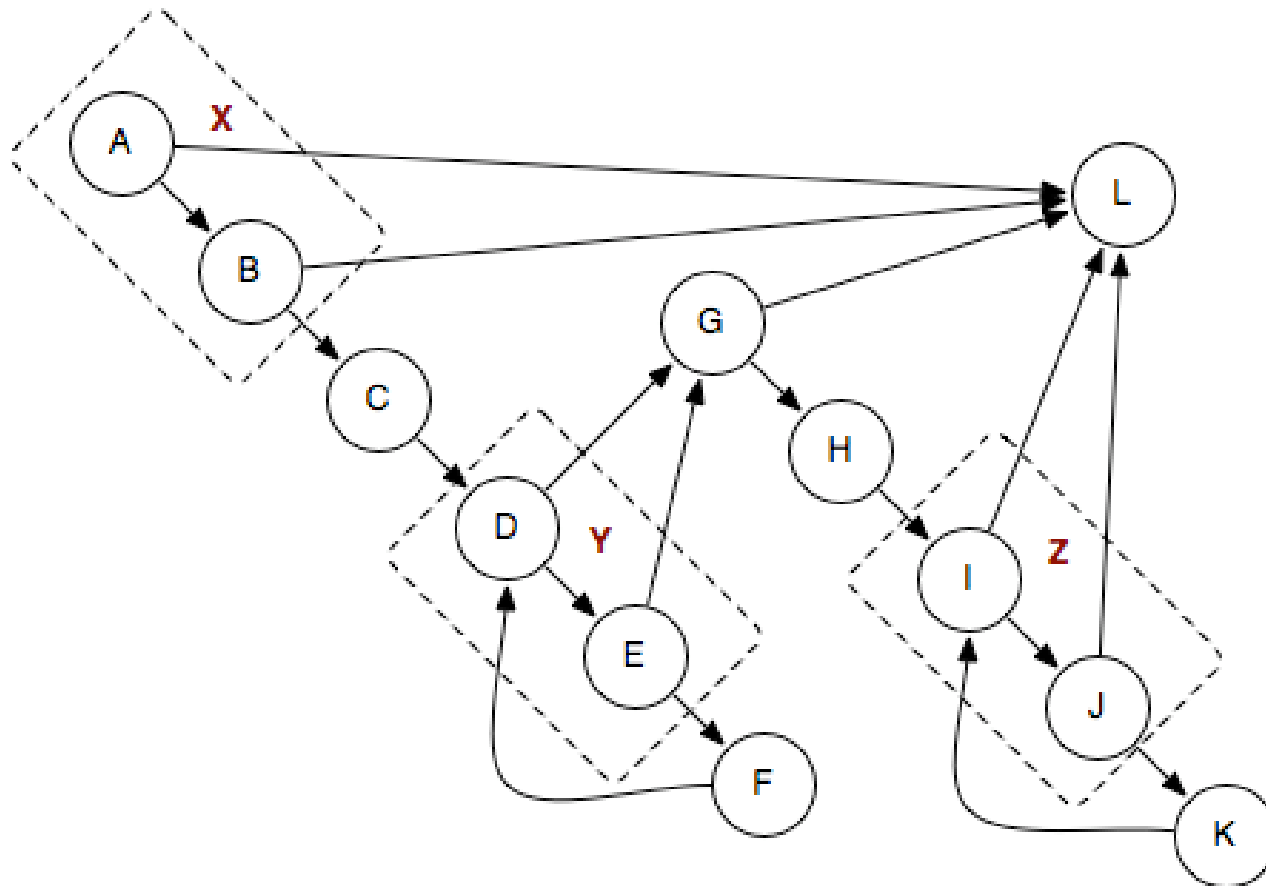
## Branch coverage – $C_{1p}$

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- Achieved when every path from a node is executed at least once
- At least one true and one false evaluation for each predicate
- Can be achieved with  $D+1$  paths in a control flow graph with  $D$  2-way branching nodes and no loops
  - Even less if there are loops
- In the Java example displayLastMsg branch coverage is achieved with three paths – see next few slides

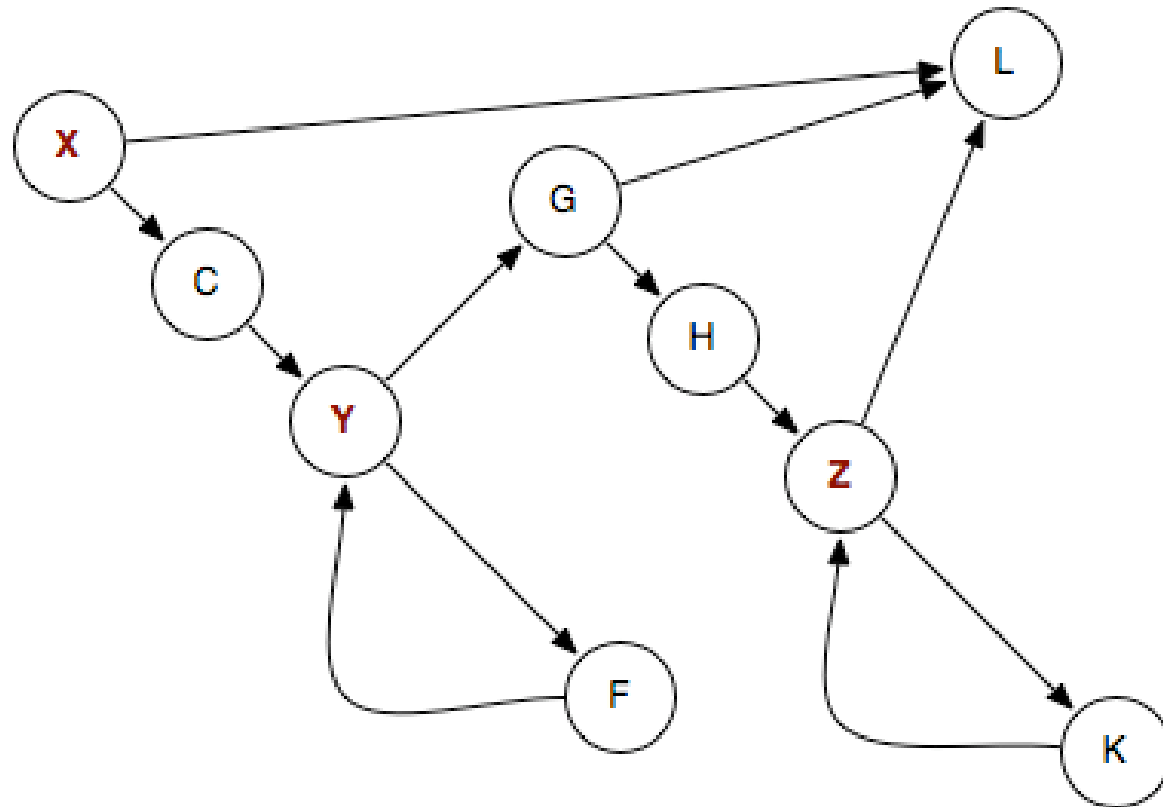
**X L**  
**X C (Y F)\* Y G L**  
**X C (Y F)\* Y G H (Z K)\* Z L**

## Java example program displayLastMsg – DD-path graph



**X, Y & Z are shorthand for the nodes within the dotted boxes; used for branch testing**

# Java example program displastLastMsg – aggregate predicate DD-path graph



## Paths aggregate – decision table – part 1

### Path condition by Segment Name

|    | Branch Coverage      | A | B | D   | E   | G   | I   | J |
|----|----------------------|---|---|-----|-----|-----|-----|---|
| 1  | X L                  | F | – | –   | –   | –   | –   | – |
| 2  | X L                  | T | F | –   | –   | –   | –   | – |
| 3  | X C Y G L            | T | T | F   | –   | F   | –   | – |
| 4  | X C Y G L            | T | T | T   | F   | –   | –   | – |
| 5  | X C (Y F)* Y G L     | T | T | T/F | T/– | F   | –   | – |
| 6  | X C (Y F)* Y G L     | T | T | T/T | T/F | F   | –   | – |
| 7  | X C Y G H Z L        | T | T | F   | –   | T   | F   | – |
| 8  | X C Y G H Z L        | T | T | F   | –   | T   | T   | F |
| 9  | X C Y G H (Z K)* I L | T | T | F   | –   | T/F | T/– | T |
| 10 | X C Y G H (Z K)* I L | T | T | F   | –   | T/T | T/F | T |
| 11 | X C Y G H Z L        | T | T | T   | F   | T   | F   | – |

x/x Conditions at loop entry and exit



## Branch coverage – decision table example – part 2

### Path condition by Segment Name

|    | Branch Coverage             | A | B | D   | E   | G | I   | J   |
|----|-----------------------------|---|---|-----|-----|---|-----|-----|
| 12 | X C Y G H Z L               | T | T | T   | F   | T | T   | F   |
| 13 | X C Y G H (Z K)* Z L        | T | T | T   | F   | T | T/F | T/- |
| 14 | X C Y G H (Z K)* Z L        | T | T | T   | F   | T | T/T | T/F |
| 15 | X C (Y F)* Y G H Z L        | T | T | T/F | T/- | T | F   | -   |
| 16 | X C (Y F)* Y G H Z L        | T | T | T/T | T/F | T | T   | F   |
| 17 | X C (Y F)* Y G H (Z K)* Z L | T | T | T/F | T/- | T | T/F | T/- |
| 18 | X C (Y F)* Y G H (Z K)* Z L | T | T | T/F | T/- | T | T/T | T/F |
| 19 | X C (Y F)* Y G H Z L        | T | T | T/T | T/F | T | F   | -   |
| 20 | X C (Y F)* Y G H Z L        | T | T | T/T | T/F | T | T   | F   |
| 21 | X C (Y F)* Y G H (Z K)* Z L | T | T | T/T | T/F | T | T   | T   |
| 22 | X C (Y F)* Y G H (Z K)* Z L | T | T | T/T | T/F | T | T   | T   |

x/x Conditions at loop entry and exit



## Branch coverage problems

- Ignores implicit paths from compound paths
  - 11 paths in aggregate model vs 22 in full model
- Short-circuit evaluation means that many predicates might not be evaluated
  - A compound predicate is treated as a single statement. If  $n$  clauses,  $2^n$  combinations, but only 2 are tested
- Only a subset of all entry-exit paths is tested
  - Two tests for branch coverage vs 4 tests for path coverage
    - $a = b = x = y = 0$  and  $a = x = 0 \wedge b = y = 1$

```
if (a == b) x++;  
if (x == y) x--;
```



## Multiple-condition coverage

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- All true-false combinations of simple conditions in compound predicates are considered at least once
  - Guarantees statement, branch and predicate coverage
  - Does not guarantee path coverage
- A truth table may be necessary
- Not necessarily achievable due to lazy evaluation or mutually exclusive conditions

```
if ((x > 0) && (x < 5)) ...
```



## Dealing with Loops

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- Loops are highly fault-prone, so they need to be tested carefully
- Simple view: Every loop involves a decision to traverse the loop or not
- A bit better: Boundary value analysis on the index variable
- Nested loops have to be tested separately starting with the innermost
- Once loops have been tested then can be condensed to a single node



## Basis path testing

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- For a vector space a basis set of vectors can be constructed
  - As a consequence every vector in the space is a linear combination of the basis vectors
- By analogy a basis set of paths can be constructed for a DD-path graph
- Problems
  - One cannot assume that testing the basis set is sufficient
  - Basis sets assume independence of members but program text paths are dependent
    - Analogous to variable dependencies causing problems for boundary value testing



## Essential complexity

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- The cyclomatic number for a graph is given by
  - $CN(G) = e - v + c$ 
    - e number of edges      v number of vertices  
c number of strongly connected components
      - **For strongly connected, need to add edges from every sink to every source**
- Condensation graphs are based on removing strong components or DD-paths
- For programs remove structured program constructs
  - One entry, one exit constructs for sequences, choices and loops
  - Each structured component once tested can be replaced by a single node when condensing its graph



## Essential complexity – 2

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- Program text that violates proper structure has
  - Branches either into or out of the middle of a loop
  - Branches either into or out of then and else phrases of if...then...else statements
  - This increases the cyclomatic number – i.e. the complexity of the program
- The higher the cyclomatic number the more tests are required.
  - If complexity is too high
    - Simplify the program rather than do more testing



## Guidelines

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- Functional testing is too far from the program text
- Path testing is too close to the program text
  - Obscures feasible and infeasible paths
    - Use dataflow testing to move out a bit
- Path testing
  - does not give good help in finding test cases
  - does give good measures of quality of testing through coverage analysis
  - Basis path testing gives a lower bound on the number of tests





## Guidelines – 2

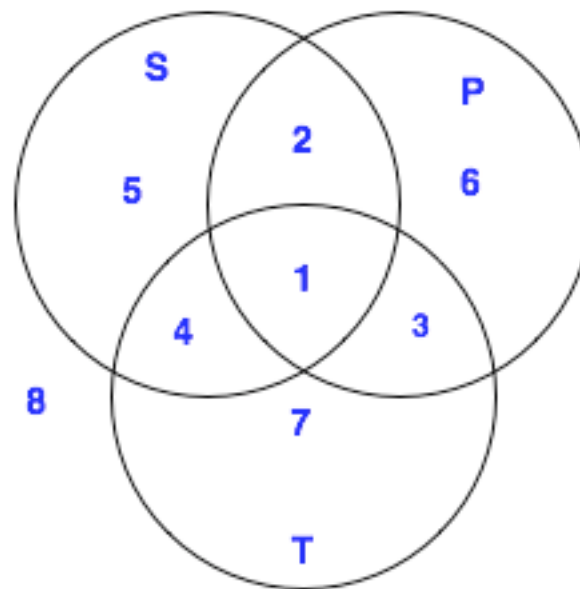
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- Path testing
  - Provides set of metrics that cross-check functional testing
  - Use to resolve gap and redundancy questions
    - Missing DD-paths – have gaps
    - Repeated DD-paths – have redundancy
- Distinctions are made with the following types of paths
  - Feasible – infeasible
  - Specified – unspecified
  - Topologically possible – impossible

## Guidelines – 3

- Re-examine the Venn diagram in the context of path testing

Specified  
behaviour



Programmed behaviour  
– feasible paths

Topologically possible paths