

Multiple Value Functions

(see Wilensky Chapter 16.4)

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adapted from Gunnar Gotshalks

multiple value functions

- in other languages, one can return multiple values on one call
 - e.g. in C, using *call by reference* (pointers)
- but in Lisp, all parameters are passed by value
 - they cannot be changed
- to return multiple values in Lisp
 - need to construct and return a list of the results you want the function to return (**this is costly!**)
 - the caller must extract, through `car` and `cdr` the values of interest (**inconvenient**)
 - this occurs frequently enough that Lisp permits multiple values to be returned by some special functions/macros

catching multiple values

- by default, if a function returns multiple values
 - only one is passed back, the rest are discarded
 - unless you specifically ask for the other values
- e.g. `(round aNumber)` returns two values
 - the rounded value and
 - the value needed to add to the rounded result to get the original number
- `(round aNumber) → roundedValue; difference`
where, `difference = aNumber - roundedValue`
- `(round 7.6) → 8; -0.4`
 - not a list! `(car (round 7.6))` fails
 - `(print (round 7.6)) → 8`
uses first value by default

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catching multiple values (cont'd)

- use the following macro to create a list of multiple value returns
 - `(multiple-value-list (round aNumber))`
→ `(roundedValue restoreNumber)`
 - `(multiple-value-list (round 7.6)) → (8 -0.4)`
- can assign the values to symbols using the following macro
 - `(multiple-value-setq (val diff) (round 7.6))`
 - `8 → val` and `-0.4 → diff`
 - note `setq` implies global symbol

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catching multiple values (cont'd)

- can create a local context for variables instead of using global variables

```
(let ((val nil) (diff nil))
  (multiple-value-setq (val diff) (round 7.6))
  ;; ... use val and diff in list of forms
  (print val)
  (print diff)
  (print (+ val diff))
)
```

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catching multiple values (cont'd)

- the following shows that let is syntactic sugar for a lambda function

```
- ( (lambda ( val diff )
    (multiple-value-setq (val diff) (round 7.6))
    ;; ... use val and diff in list of forms
    (print val)
    (print diff)
    (print (+ val diff))
  )
  nil nil ;; initial values for val & diff
)
```

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catching multiple values (cont'd)

- instead of using `let` which needs initial values for its parameters, can use the following

```
( multiple-value-bind (val diff) (round 7.6)
  ;; ... list of forms using val and diff ...
  ( print val )
  ( print diff )
  ( print ( + val diff ) )
)
```

catching multiple values (cont'd)

- consider the following:

```
(defun functionName (val diff)
  (print val) (print diff) (print (+ val diff))
)
```
- suppose we want to pass the values returned by `round` to `functionName`

```
(functionName (round 7.6))
```
- but ordinary cLisp argument handling mechanism only passes a single value from a form to a function

catching multiple values (cont'd)

- can use the following to pass the return values to a function
 - its arity equals the number of returned values

- (multiple-value-call

- #'functionName (round 7.6))

```
(defun functionName (val diff)
  (print val) (print diff) (print (+ val diff))
)
```

generating multiple values

- the last form in a function is a call to **values**

- (values 1 2 3) → 1; 2; 3

- here is a function to tear a list into its first and rest parts

```
(defun unCons ( theList )
  (values ( car theList ) ( cdr theList ) )
)
```

```
(uncons '( a b c ) ) → a; ( b c )
```

- what about unconsing an entire list? use **apply** to strip the outer level of parenthesis

```
(apply 'values '(a b c d e)) ==> a; b; c; d; e
```

generating multiple values (cont'd)

- can use `values` (with no arguments) to build a Lisp function that returns no values at all
 - the last statement of the function: `(values)`
 - useful if a function is used only for its side-effects
 - Lisp supplies a gratuitous value of `nil` if such a function is used in a context where it is not anticipated
 - e.g. `(print (values))` → `nil`

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consequences of passing around multiple values

- has some consequences on the design of a Lisp system
- recall: code that does not anticipate multiple values ignores all but the first value
- however, most built-in functions/macros that tends to return the values of other forms are set up to handle multiple values
 - e.g. `cond`, `let`, ... passes multiple values
 - `and`, `or` passes multiple values from the last sub-forms
 - `(and nil (values 3 4))` → `nil`
`(and t (values 3 4))` → `3; 4`, `(and (values 1 2) t)` → `t`

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Pattern Matching

(see Wilensky Chapter 21)

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pattern matching

- a ubiquitous function in intelligence is pattern matching
 - e.g. IQ tests often contain pattern matching problems
 - pattern matching means to compare one object with another object and recognize if they are similar
 - basic case is comparing constants
 - more interesting is to compare parameterized patterns
 - > A is like B except for
 - > A is like B where ...
- (a statement that sub-objects, while not identical, correspond to each other)

applications

- to classify data
 - whether it has a certain property
- AI applications
 - e.g. to extract information from natural language like text
 - “John hit Mary” → (hurt Mary)

criterion for similarity

- when can we consider two patterns to be similar?
 - exact match
 - the first two items are the same
 - the last item is the same
 - ...
- we want to build a generic pattern matcher
 - can't decide in advance what criterion to use
 - rather, provide a fairly general scheme and later implement different criteria for different applications
 - one way to achieve this → introduce **pattern matching variables**

what is a pattern?

- in Lisp, a pattern is a form (s-expression) that contains
 - constants – called literals
 - pattern matching variables
- we need a syntax to differentiate the two
 - can prefix pattern matching variables with ?
 - e.g. ?x ?abc
- an abstract pattern could look like
 - (a b ?x c ?y)
- a more meaningful pattern could be
 - (causes (hit ?x ?y) (hurt ?y))
 - interpreted as – x hitting y, causes y to be hurt

pattern variable representation

- how will we represent pattern matching variables in Lisp?
 - the rest is simply a list with symbols for the constants
- use the construct (***VAR*** X)
 - where ***VAR*** is a special symbol we recognize within the matcher program

when do two patterns match?

- two patterns can be matched when it is possible to **unify** them
- unification (a term borrowed from theorem proving) means an assignment can be made to the variables in each pattern such that the patterns become identical
 - we usually mean the most general possible assignment
- an assignment is shown by the pair (**variable value**)
 - ((*VAR* X) abc)
 - ((*VAR* X) (*VAR* Y))

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unification examples – 1

- (a ?x b)
(a y b) match if ?x <-- y
we say that ?x is bound to y
- (a ?x b)
(a ?y b) match if ?x <-- ?y
- (a ?x (b ?z))
(a (((e))) ?y) match if ?x <-- (((e)))
?y <-- (b ?z)

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unification examples – 2

- more complex examples
 - (a ?x ?x) match if ?x = ?y
 (a ?y c) and ?y = c
 - cannot naively bind ?x to ?y and then ?x to c as then we are trying to assign two different values to ?x
 - need to substitute ?y for ?x and then see that ?y binds to c
 - (a ?x ?x ?x)
 (a ?y ?y ?y)
 - cannot naively try to bind ?x to ?y, as on the second attempt, we end up binding ?y to ?y, then on the third attempt, we have an infinite loop

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unification examples – 3

- more complex examples
 - (a ?x ?x) there is no consistent
 (a ?y (b ?y)) binding to make a match
 - again need to prevent an infinite loop

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pattern variable input

- how do we represent input?
 - we would like to keep the notation `?x`
 - instruct the read program to recognize the construct `?symbol` and create the list `(*VAR* symbol)`
`(set-macro-character #\? ;;see page 245`
`#'(lambda (stream char)`
`(list '*var* (read stream t nil t))))`
 - test with `(read)`, enter `'?x` and see `(*VAR* x)` as the result

pattern matcher output

- need to distinguish three cases (see p369 for a discussion)
 - no match is possible
→ output is `nil`
 - match is possible but no variable bindings are required
→ output is `T ; nil` – two values returned
 - match is possible with variable bindings
→ output is `T ; (list of bindings)`
 - a binding is a pair `((*VAR* variable) value)`
- example with a binding required
 - `(match '(a ?x c ?y e) '(a b ?z d e))`
→ `T ; (((*VAR* Y) D) ((*VAR* Z) C) ((*VAR* X) B))`

matcher

- reminder that we need to define the macro character ?

```
(set-macro-character #\  
  #'( lambda ( stream char )  
        ( list '*var* ( read stream t nil t ) )))
```

- the entry function creates the initial empty binding

```
(defun match ( pattern1 pattern2 )  
  (match-with-bindings pattern1 pattern2 nil ))
```

matching cases

- matching two patterns requires a recursive descent into the patterns to match sub-patterns; the following cases can occur
 - pattern1 – a variable, an atom, a list
 - pattern2 – a variable, an atom, a list

matching cases (cont'd)

- the matching program has to examine the possible combinations
- | pattern1 | pattern2 | result |
|----------|----------|-------------------------------------|
| atom | atom | match if equal, else no match |
| atom | variable | try to bind atom to variable |
| atom | list | no match |
| variable | atom | try to bind atom to variable |
| variable | variable | try to bind variable to variable |
| variable | list | try to bind list to variable |
| list | atom | no match |
| list | variable | try to bind list to variable |
| list | list | recursive descent on first and rest |

match with bindings

- organize when bindings need to be done
- ```
(defun match-with-bindings (pattern1 pattern2 bindings)
 (cond
 ;; pattern 1 is a variable?
 ((pattern-var-p pattern1)
 (variable-match pattern1 pattern2 bindings))
 ;; pattern 2 is a variable?
 ((pattern-var-p pattern2)
 (variable-match pattern2 pattern1 bindings))
 ;; pattern 1 is an atom? note use of values
 ((atom pattern1)
 (if (eq pattern1 pattern2) (values t bindings)))
 ;; pattern 2 is an atom?
 ((atom pattern2) nil)
```

## match with bindings (cont'd)

---

```
;; pattern1 and pattern2 are both lists – use recursion and
multiple values
(t
 (multiple-value-bind (flag carbindings)
 (match-with-bindings (car pattern1)
 (car pattern2)
 bindings)
 (and flag
 (match-with-bindings (cdr pattern1)
 (cdr pattern2)
 carbindings)
)))
```

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## variable match

---

- find a binding for `pattern-var` within `item` using the current `bindings`
- `(defun variable-match (pattern-var item bindings)`
  - ;; check for equality – no additional bindings are necessary
  - `(if (equal pattern-var item) (values t bindings)`
  - ;; otherwise ...

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## variable match (cont'd)

---

- need a binding
- ```
(let ((var-binding ;; determine if a binding already exists
      (get-binding pattern-var bindings)))
    ;; handle the case where a binding exists
    (cond (var-binding
           (match-with-bindings var-binding item bindings))
          ;; no binding for the variable – check for circularity –
          ;; need to see if the pattern-var occurs in item or is
          ;; bound to a variable in item
          ((not (contained-in pattern-var item bindings))
           (values t
                  (add-binding pattern-var item bindings))))
    )
  )))
```

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contained-in

- check for circularity by – seeing if `pattern-var` occurs in `item` or is defined as the value of a binding of a variable in `item`
- ```
(defun contained-in (pattern-var item bindings)
 ;; cannot be contained in an atom
 (cond ((atom item) nil)
 ;; check if item is a variable
 ((pattern-var-p item)
 ;; does pattern-var occur in item
 (or (equal pattern-var item)
 ;; does pattern-var occur as the value of a binding?
 (contained-in pattern-var
 (get-binding item bindings)
 bindings)))
))
```

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## contained-in (cont'd)

---

```
;; the item is a list so recursively check for contained-in
(t
 (or (contained-in pattern-var (car item)
 bindings)
 (contained-in pattern-var (cdr item)
 bindings))
))
```

## matcher – housekeeping functions

---

- add the binding to the current **bindings** (a list of 2 element lists)  

```
(defun add-binding (pattern-var item bindings)
 (cons (list pattern-var item) bindings))
```
- if **item** is a pattern variable return true, else return false  

```
(defun pattern-var-p (item)
 (and (listp item) (eq '*var* (car item))))
```
- get the binding, if any, for **pattern-var** in the binding list **bindings**  

```
(defun get-binding (pattern-var bindings)
 (cadr (assoc pattern-var bindings :test #'equal)))
```

# info

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- class test 1 on June 11
  - closed book exam
  - syllabus: everything covered up to and including multiple value functions
  - bring York photo ID
- good luck!