## More proof exercises

- Pigeonhole Principle: If $n+1$ balls are distributed among $n$ bins then at least one bin has more than 1 ball
- Generalized Pigeonhole Principle: If $n$ balls are distributed among $k$ bins then at least one bin has at least ceiling( $\mathrm{n} / \mathrm{k}$ ) balls


## Meaningful diagrams

- Pythagoras



## Meaningful diagrams - 2

- Sum of an arithmetic series (from http://www.tonydunford.com/images/math-and-geometry/sum-of-number-series/SumOfOdd.jpg)



## Meaningful diagrams - 3

- Sum of a geometric series (from http://math.rice.edu/~lanius/Lessons/Series/one.gif)



## Meaningful diagrams - 4

- $1 / 4+1 / 16+1 / 64+1 / 256+\ldots=1 / 3$
(from http://www.billthelizard.com/2009/07/six-visualproofs_25.html)


