

## **Constraint Satisfaction Problems**

- Many problems can be represented as a search for a vector of feature values.
  - k-features: variables.
  - Each feature has a value. Domain of values for the variables.
  - e.g., height = {short, average, tall}, weight = {light, average, heavy}.
- In these problems the problem is to search for a set of values for the features (variables) so that the values satisfy some conditions (constraints).

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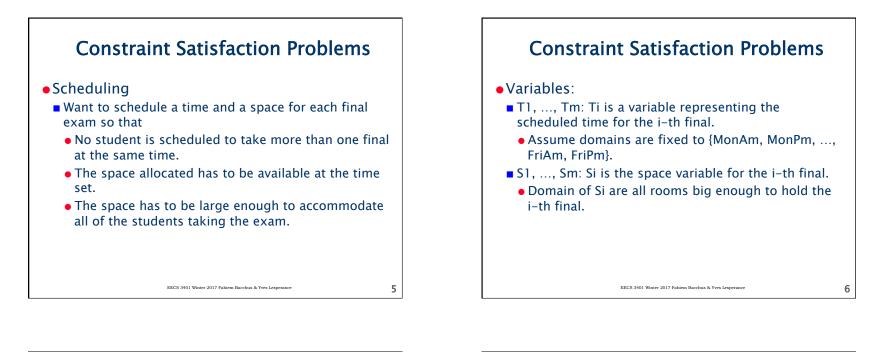
**Constraint Satisfaction Problems** 

• Sudoku:

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- 81 variables, the value in each cell.
- Values: a fixed value for those cells that are already filled in, the values {1-9} for those cells that are empty.
- Solution: a value for each cell satisfying the constraints:
  - no cell in the same column can have the same value.
  - no cell in the same row can have the same value.
- no cell in the same sub-square can have the same value.

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- Want to find an assignment of values to each variable (times, rooms for each final), subject to the constraints:
  - For all pairs of finals i, j such that there is a student taking both:
    - Ti ≠ Tj
  - For all pairs of finals i, j
    - Ti  $\neq$  Tj or Si  $\neq$  Sj
    - either i and j are not scheduled at the same time, or if they are they are not in the same space.

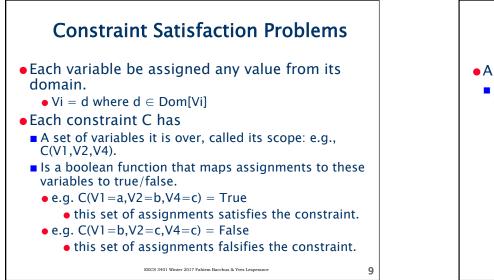
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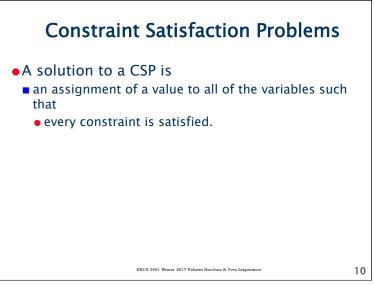
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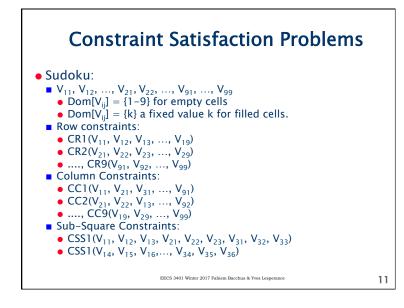
## Constraint Satisfaction Problems (CSP)

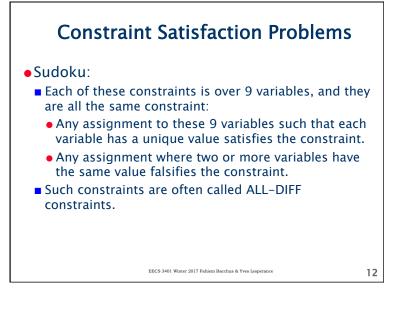
- More formally.
- A CSP consists of
- a set of variables V1, ..., Vn
- for each variable a domain of possible values Dom[Vi].
- A set of constraints C1,..., Cm.

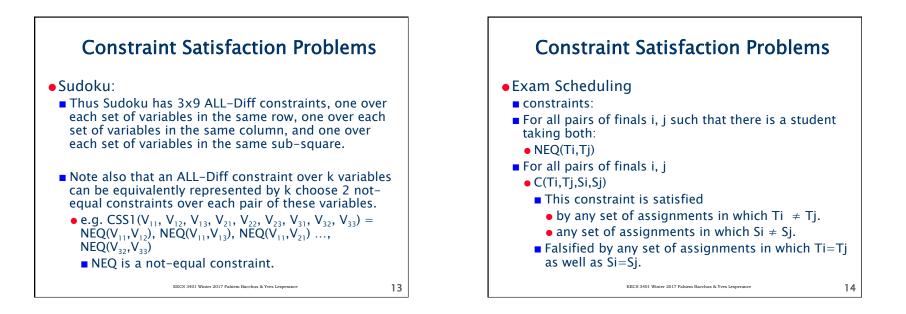
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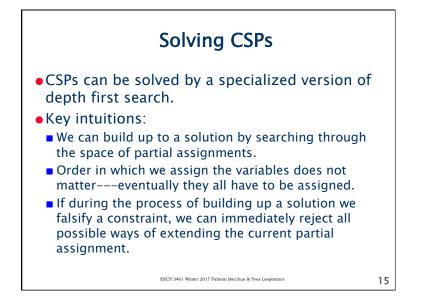


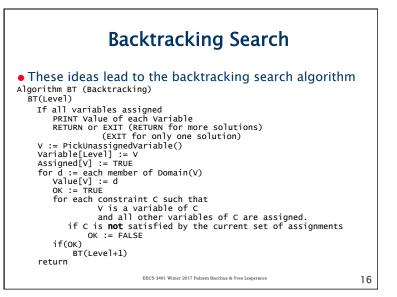


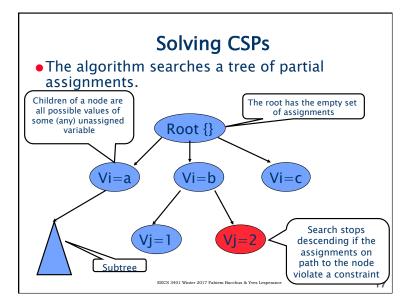


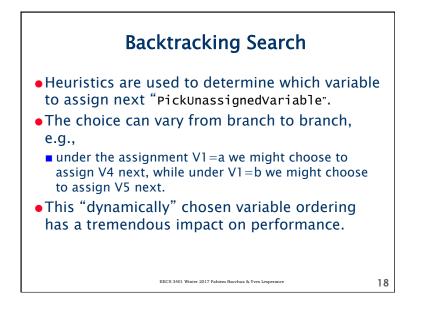


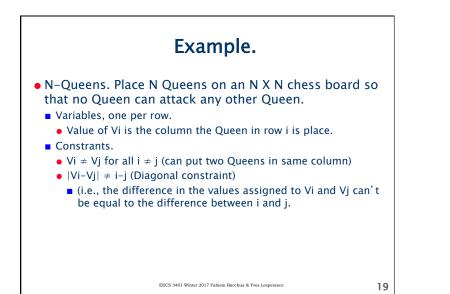


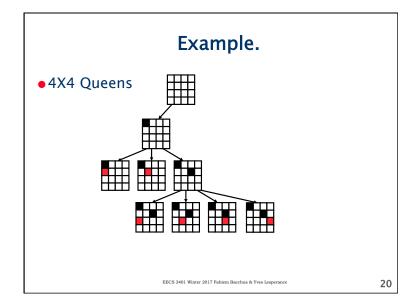


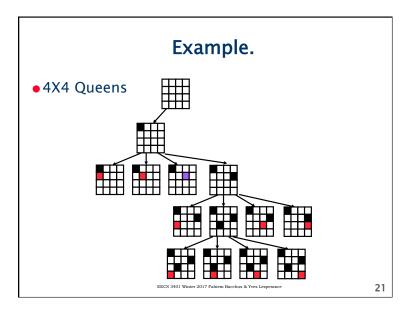


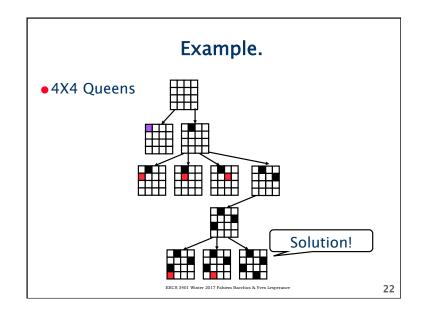


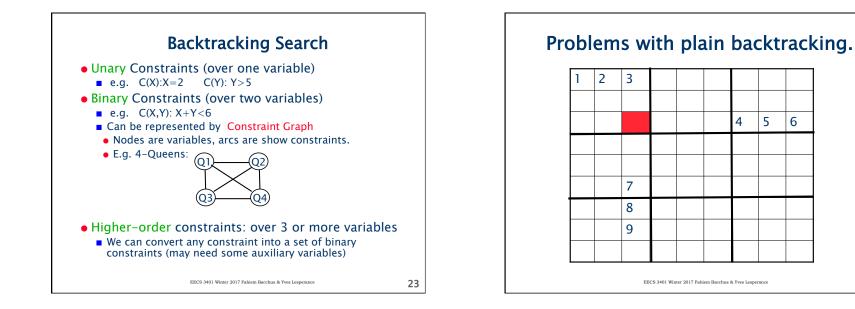


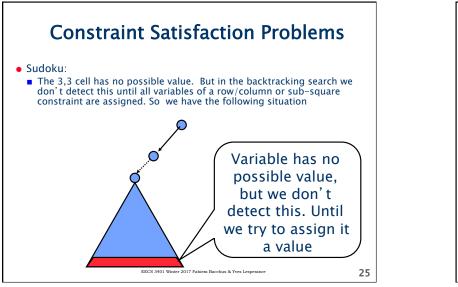


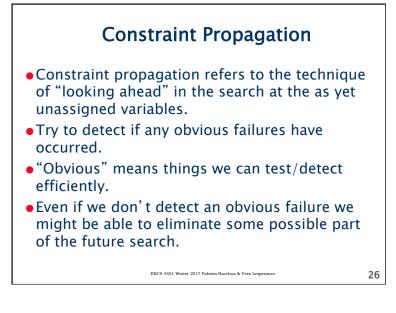


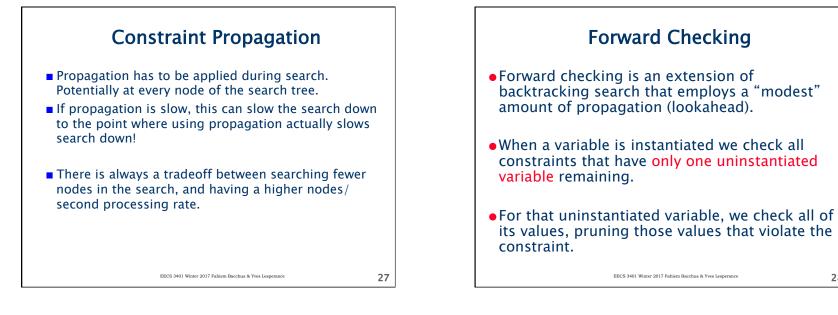


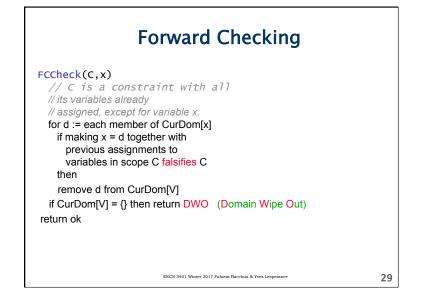






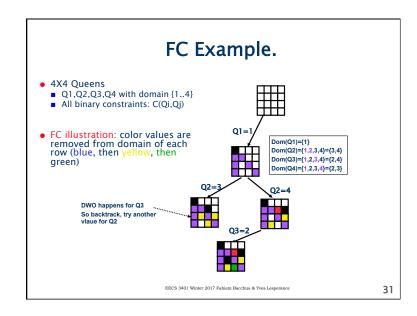


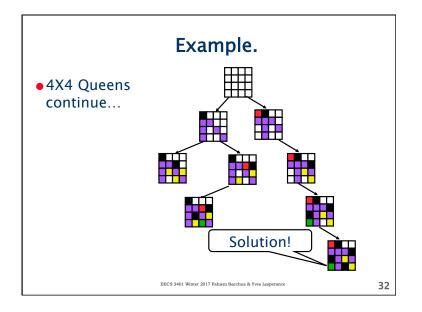


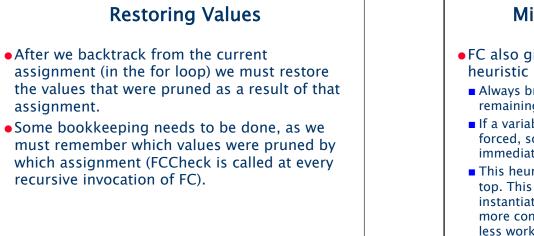


## **Forward Checking**

FC(Level) (Forward Checking) If all variables are assigned PRINT Value of each Variable RETURN or EXIT (RETURN for more solutions) (EXIT for only one solution) V := PickAnUnassignedVariable() Variable[Level] := V Assigned[V] := TRUE for d := each member of CurDom(V) value[v] := d for each constraint C over V that has one <u>unassigned variable</u> in its scope X. val := FCCheck(C,X) if(val != DWO) FC(Level+1) RestoreAllValuesPrunedByFCCheck() return; EECS 3401 Winter 2017 Fahiem Bacchus & Yves Lesperance







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## **Minimum Remaining Values**

- FC also gives us for free a very powerful heuristic
  - Always branch on a variable with the smallest remaining values (smallest CurDom).
  - If a variable has only one value left, that value is forced, so we should propagate its consequences immediately.
  - This heuristic tends to produce skinny trees at the top. This means that more variables can be instantiated with fewer nodes searched, and thus more constraint propagation/DWO failures occur with less work.

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