

Exercise #8

Due: March 18, 2008

8. Consider an asynchronous system of n processes, where processes may experience halting failures.

We can define the **1-2-Counter** type as follows. The state of the object stores a natural number. It provides three operations: **READ** returns the state of the object without changing it, **INC** increases the state of the object by 1 and returns **ack**, **INC-BY-2** increases the state of the object by 2 and returns **ack**.

- (a) Here is a proposed implementation of a **1-2-Counter** for n processes from n shared **read/write registers**, $A[1], \dots, A[n]$. Process i would execute the following code to perform an operation on the **1-2-counter**. (Here, x and v are local variables of the process performing the operation.)

```

READ
  v ← 0
  for j ← 1 to n
    v ← v + A[j] % this is a read of register A[j]
  end for
  return v
end READ

```

```

INC
  x ← A[i] % This is a read of register A[i]
  A[i] ← x + 1 % This is a write to register A[i]
end INC

```

```

INC-BY-2
  x ← A[i] % This is a read of register A[i]
  A[i] ← x + 2 % This is a write to register A[i]
end INC-BY-2

```

Prove this is *not* a linearizable implementation.

- (b) Is there a wait-free, linearizable implementation of a **1-2-counter** from registers? Prove your answer is correct.
- (c) Is there a non-blocking, linearizable, anonymous implementation of a **1-2-counter** from registers? Prove your answer is correct. Hint: think about what happens when two processes trying to do the same operation run at exactly the same speed.