

## Example [ Aloha – avoiding collision ]

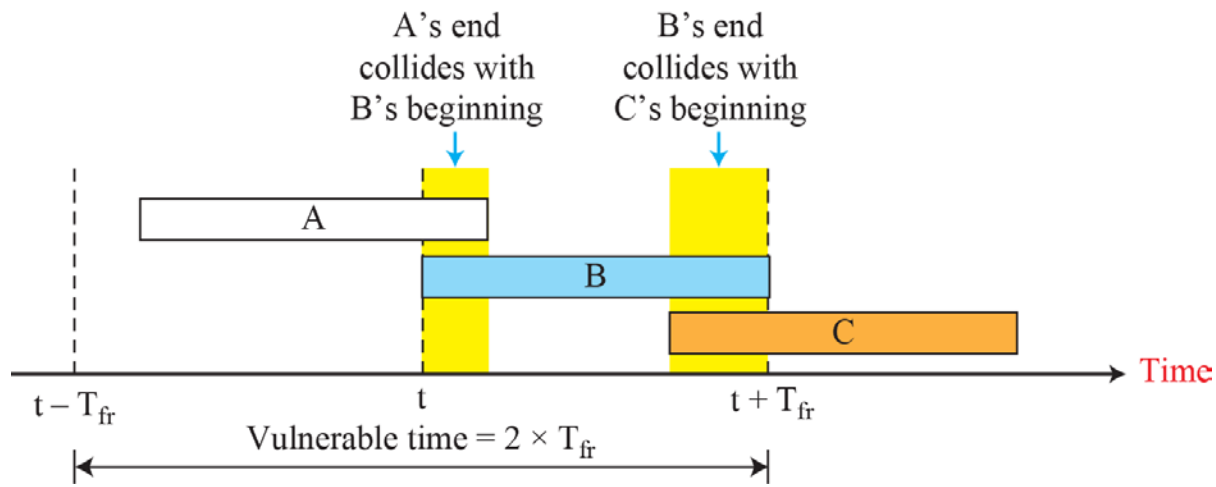
A pure ALOHA network transmits a 200-bit frame on a shared channel Of 200 kbps at time  $t_0$ . What is the requirement to make this frame collision free?

**Solution:**

Frame transmission time  $T_f = 200 \text{ bits} / 2000 \text{ kbps} = 1 \text{ msec}$ .

Vulnerability period =  $2 * 1 \text{ msec} = 2 \text{ msec}$

Collision will be avoided if no other station start transmitting 1 msec before and during the transmission of this frame.



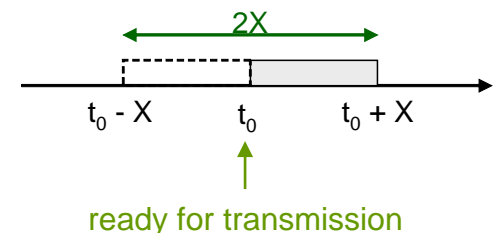
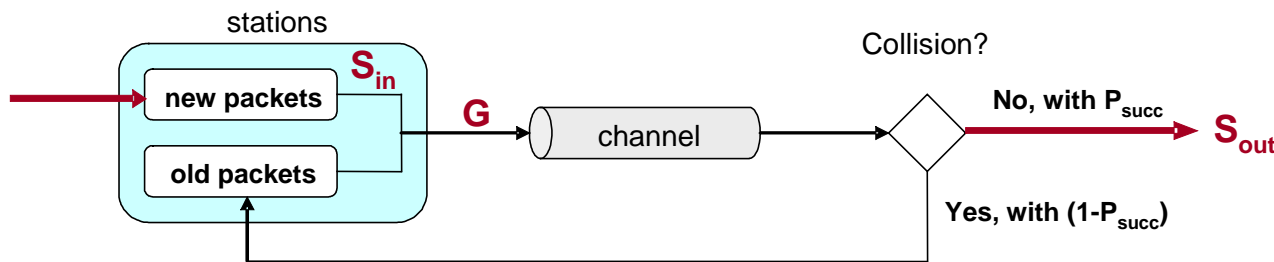
## Throughput

- definitions and assumptions:

- **S ( $S_{out}$ ) – throughput:** average # of successful frame transmiss. per X sec (if network operates under ‘stable conditions’  
 $S_{out} = S_{in}$  , where  $S_{in}$  - arrival rate of new frames to the system)
- **G – load** – average # of overall transmission attempts! per X sec
- **$P_{succ}$**  – probability of a successful frame transmission

$$S = P_{succ} \cdot G$$

- **How to find  $P_{succ}$ ?** – suppose a frame is ready for transmission at time  $t_0$  – frame will be transmitted successfully if no other frame attempts transmission X sec before and after  $t_0$
- random backoff spreads retransmissions so that frame transmission (arrivals) are equally likely at any instant in time – **Poisson process!!!**



- if general, if frame arrivals are equally likely at any instant in time, and arrivals occur at an average rate of  $\lambda$  [arrivals per sec]

Poisson process

$$P[k \text{ arrivals in } T \text{ seconds}] = \frac{(\lambda T)^k}{k!} e^{-\lambda T}$$

- to get [arrivals per second]  $\lambda$  is calculated as  $\lambda = G/X$ , while interval of interest is  $T = 2X$ , hence

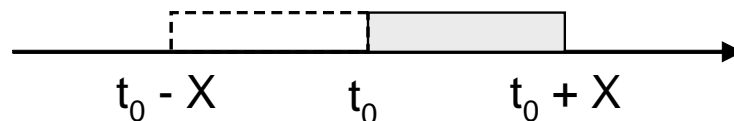
$$P[k \text{ transmissions in } 2X \text{ seconds}] = \frac{(2G)^k}{k!} e^{-2G}$$

- thus, probability of successful transmission (no other transmission in  $T = 2X$  seconds) is:

$$P_{\text{succ}} = P[0 \text{ transmissions in } 2X \text{ seconds}] = e^{-2G}$$

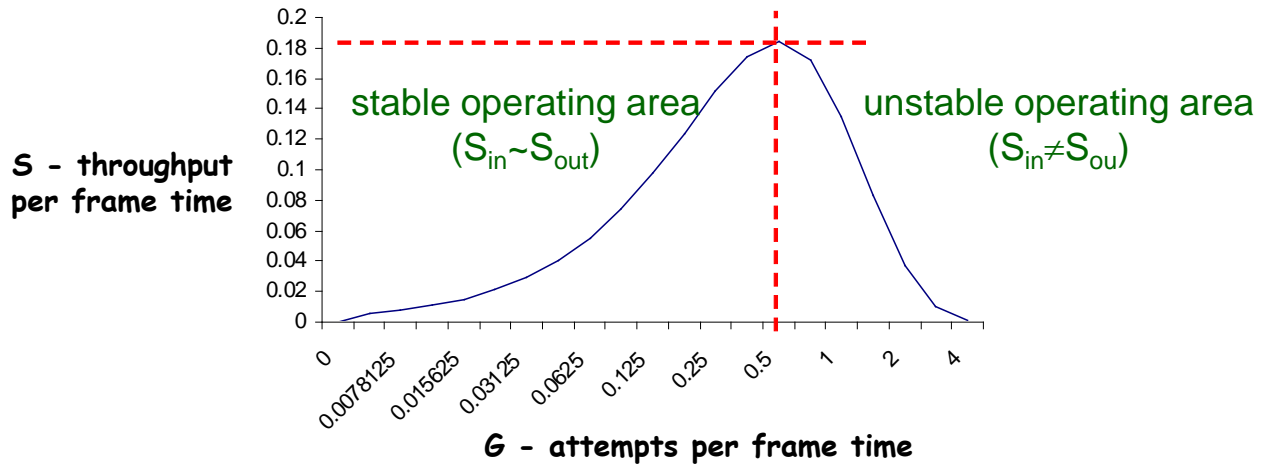
and throughput

$$S = G \cdot P_{\text{succ}} = G \cdot e^{-2G}$$



## S vs. G in Pure ALOHA

- **NOTE:** our analysis assumed that many nodes share a common channel & have comparable transmiss. rates (if only 1 node uses the medium,  $S=1$ )
- initially, as  $G$  increases  $S$  increases until it reaches  $S_{max}$  – after that point the network enters ‘**unstable operating conditions**’ in which collisions become more likely and the number of backlogged stations increases (consequently,  $S_{in} > S_{out}$ )
- **max throughput of ALOHA ( $S_{max} = 0.184$ ) occurs at  $G=0.5$** , which corresponds to a total arrival rate of ‘one frame per vulnerable period’
- $S_{max} = 0.184 \Rightarrow$  max ALOHA throughput = 18% of channel capacity



**18% of channel utilization, with Aloha, is not encouraging. But, with everyone transmitting at will we could hardly expect a 100% success rate.**

## Example [ Aloha ]

A pure ALOHA network transmits 200-bits frames on a shared channel of 200 kbps.

What is the throughput of this system if all stations together produce 1000 frames per second?

Solution:

Throughput of pure ALOHA: 
$$S = G \cdot e^{-2G} \frac{\text{frames}}{\text{frame time}}$$

$G = 1000$  [frames / second], but we need it in [frames / frame time]

Frame time  $X = 200 \text{ bits} / 200 \text{ kbps} = 1 \text{ msec}$

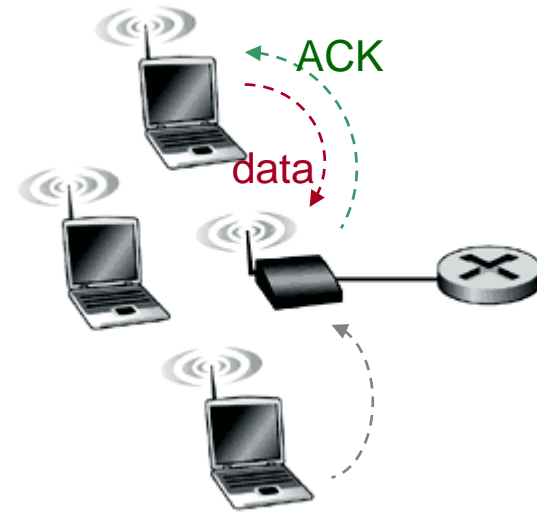
$G = 1000$  [frames / 1000 frame times] = 1 [frame / frame time]

Hence,

$$S(G = 1) = e^{-2} = 0.135 \frac{\text{frames}}{\text{frame time}} = 0.135 \frac{\text{frames}}{1 \text{ msec}} = 135 \frac{\text{frames}}{\text{sec}}$$

## Example [ Aloha ]

- a) What is the vulnerable period (in milliseconds) of a pure ALOHA broadcast system with  $R=50$ -kbps wireless channel, assuming 1000-byte frames.
- b) What is the maximum possible throughput  $S$  of such a channel (system), in kbps?



- a) (frame transmission time  $\Rightarrow$ )  $X = 1000 \text{ bytes} / 50 \text{ kbps} = 8000 \text{ bits} / 50 \text{ kbps}$   
 $\Rightarrow X = 160 \text{ milliseconds}$

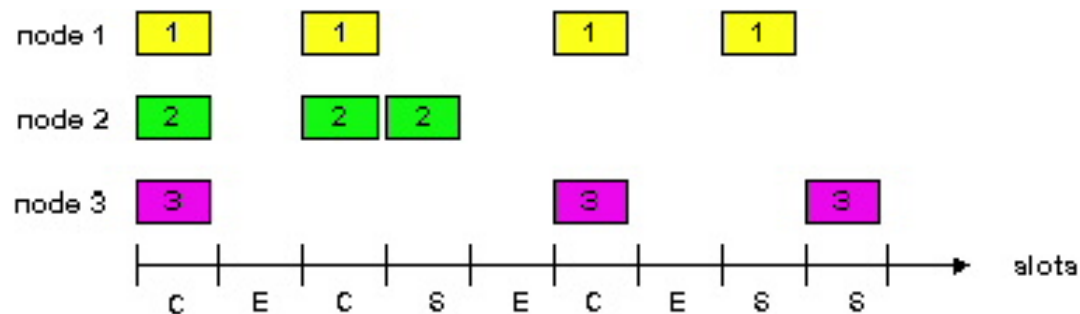
**vulnerable period =  $2 * X = 320 \text{ milliseconds}$**

- b) We do not have enough information to determine  $G$ . The best we can do ...  
From theory,  $\text{max throughput} = 0.18 * R = 0.18 * 50 \text{ kbps} = 9.179 \text{ kbps}$

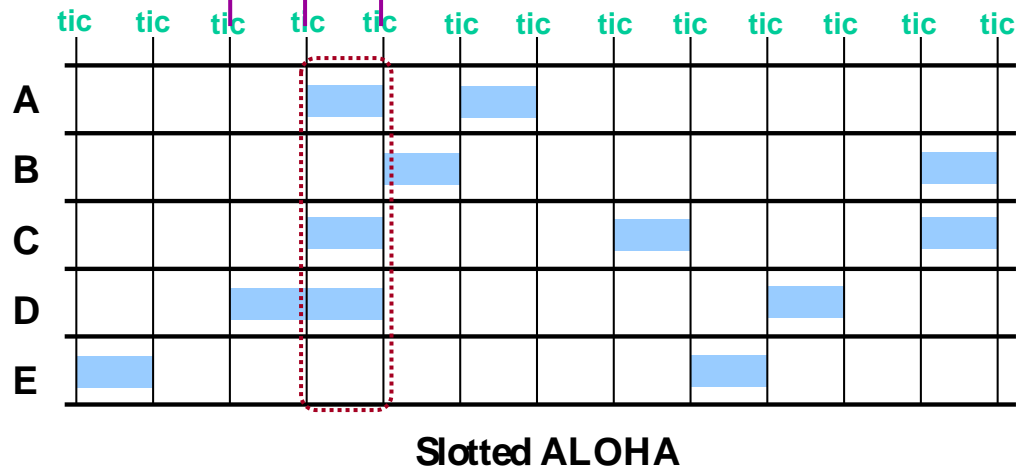
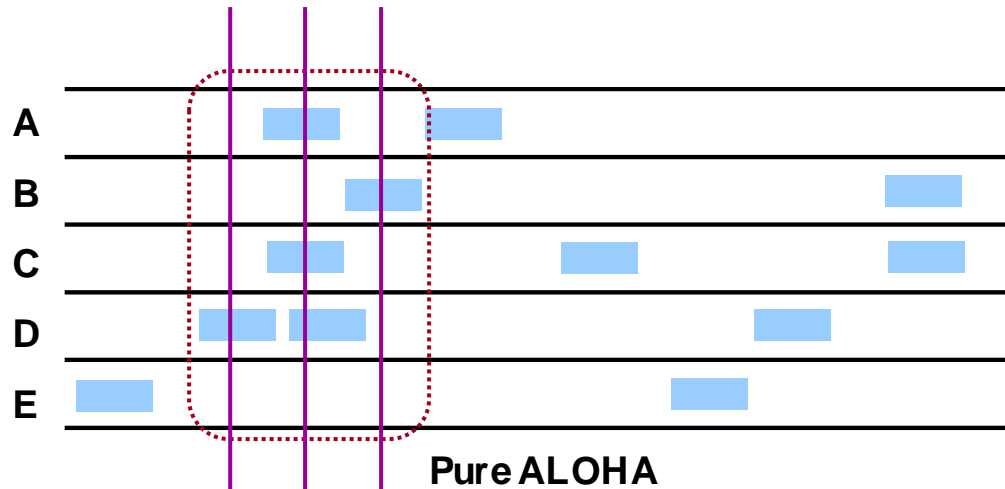
# Random Access Techniques: Slotted ALOHA

**Slotted ALOHA** – “improved ALOHA”, with reduced probability of collision

- assumptions:
  - time is divided into slots of size  $X=L/R$  (one frame time)
  - **nodes start to transmit only at the beginning of a slot**
  - nodes are synchronized so that each node knows when the slots begin
- operation:
  - 1) when node has a fresh frame to send, it waits until next frame slot and transmits
  - 3) if there is a collision, node retransmits the frame after a backoff-time (backoff-time = multiples of time-frames)



## Example [ Aloha vs. Slotted Aloha ]





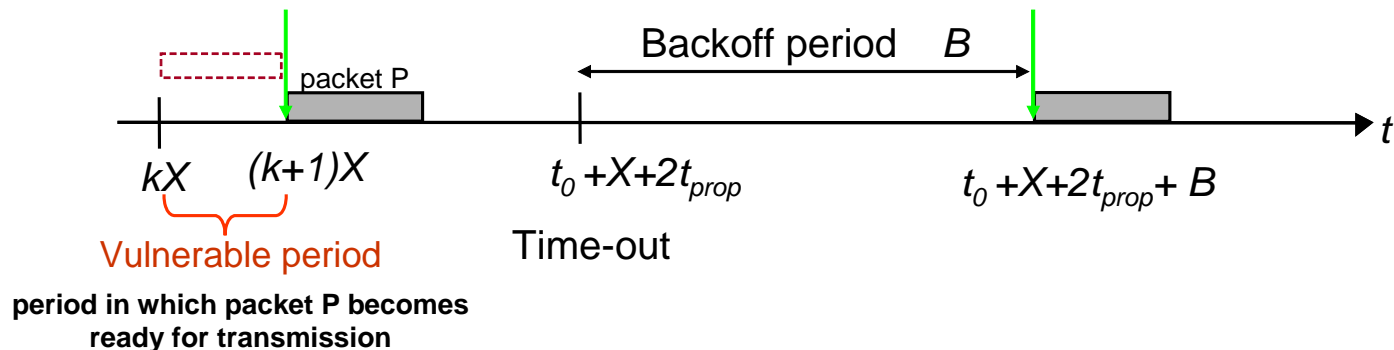
## Vulnerable Period of Slotted ALOHA

- consider one arbitrary packet P that becomes ready for transmission at some time  $t$  during the time slot  $[k, k+1]$
- packet P will be transmitted successfully if no other packet becomes available for transmission during the same time slot

**vulnerable period =  $[t_0 - X, t_0]$**

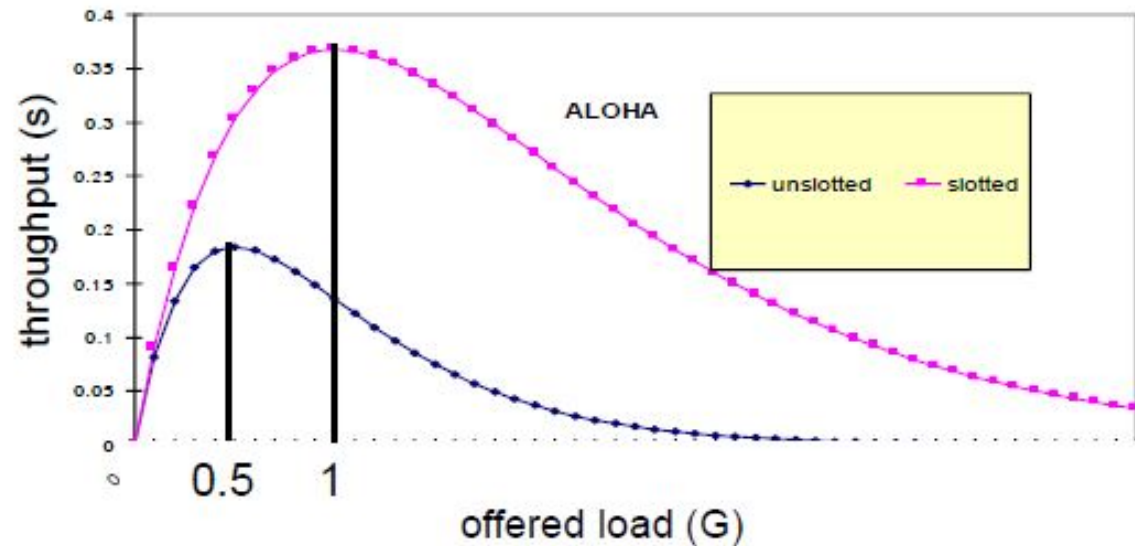
$$P_{\text{succ}} = P[0 \text{ arrivals in } X \text{ seconds}] = e^{-G}$$

$$S = G \cdot P_{\text{succ}} = G \cdot e^{-G}$$



## S vs. G in Slotted ALOHA

- **max throughput of Slotted ALOHA ( $S_{\max} = 0.36$ ) occurs at  $G=1$** , which corresponds to a total arrival rate of 'one frame per vulnerable period'
- $S_{\max} = 0.36 \Rightarrow$  max Slotted ALOHA throughput = 36% of actual channel capacity



## Slotted ALOHA vs. Pure ALOHA

- slotted ALOHA reduces vulnerability to collision, but also adds a waiting period for transmission
- if contention is low, it will prevent very few collisions, & delay many of the (few) packets that are sent

## Example [ slotted Aloha ]

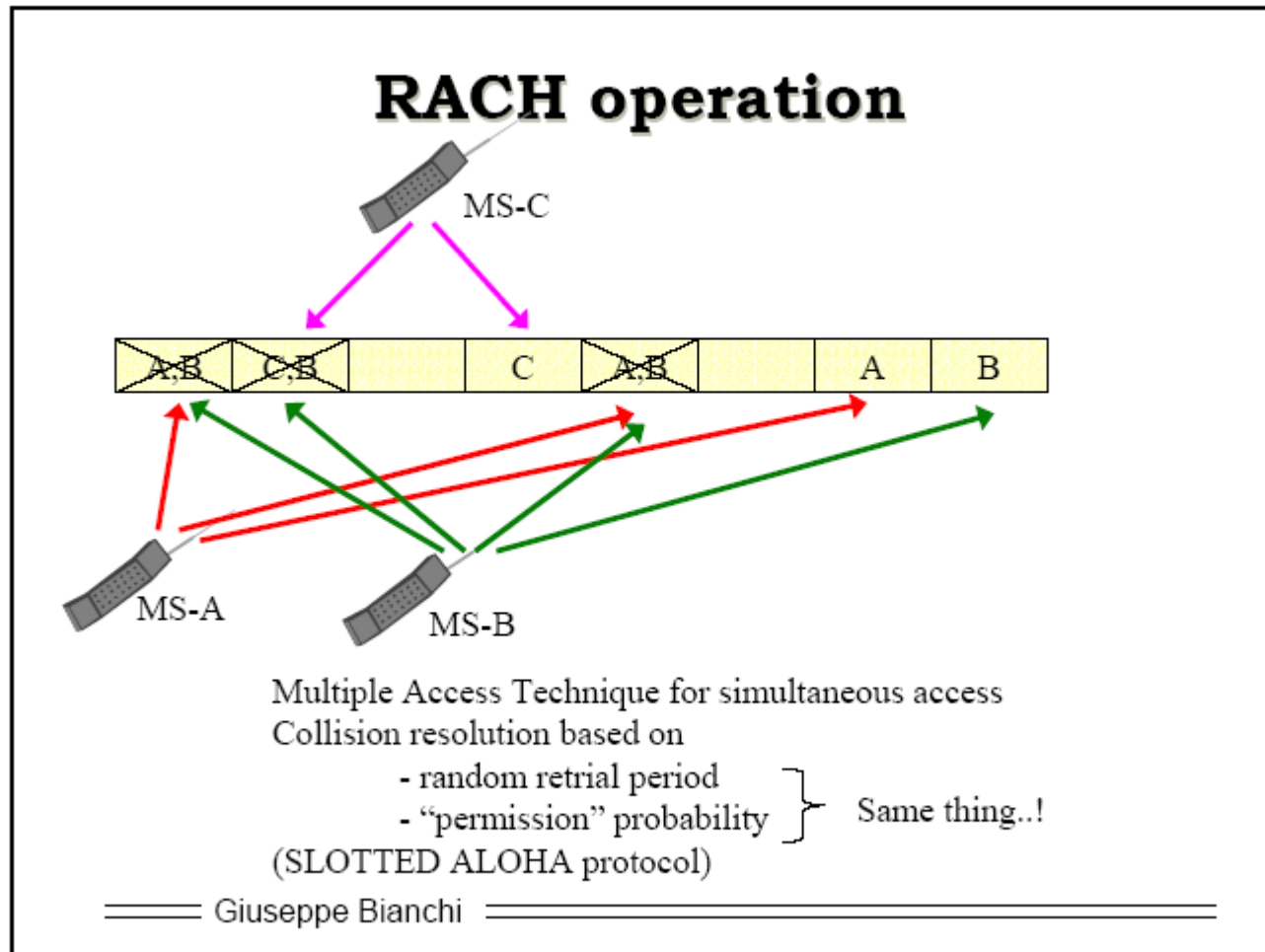
Measurements of slotted ALOHA channel with an infinite number of users show that 10% of the slots are idle.

- What is the channel load,  $G$ ?
- What is the throughput,  $S$ ?
- Is the channel underloaded or overloaded?



- 10% of slots idle  $\Rightarrow$   
frame will be successfully transmitted if sent in those 10% of slots  $\Rightarrow$   
 $P_{\text{succ}} = 0.1$   
According to theory,  $P_{\text{succ}} = e^{-G} \Rightarrow G = -\ln(P_{\text{succ}}) = -\ln(0.1) = 2.3$
- According to theory,  $S = P_{\text{succ}} * G = G * e^{-G}$   
as  $G=2.3$  and  $e^{-G}=0.1 \Rightarrow S = 0.23$
- Whenever  $G>1$ , the channel is overloaded, so it is overloaded in this case.

## Example [ slotted Aloha in cellular (GSM) systems ]



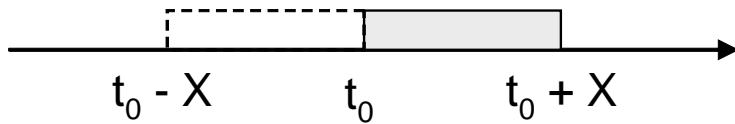
- if general, if frame arrivals are equally likely at any instant in time, and arrivals occur at an average rate of  $\lambda$  [arrivals per sec]

**Poisson process**



$$P[k \text{ arrivals in } T \text{ seconds}] = \frac{(\lambda T)^k}{k!} e^{-\lambda T}$$

- to get [arrivals per second],  $\lambda$  is calculated as  $\lambda = G/X$
- to avoid collision, there should be only 1 transmission in the interval  $X$  starting at  $t_0$  AND 0 transmissions in the interval  $X$  preceding  $t_0$



$$P_1 = P[1 \text{ transmissions in } X \text{ seconds}] = \frac{\left(\frac{G}{X} \cdot X\right)^1}{1!} \cdot e^{-\frac{G}{X} \cdot X} = G \cdot e^{-G}$$

$$P_2 = P[0 \text{ transmissions in } X \text{ seconds}] = e^{-G}$$

$$P_{\text{succ}} = P_1 \cdot P_2 = G \cdot e^{-2G}$$

$$P_{\text{succ}} = P_1 \cdot P_2 = G \cdot e^{-2G}$$