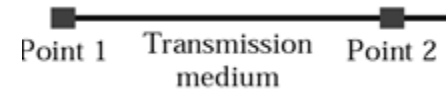


how many times the output signal has attenuated relative to the input signal – **should be ≥ 1**

$$L(f) = \frac{P_{in}(f)}{P_{out}(f)} = \frac{A_{in}(f)^2}{A_{out}(f)^2}$$



how many times the output signal has been amplified relative to the input signal – **should be ≥ 1**

$$G(f) = \frac{P_{out}(f)}{P_{in}(f)} = \frac{1}{L(f)}$$



In multi-cascade system



$$L(f) = L_1(f) \cdot L_2(f) \cdot L_2(f) \cdot \dots$$

$$L(f)[dB] = L_1(f)[dB] + L_2(f)[dB] + L_2(f)[dB] + \dots$$

$$L \text{ [dB]} \leftrightarrow G \text{ [dB]}$$

$$L[\text{dB}] = 10 \cdot \log \frac{P_{\text{in}}}{P_{\text{out}}} \text{ [dB]} = 10 \cdot \log \left(\frac{P_{\text{out}}}{P_{\text{in}}} \right)^{-1} \text{ [dB]} = -10 \log \frac{P_{\text{out}}}{P_{\text{in}}} = -G[\text{dB}]$$

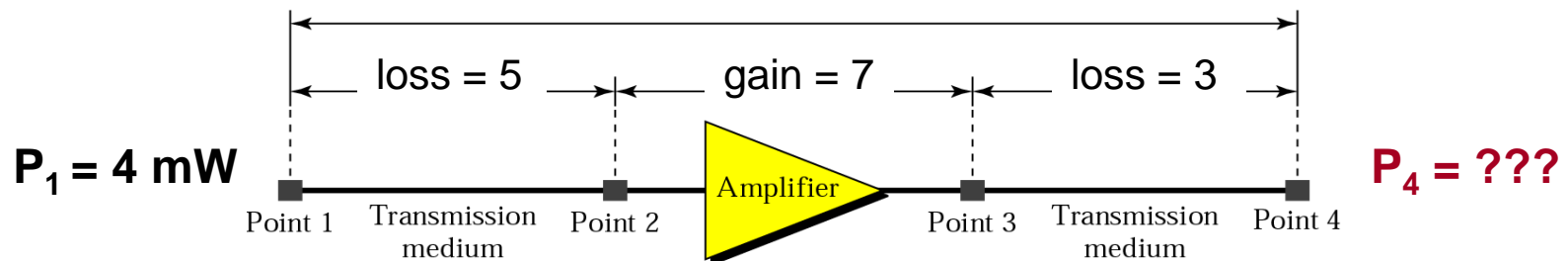
$$G \text{ [dB]} = -L \text{ [dB]}$$

Example [attenuation]

Consider a series of transmission elements as shown in the figure below.

The input signal has the power of $P_1 = 4 \text{ mW}$. The 1st element is a transmission line with a loss of **5 (x)**, the 2nd element is an amplifier with a gain of **7 (x)**, and the 3rd element is a transmission line with a loss of **3 (x)**.

Calculate the output power P_4 .



$$G = \frac{1}{L} = \frac{P_4}{P_1} = \frac{P_4}{P_3} \cdot \frac{P_3}{P_2} \cdot \frac{P_2}{P_1} = \frac{1}{5} \cdot \frac{7}{1} \cdot \frac{1}{3} = 0.47$$

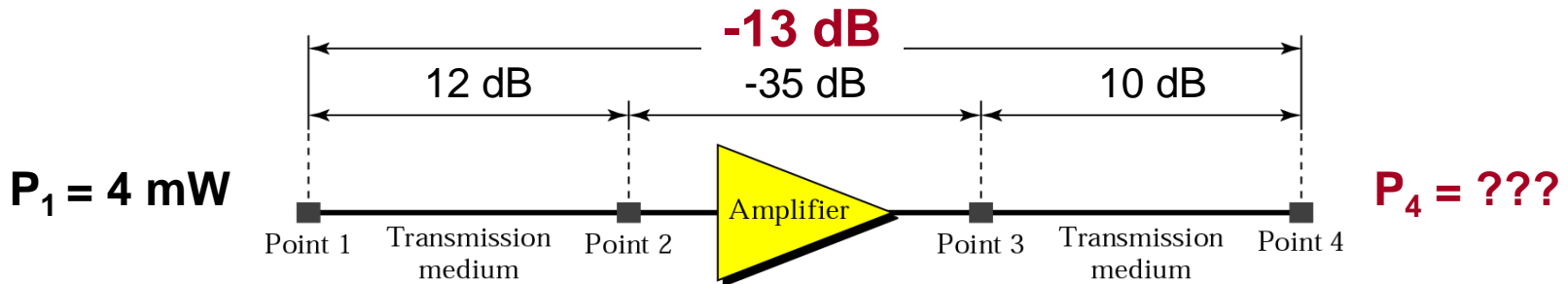
$$P_4 = G \cdot P_1 = 0.47 \cdot 4 \text{ [mW]} = 1.88 \text{ [mW]}$$

Example [attenuation]

Consider a series of transmission elements as shown in the figure below.

The input signal has the power of $P_1 = 4 \text{ mW}$. The 1st element is a transmission line with a 12 dB loss, the 2nd element is an amplifier with a 35 dB gain, and the 3rd element is a transmission line with a 10 dB loss.

Calculate the output power P_4 .

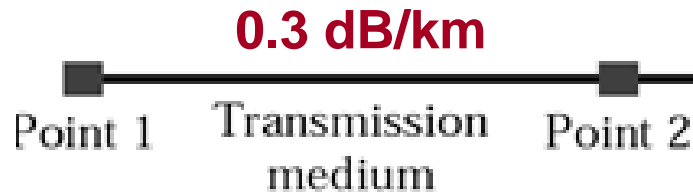


$$10 \cdot \log \frac{P_{in}}{P_{out}} = -13 \text{ [dB]} \quad \frac{P_{in}}{P_{out}} = 10^{-1.3} \text{ [dB]}$$

$$P_{out} = \frac{P_{in}}{10^{-1.3}} = P_{in} \cdot 10^{1.3} = 4 \cdot 19.95 = 79.8 \text{ [mW]}$$

Example [attenuation]

The loss in a cable is usually defined in decibels per kilometer (dB/km). If the signal at the beginning of a cable with 0.3 dB/km has a power of $P_1 = 2 \text{ mW}$, what is the power of the signal at 5km?



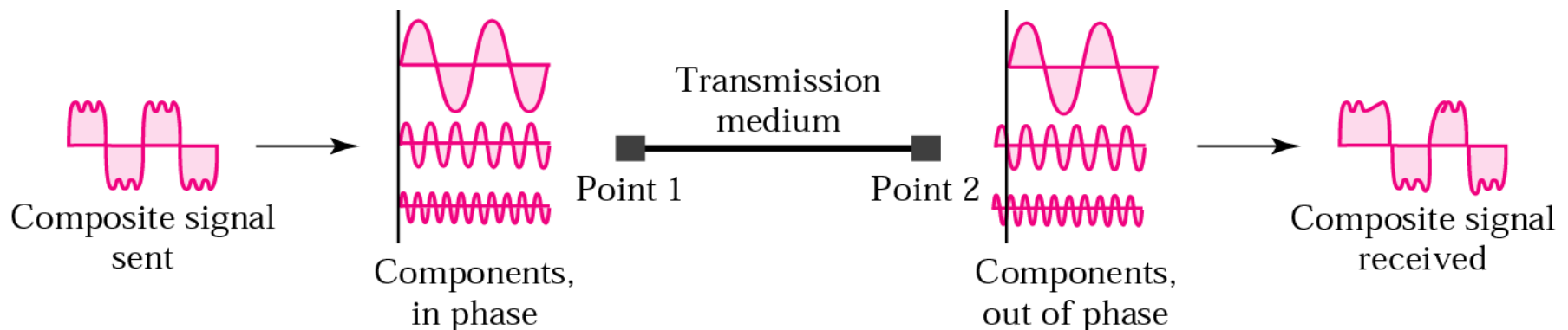
$$L_{\text{total} = 5\text{km}} = 5 \cdot L_{1\text{km}} = 1.5 \text{ [dB]}$$

$$10 \cdot \log \frac{P_{\text{in}}}{P_{\text{out}}} = 1.5 \text{ [dB]} \quad \frac{P_{\text{in}}}{P_{\text{out}}} = 10^{0.15} \text{ [dB]}$$

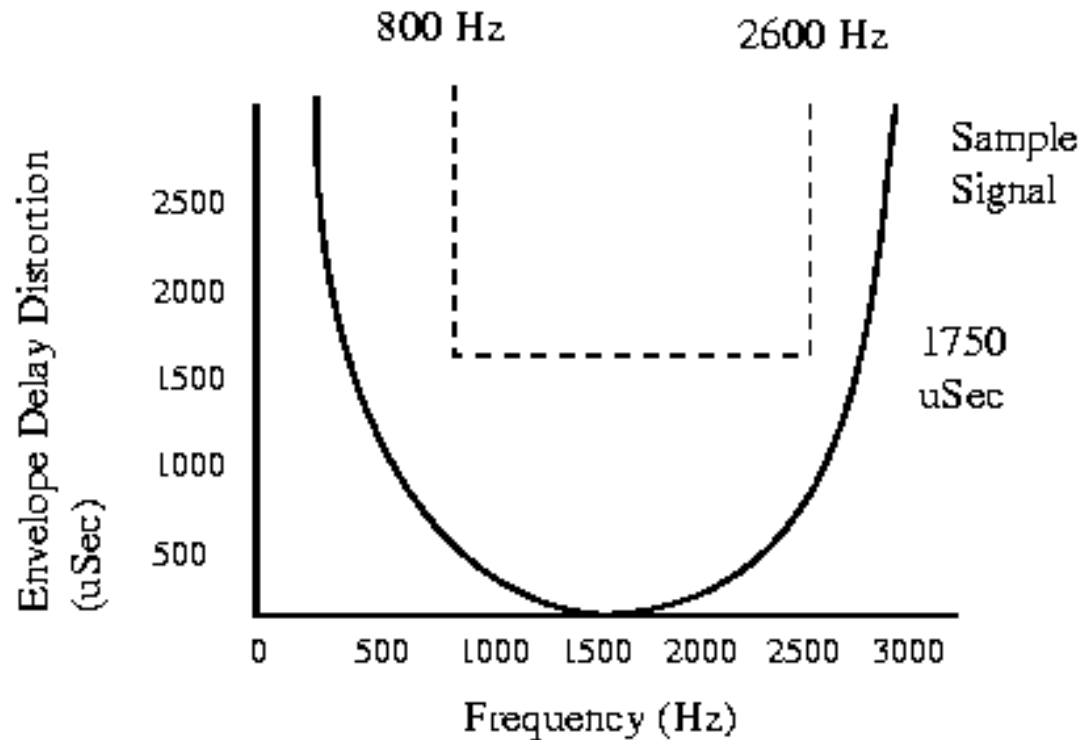
$$P_{\text{out}} = \frac{P_{\text{in}}}{10^{0.15}} = \frac{2 \text{ [mW]}}{1.41} = 1.41 \text{ [mW]}$$

Delay Distortion – change in signal's form / shape

- each signal component has its own propagation speed through a medium, and therefore, its own delay in arriving at the final destination
- **critical for composite-analog** and **digital signals** – some of the signal components of one bit position will spill over into other bit position, contributing to '**intersymbol interference**'
 - one of major limitation to achieving high bit rates
- in bandlimited channels, velocity tends to be highest near the center frequency and fall off towards the edges of the band

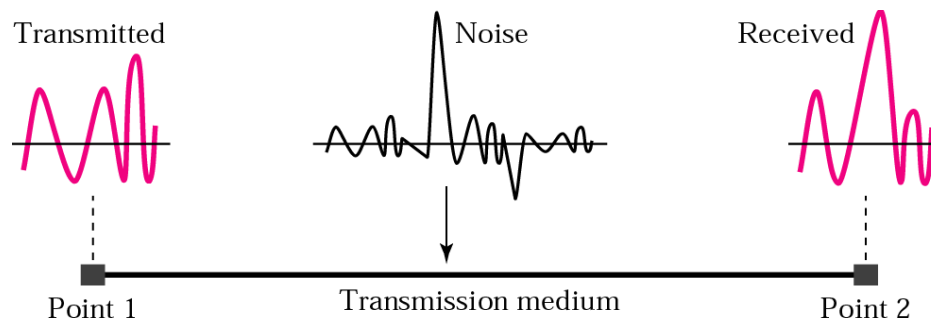


Example [delay distortion in telephone lines – measured in μsec]



Noise – unwanted signals that get inserted / generated somewhere between transmitter and receiver

- **major limiting factor in communications system performance**
 - **cannot be predicted – appears at random!**
- the presence of noise limits the reliability with which the receiver can correctly determine the information that was transmitted
- main categories of noise:
 - (1) thermal noise
 - (2) intermodulation noise
 - (3) crosstalk
 - (4) impulse noise



- (1) **Thermal Noise** – **result of random motion of electrons** – appears in all electronic devices and transmission media – cannot be eliminated
- **function of temperature**
 - **uniformly distributed across frequency spectrum** ⇒ aka white noise
 - **noise power density (N_o)** = amount of thermal noise to be found in a bandwidth of 1Hz

$$N_o = k \cdot T \text{ [W/Hz]}$$

where k = Boltzmann's constant = $1.3803 \cdot 10^{-23}$ [J/K]
 T = temperature [K]

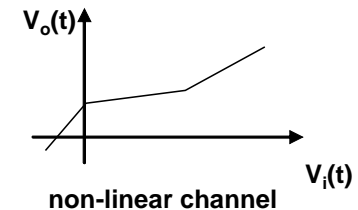
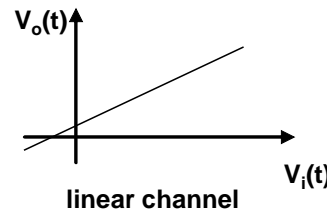
- **thermal noise (N)** in [W] present in a bandwidth of B [Hz]

$$N = k \cdot T \cdot B \text{ [W]}$$

Example Calculate N on 20C and 1GHz: $N = k \cdot (273+20) \cdot 10^9 = 3.8 \cdot 10^{-12}$.

(2) Intermodulation Noise – signals that are sum / difference of original frequencies sharing a medium

- result of nonlinearity in transmission medium – output signal is a complex function of the input



(3) Crosstalk – effect of one wire on the other – one wire acts as a sending antenna and the other as the receiving antenna

- can be reduced by careful shielding and using twisted pairs
- of the same magnitude, or less, than thermal noise



(4) Impulse Noise – non-continuous, consisting of irregular pulses or noise spikes of short duration and of relatively high amplitude

- induced by external electromagnetic disturbances, such as lightning, faults and flaws in communication system

$$s_{in}(t) = \sin(2\pi f_1 t) + \sin(2\pi f_2 t)$$

Example [**linear channel**]

$$s_{out}(t) = k \cdot s_{in}(t)$$

$$s_{out}(t) = k \cdot \sin(2\pi f_1 t) + k \cdot \sin(2\pi f_2 t)$$

Example [**non-linear channel**]

$$s_{out}(t) = k \cdot (s_{in}(t))^2$$

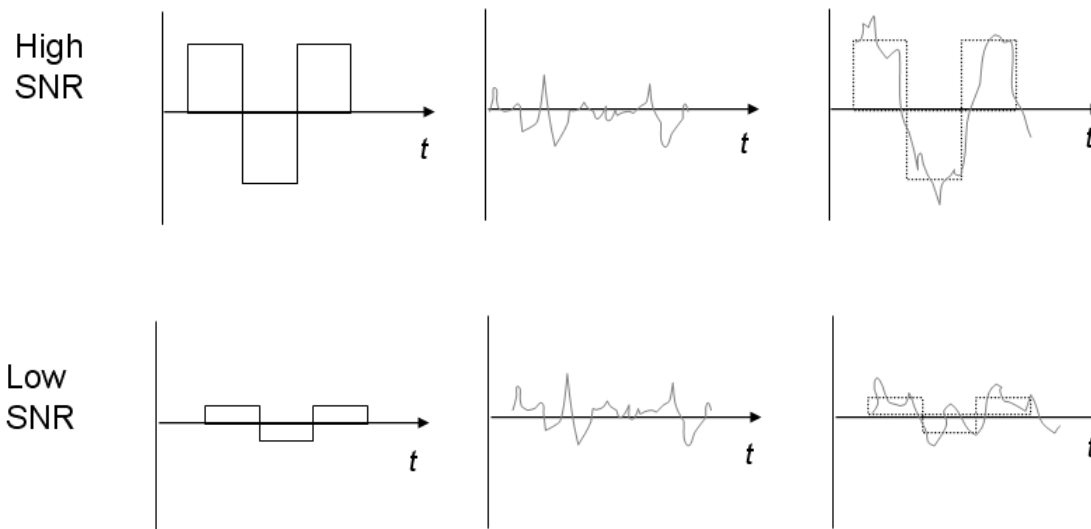
$$\begin{aligned} s_{out}(t) &= k \cdot (\sin(2\pi f_1 t) + \sin(2\pi f_2 t))^2 = \\ &= k \cdot [\sin^2(2\pi f_1 t) + 2\sin(2\pi f_1 t)\sin(2\pi f_2 t) + \sin^2(2\pi f_2 t)] = \\ &= k \cdot \left[\frac{1 - \cos(4\pi f_1 t)}{2} + \cos(2\pi(f_1 - f_2)t) - \cos(2\pi(f_1 + f_2)t) + \frac{1 - \cos(4\pi f_2 t)}{2} \right] \end{aligned}$$

Signal to Noise Ratio (SNR) – ratio of the power in the desired signal to the power in the superimposed noise

$$\text{SNR} = \frac{\text{average signal power}}{\text{average noise power}}$$

$$\text{SNR (dB)} = 10 \log_{10} \text{SNR}$$

- **high SNR \Rightarrow high-quality signal and low number of required amplifiers / repeaters**



Analog Transmission

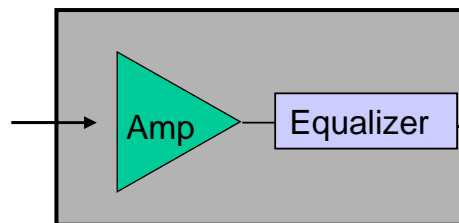
Analog Long-Distance Communications

Goals:

- 1) restore amplitude
- 2) remove delay distortion
- 3) remove noise

- each repeater attempts to restore analog signal to its original form
- **restoration (noise removal) is imperfect – noise gets amplified too !**
 - if signal only had components in certain frequency band, repeater could remove noise components outside signal band – but, not those inside ☹
- signal quality decreases with # of repeaters ⇒ **communications is distance-limited**
- analogy: copy a song using a cassette recorder

Attenuated and distorted signal
+
noise



Repeater

Recovered signal
+
residual noise

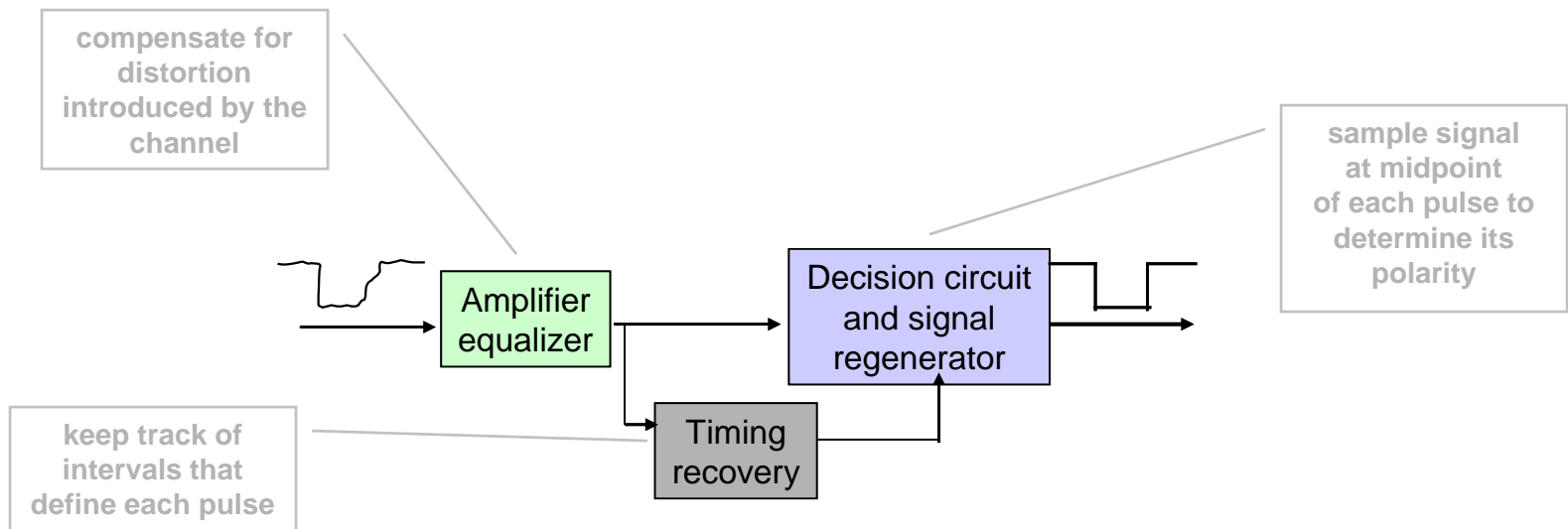




Digital Transmission

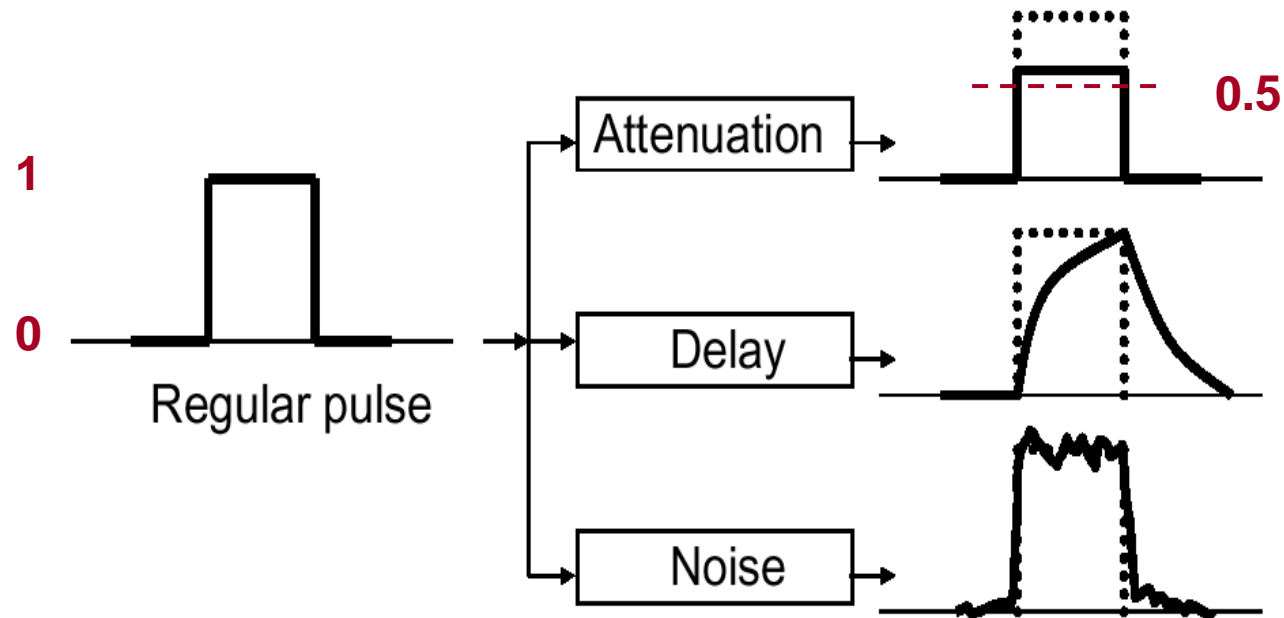
Digital Long-Distance Communications

- **regenerator does not need to completely recover the original shape of the transmitted signal** – it only needs to determine whether the original pulse was positive or negative
- original signal can be completely recovered each time \Rightarrow **communication over very long distance is possible**
- analogy: copy an MP3 file



Example [transmission impairments in digital transmission]

Digital transmission can easily recover from various types of channel impairments.



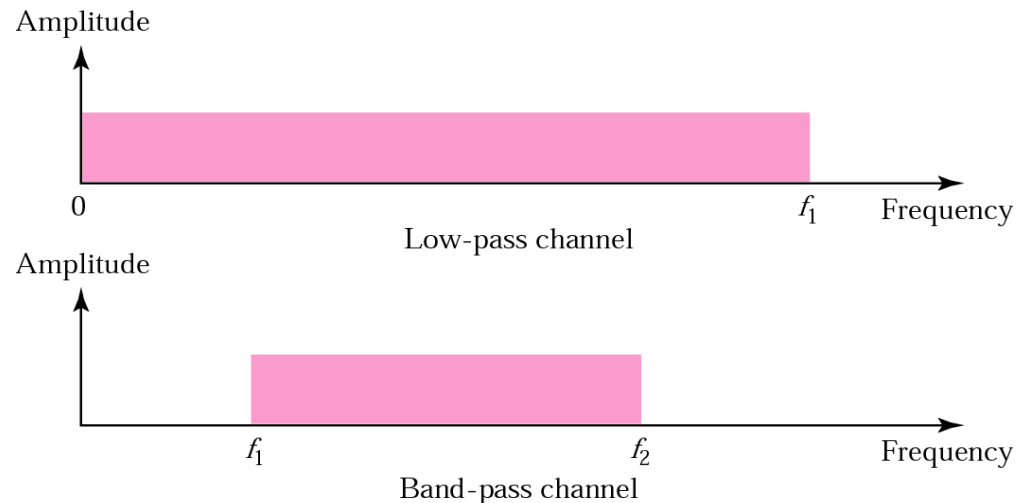
So, is digital transmission the ultimate winner?!

Low-pass Channel – bandwidth = $[0, f_1)$

- **entire medium (bandwidth) is dedicated to two devices**
- **devices alternate in transmission**

Band-pass Channel – bandwidth = $[f_1, f_2)$

- **medium is shared among multiple users**
- **each pair of users gets a portion of overall bandwidth**



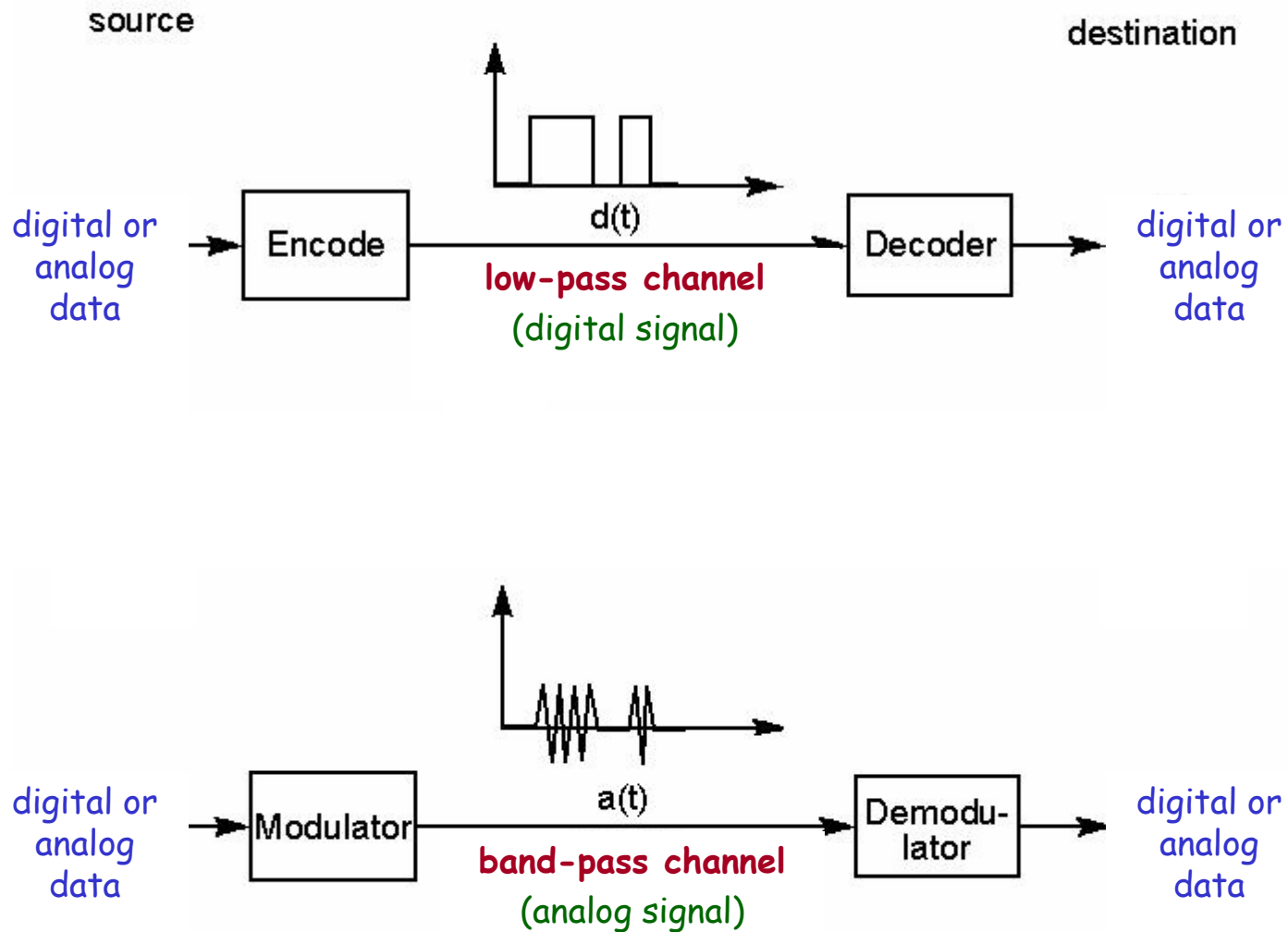
Digital Transmission Advantages

- signal can be transmitted over long-distance without losing any quality
- can operate with lower signal levels \Rightarrow lower system cost
- easier to apply encryption
- easier integration of voice, video and data

Digital Transmission Disadvantages

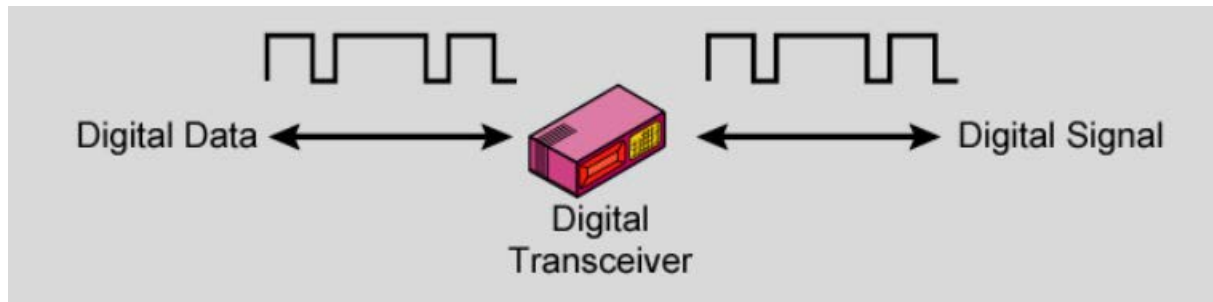
- digital signal theoretically needs a bandwidth $[0, \infty)$ – upper limit can be relaxed if we decide to work with a limited number of harmonics \Rightarrow **digital transmission needs a low-pass channel**
- **analog transmission can use a band-pass channel**

Both analog and digital data may be transmitted on suitable transmission media using either **digital coding** or **analog modulation**.

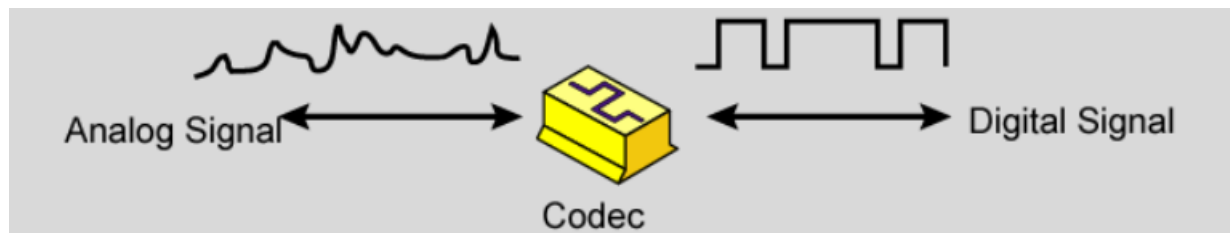


Example [digital transmission of digital and analog data]

Digital Data → Digital Signal: **Line Coding**

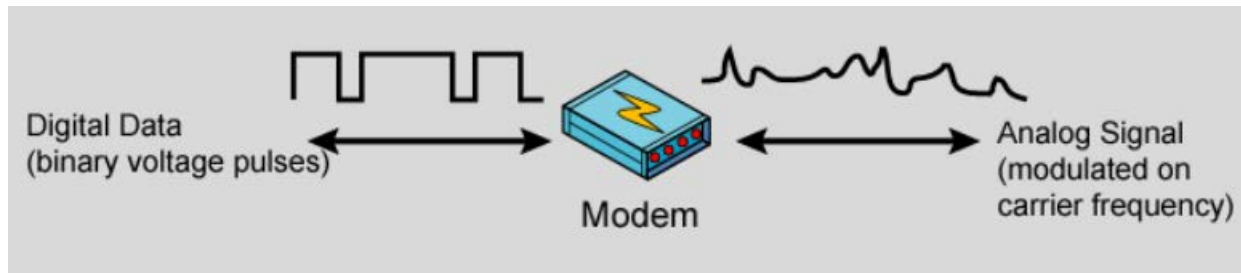


Analog Data → Digital Signal: **PCM (Pulse Code Modul.) or Delta Modulation**

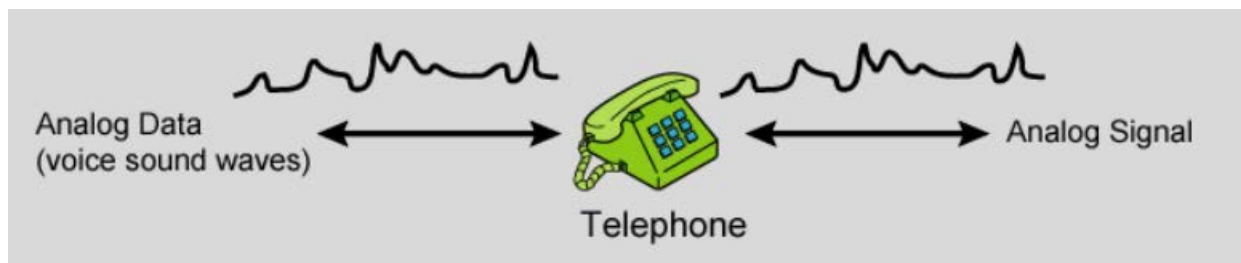


Example [analog transmission of digital and analog data]

Digital data → Analog Signal: **Digital Modulation**



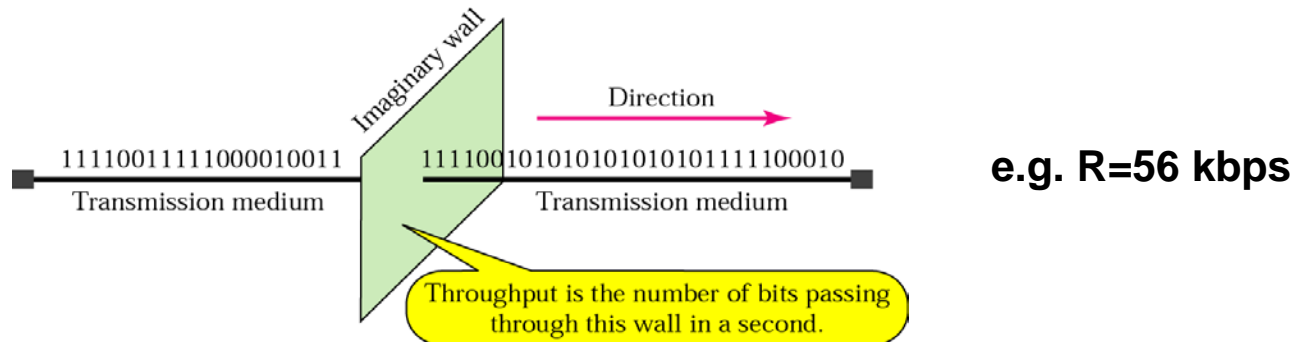
Analog data → Analog Signal: **Analog Modulation**



Last Note about Signals ...

Throughput – measurement of how fast data can pass through an entity in the network (computer, router, channel, etc.)

- if we consider this entity as a wall through which bits pass, throughput is the number of bits that can pass this wall in one second



Example [throughput]

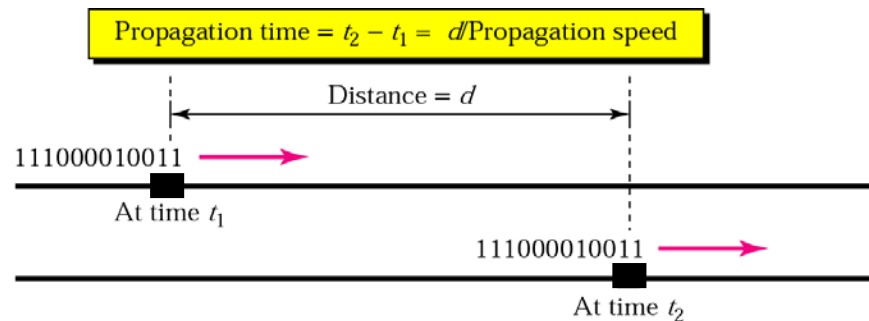
If the throughput at the connection between a device and the transmission medium is 56 kbps, how long does it take to send 100,000 bits out of this device?

$$t = \frac{N[\text{bits}]}{R[\text{bps}]} = \frac{100000 [\text{bit}]}{56000 [\text{bps}]} = 1,786 [\text{sec}]$$

Propagation Time – measures the time required for a signal (or a bit) to travel from one point of the transmission medium to another

$$p = \frac{d}{c} [\text{sec}]$$

- d – length of physical link [m]
- c – signal propagation speed in medium $\sim 2 \cdot 10^8$ [m/s]



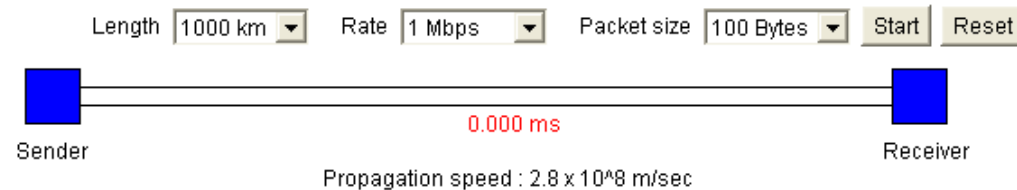
Example [propagation time]

The light of the Sun takes approximately 8 minutes to reach the Earth? What is the distance between the Sun and the Earth?

$$d = p [\text{sec}] \cdot c \left[\frac{\text{m}}{\text{sec}} \right] = 8 * 60 [\text{sec}] \cdot 3 \cdot 10^8 \left[\frac{\text{m}}{\text{sec}} \right] = 144 \cdot 10^9 [\text{m}] = 144 \cdot 10^6 [\text{km}]$$

Overall Delay

- L [bits] number of bits in message
- R [bps] speed of digital transmission system
- d [m] distance in meters
- c [m/s] speed of light (3×10^8 m/s in vacuum)



Time to deliver a block of L bits:

$$\text{Delay} = t_{\text{propagation}} + t_{\text{transmission}} = \frac{d}{c} [\text{sec}] + \frac{L}{R} [\text{sec}]$$

Use data compression to reduce L .

Use higher speed modem/cable to increase R .

Place server closer to reduce d .