

# **Abstract Data Types Documentation**

# Documentation

- Users are only interested in the properties of the ADT
- Programmers and designers require all the information which a user needs AND all information pertaining to the design and implementation
- Useful to think of the documentation as being an annotated definition of an abstract data type

# Documentation Table of Contents

- Cover page, table of contents and abstract
- Document introduction
  - » **Informal overview of the facilities provided. Help readers determine if this is what they need**
- Data type objects
  - » **Description of all the objects – include diagrams**
  - » **Split into**
    - > **Imported – which predefined objects are used**
    - > **Exported – for others to use**
    - > **Hidden – used in the implementation**

## Operations TOC – 2

- Operations
  - » **Give**
    - > **Signature**
    - > **Informal description**
    - > **pre- and post- conditions**
  - » **Use natural language, mathematics, diagrams – whatever best gets the meaning across.**
  - » **Be simple, complete, clear, precise, concise as possible**

## Operations TOC – 3

- Example – partial axiomatic description of bank accounts

» **The operation signatures only – no pre- post- given**

**new : [] → account**

- Create an account with a zero balance

**withdraw : account X amount → account**

- Remove amount from account

**deposit : account X amount → account**

- Add amount to account

**balance : account → amount**

- What is the amount in the account?

## Operations TOC – 4

- Operation interaction
  - » **Previous section describes operations in isolation**
  - » **Provide better understanding by showing properties when operations are used in combination**
  - » **Common descriptive method in use is axiomatic**
    - > **List of axioms or statements which must be true if the ADT is implemented and used correctly**

## Operations TOC – 5

- Axioms about the data type
  - » **Axiom 1: New account has a balance of zero dollars**  
 $\text{balance}(\text{new}) = 0$
  - » **Axiom 2: Cannot withdraw from a new account**  
 $\text{withdraw}(\text{new}, \text{amt}) = \text{error}$
  - » **Axiom 3: Deposit amt and then withdraw amt with no intervening operations the balance does not change**  
$$\text{balance}(\text{withdraw}(\text{deposit}(\text{acct}, \text{amt}), \text{amt})) = \text{balance}(\text{acct})$$
  - » **Axiom 4: Only withdraw if the balance is  $\geq$  the amount to withdraw. The amount is deducted from the balance**  
$$\text{balance}(\text{acct}) < \text{amt} \rightarrow \text{withdraw}(\text{acct}, \text{amt}) = \text{error}$$
$$\text{balance}(\text{acct}) \geq \text{amt} \rightarrow \text{balance}(\text{withdraw}(\text{acct}, \text{amt})) = \text{balance}(\text{acct}) - \text{amt}$$

## TOC – 6

- How to use the ADT
  - » **Tutorial guide on use. Dwell on nuances. Describe various examples**
- Dictionary
  - » **Define new terminology or domain specific jargon that implementers or users may not know**
- Undesired Event Dictionary
  - » **Description of possible errors which can occur**
  - » **Contains warnings**
  - » **How to recognize error situations**
  - » **How to recover from error situations**
  - » **What to do if recovery is impossible**



## TOC – 7

- ADT generation parameters
  - » **Describe how instances and variations can be implemented from this generic data type**
    - > **How to change base types**
    - > **How to change amount of storage for a customer name**
  - » **Describe changes that can be made that will not violate assumptions and specifications. Design for a class of similar data types**
  - » **State what programming tools can be used to modify the implementation**

## TOC – 8

- Design issues
  - » **What were the design choices and why were the actual choices chosen. Help guide future changes to keep in the spirit of the original**
    - > **Why was fixed memory allocation used instead of dynamic?**
    - > **Why were size limits imposed?**
    - > **Why was a particular data structure chosen?**

## TOC – 9

- Implementation notes
  - » **Designer may have information of use to the implementer. Know properties that can improve implementation**
- List of assumptions – those assumptions that
  - » **Cannot be violated**
  - » **Not implicit in the context**
  - » **Global**
  - » **Note: cannot state all assumptions so state those that**
    - > **Are most important**
    - > **Most likely to cause problems if violated**
    - > **Are not easily detected as causing problems until a long time later**

## TOC – 10

- Normal use assumptions
  - » **Information available from the ADT**
  - » **Information that must be supplied to the ADT**
  - » **Events reported by the ADT**
  - » **Tasks that can be performed by the ADT**
  - » **Operating states of the ADT and how they affect the Information obtained from and supplied to the ADT**
  - » **Failure states of the ADT and how they affect the information obtained from and supplied to the ADT**

## TOC – 11

- Incorrect use assumptions
  - » **Associated with run time undesired events**
  - » **What may or may not happen if the production version has undesired event handling code removed to speed up the system**
- Program source text
  - » **If the source test is small may be included with the description of the operations**
- Facilities index
  - » **A quick look up reference of all programs, modules, operations, objects and terms defined**

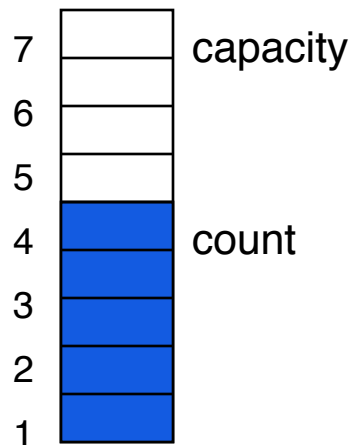
# Minimal Documentation

- Objects

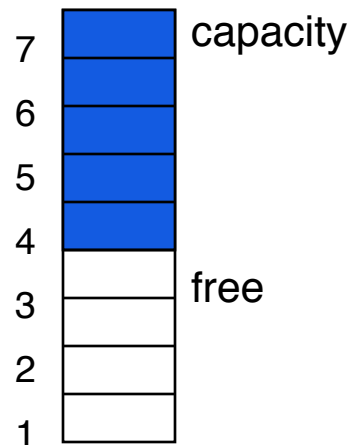
- » **Types**                      **Diagrams where possible**

- Example – stack

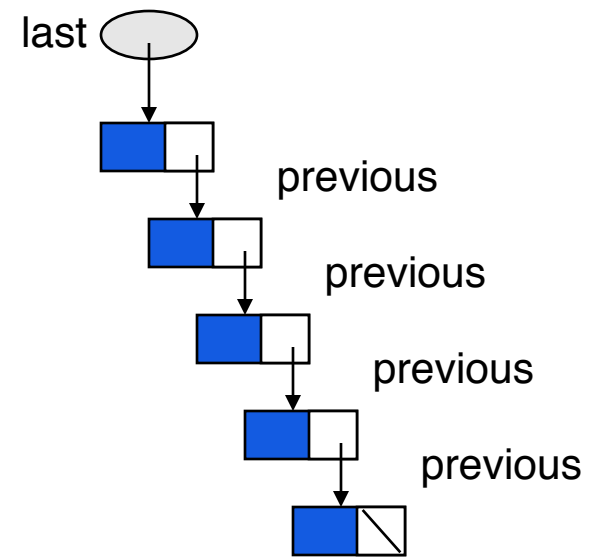
- » **Imported – none**
  - » **Exported – STACK [ G ]**
  - » **Hidden – implementation**



**Array up**



**Array down**



**Linked list**

## Minimal Documentation – 2

- Operations – example for a stack

- » **Signatures, pre & post conditions**

> **push : STACK [ G ] x G → STACK [ G ]**

– **require**    true  
  **ensure**    result = x ^ s & count = old count + 1

> **pop : STACK [ G ] → STACK [ G ]**

– **require**    not empty ( s )  
  **ensure**    result = s' & count = old count - 1

> **top : STACK [ G ] → G**

– **require**    not empty ( s )  
  **ensure**    result = s<sub>1</sub>

## Minimal Documentation – 3

- Operations – example for a stack cont'd

> **empty : STACK [ G ] → BOOLEAN**

– **require**    **true**  
  **ensure**    **result = ( count = 0 )**

> **new : [ ] → STACK [ G ]**

– **require**    **true**  
  **ensure**    **result = STACK [ G ] ∧ count = 0**

» **Note: often "require true" is not written but is assumed**

» **It is better to write it as then one can wonder if it was left out by accident**

> **"nothing" is often represented with a special symbol.  
e.g. nil , λ , ε , Δ**



## Minimal Documentation – 4

- Operations – example for a stack cont'd

- » **Axioms**

>  $\forall x : G, s : \text{STACK} [ G ] \cdot$   
     $\text{top} ( \text{push} ( s, x ) ) = x$   
     $\wedge \text{pop} ( \text{push} ( s, x ) ) = s$   
     $\wedge \text{empty} ( \text{new} )$   
     $\wedge \sim \text{empty} ( \text{push} ( s, x ) )$

- is read as  
"it is the case that"

- » **Alternately can use natural language**

> forall  $x : G, s : \text{STACK} [ G ] ::$   
     $\text{top} ( \text{push} ( s, x ) ) = x$   
    and  $\text{pop} ( \text{push} ( s, x ) ) = s$   
    and  $\text{empty} ( \text{new} )$   
    and not  $\text{empty} ( \text{push} ( s, x ) )$

## ADT Invariants

- Conditions that must be true after the execution of any method in the the class
- The conditions that hold, at all times, among the objects in an instance of the ADT
  - » **More on this when we discuss design by contract**

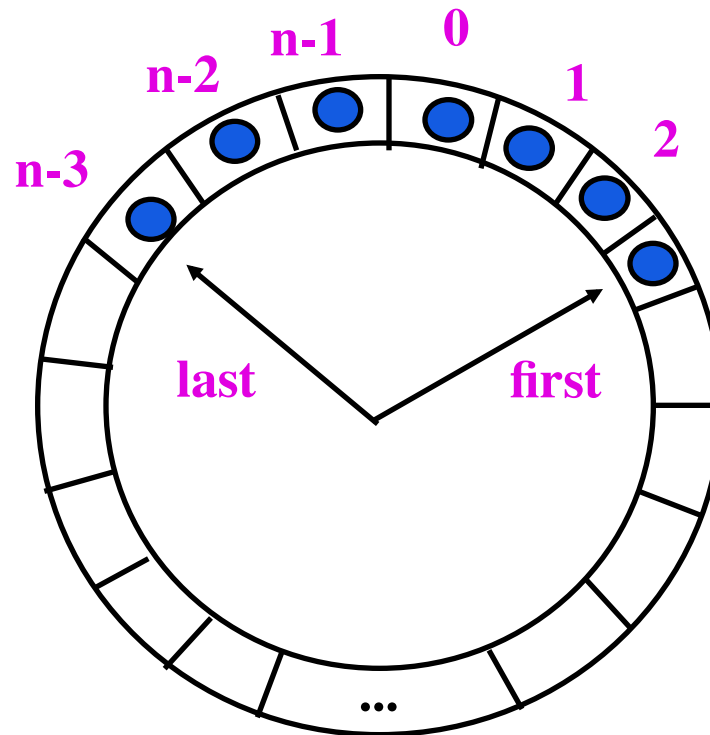
# Example Circular Queue

**isEmpty**  $\rightarrow$  **length** = 0  $\wedge$  (last-1) mod Size = first

**isFull**  $\rightarrow$  **length** = Size - 1

**not isFull**  $\rightarrow$  **length** = (Size + first - last + 1) mod Size

**last** is the last  
Item to remove



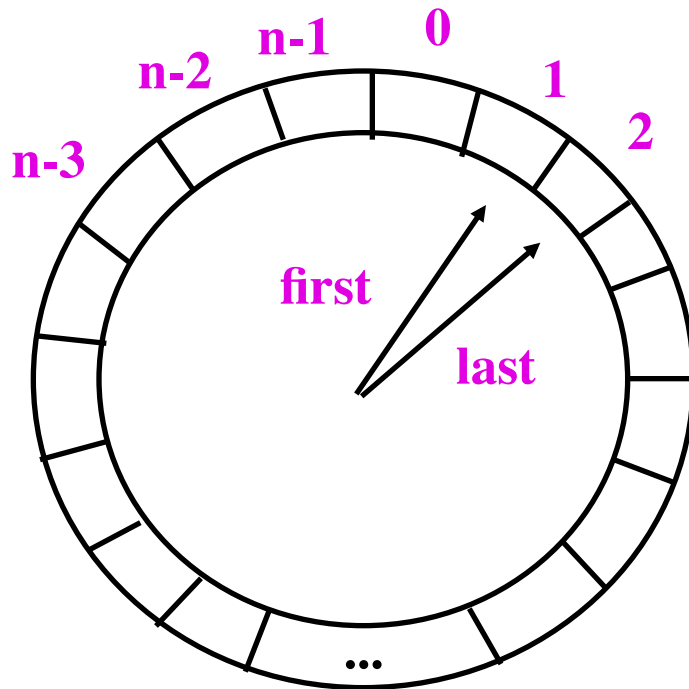
**first** is the first  
Item to remove

# Empty Circular Queue

**isEmpty**  $\rightarrow$  **length = 0**  $\wedge$  **(last-1) mod Size = first**

**isFull**  $\rightarrow$  **length = Size - 1**

**not isFull**  $\rightarrow$  **length = (Size + first - last + 1) mod Size**



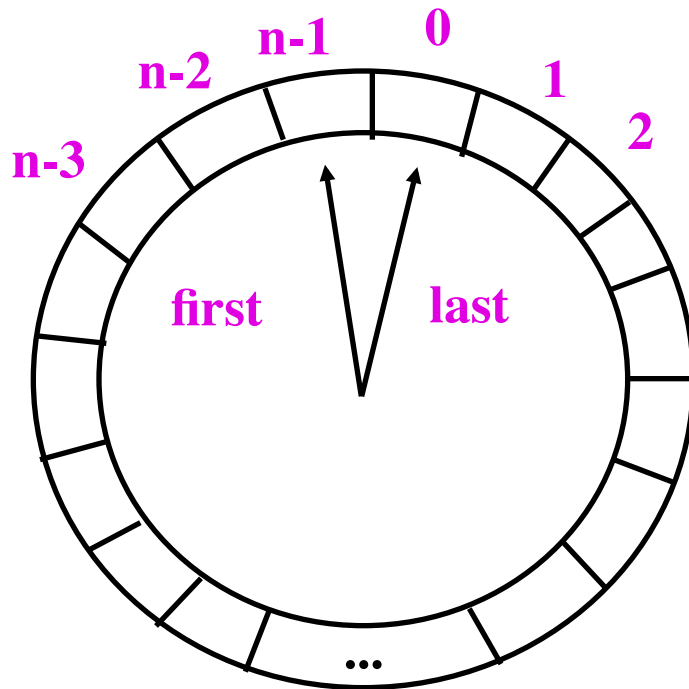
$$\begin{aligned}\text{length} &= (n + 1 - 2 + 1) \bmod n \\ &= (n + 0) \bmod n \\ &= 0\end{aligned}$$

## Empty Circular Queue – 2

**isEmpty**  $\rightarrow$  **length** = 0  $\wedge$  (last-1) mod Size = first

**isFull**  $\rightarrow$  **length** = Size - 1

**not isFull**  $\rightarrow$  **length** = (Size + first - last + 1) mod Size



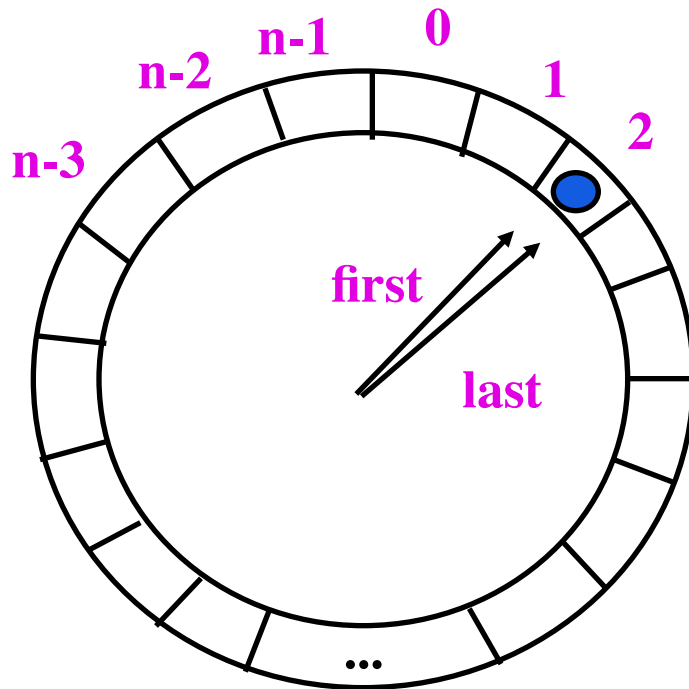
$$\begin{aligned}\text{length} &= (n + (n-1) - 0 + 1) \bmod n \\ &= (2n + 0) \bmod n \\ &= 0\end{aligned}$$

# Length 1 Circular Queue

**isEmpty**  $\rightarrow$  **length** = 0  $\wedge$  (last-1) mod Size = first

**isFull**  $\rightarrow$  **length** = Size - 1

**not isFull**  $\rightarrow$  **length** = (Size + first - last + 1) mod Size



$$\begin{aligned}\text{length} &= (n + 2 - 2 + 1) \bmod n \\ &= (n + 1) \bmod n \\ &= 1\end{aligned}$$

# Longer length Circular Queue

$$\text{length} = (\text{Size} + \text{first} - \text{last} + 1) \bmod \text{Size}$$

$$\begin{aligned}\text{length} &= (n + 3 - (n-3) + 1) \bmod n \\ &= (7) \bmod n \\ &= 7\end{aligned}$$

