#### Hash-Based Indexes

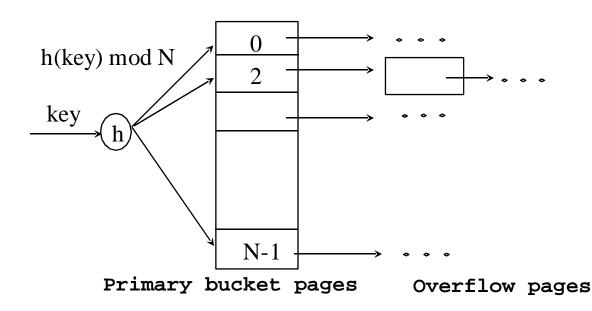
Chapter 11

#### Introduction

- As for any index, 3 alternatives for data entries**k**\*:
  - Data record with key value k
  - <k, rid of data record with search key value k>
  - $\langle \mathbf{k}$ , list of rids of data records with search key  $\mathbf{k} \rangle$
  - Choice orthogonal to the *indexing technique*
- \* <u>Hash-based</u> indexes are best for <u>equality selections</u>.
  Cannot support range searches.
- Static and dynamic hashing techniques exist; tradeoffs similar to ISAM vs. B+ trees.

# Static Hashing

- # primary pages fixed, allocated sequentially, never de-allocated; overflow pages if needed.
- h(k) mod M = bucket to which data entry with key k belongs. (M = # of buckets)



## Static Hashing (Contd.)

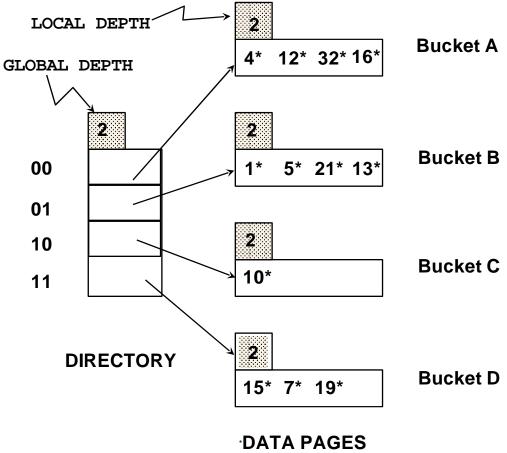
- \* Buckets contain data entries.
- ❖ Hash fn works on search key field of record r. Must distribute values over range 0 ... M-1.
  - h(key) = (a \* key + b) usually works well.
  - a and b are constants; lots known about how to tune **h**.
- Long overflow chains can develop and degrade performance.
  - *Extendible* and *Linear Hashing*: Dynamic techniques to fix this problem.

## Extendible Hashing

- Situation: Bucket (primary page) becomes full. Why not re-organize file by *doubling* # of buckets?
  - Reading and writing all pages is expensive!
  - <u>Idea</u>: Use <u>directory of pointers to buckets</u>, double # of buckets by *doubling the directory*, splitting just the bucket that overflowed!
  - Directory much smaller than file, so doubling it is much cheaper. Only one page of data entries is split. No overflow page!
  - Trick lies in how hash function is adjusted!

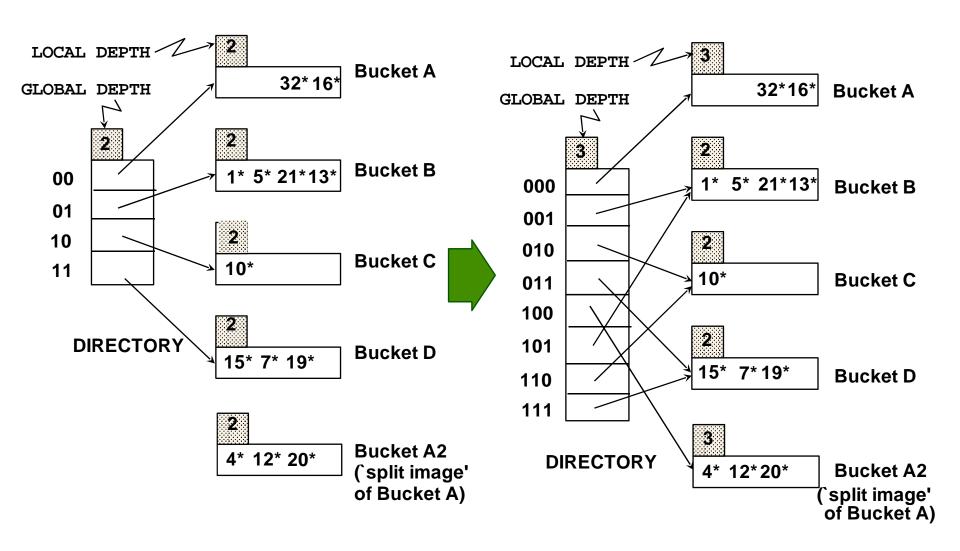


- ❖ Directory is array of size 4.
- To find bucket for r, take last 'global depth' # bits of h (r); we denote r by  $\mathbf{h}(r)$ .
  - If  $\mathbf{h}(r) = 5 = \text{binary } 101$ , it is in bucket pointed to by 01.



- ·<u>Insert</u>: If bucket is full, <u>split</u> it (allocate new page, re-distribute).
- · If necessary, double the directory. (As we will see, splitting a
- · bucket does not always require doubling; we can tell by
- · comparing *global depth* with *local depth* for the split bucket.)

## Insert h(r)=20 (Causes Doubling)

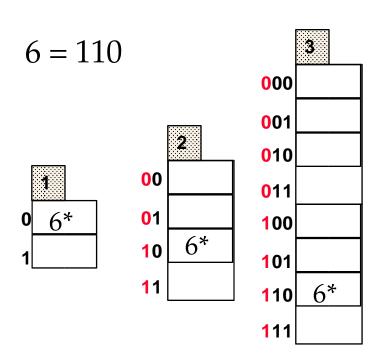


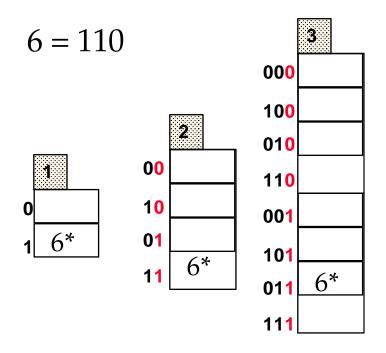
#### Points to Note

- \* 20 = binary 10100. Last **2** bits (00) tell us *r* belongs in A or A2. Last **3** bits needed to tell which.
  - Global depth of directory: Max # of bits needed to tell which bucket an entry belongs to.
  - Local depth of a bucket: # of bits used to determine if an entry belongs to this bucket.
- When does bucket split cause directory doubling?
  - Before insert, local depth of bucket = global depth. Insert causes local depth to become > global depth; directory is doubled by copying it over and 'fixing' pointer to split image page. (Use of least significant bits enables efficient doubling via copying of directory!)

# Directory Doubling

- •Why use least significant bits in directory?
- •Allows for doubling via copying!





Least Significant

VS.

Most Significant

# Comments on Extendible Hashing

- ❖ If directory fits in memory, equality search answered with one disk access; else two.
  - 100MB file, 100 bytes/rec, 4K pages contains 1,000,000 records (as data entries) and 25,000 directory elements; chances are high that directory will fit in memory.
  - Directory grows in spurts, and, if the distribution of hash values is skewed, directory can grow large.
  - Multiple entries with same hash value cause problems!
- ❖ <u>Delete</u>: If removal of data entry makes bucket empty, can be merged with 'plit image'. If each directory element points to same bucket as its split image, can halve directory.

# Linear Hashing

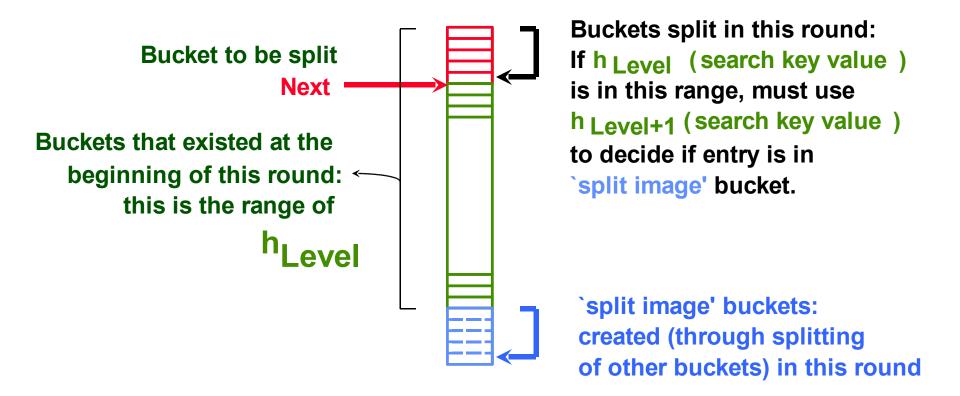
- This is another dynamic hashing scheme, an alternative to Extendible Hashing.
- LH handles the problem of long overflow chains without using a directory, and handles duplicates.
- $\bullet$  <u>Idea</u>: Use a family of hash functions  $\mathbf{h}_0$ ,  $\mathbf{h}_1$ ,  $\mathbf{h}_2$ , ...
  - $h_i(key) = h(key) \mod(2^iN)$ ; N = initial # buckets
  - **h** is some hash function (range is *not* 0 to N-1)
  - If  $N = 2^{d0}$ , for some d0,  $h_i$  consists of applying h and looking at the last di bits, where di = d0 + i.
  - $\mathbf{h}_{i+1}$  doubles the range of  $\mathbf{h}_{i}$  (similar to directory doubling)

## Linear Hashing (Cont.)

- Directory avoided in LH by using overflow pages, and choosing bucket to split round-robin.
  - Splitting proceeds in 'rounds'. Round ends when all  $N_R$ initial (for round *R*) buckets are split. Buckets 0 to *Next*-1 have been split; Next to  $N_R$  yet to be split.
  - Current round number is Level.
  - Search: To find bucket for data entry r, find  $\mathbf{h}_{Level}(r)$ :
    - If  $\mathbf{h}_{Level}(r)$  in range '*Next* to  $N_R$ ', r belongs here.
    - Else, r could belong to bucket  $\mathbf{h}_{Level}(r)$  or bucket  $\mathbf{h}_{Level}$  $(r) + N_R$ ; must apply  $\mathbf{h}_{I,evel+1}(r)$  to find out.

# Overview of LH File

❖ In the middle of a round.

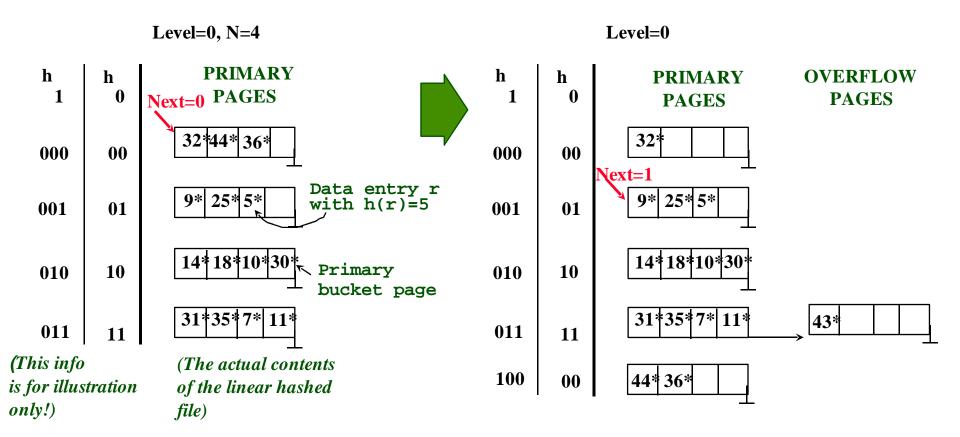


## Linear Hashing (Contd.)

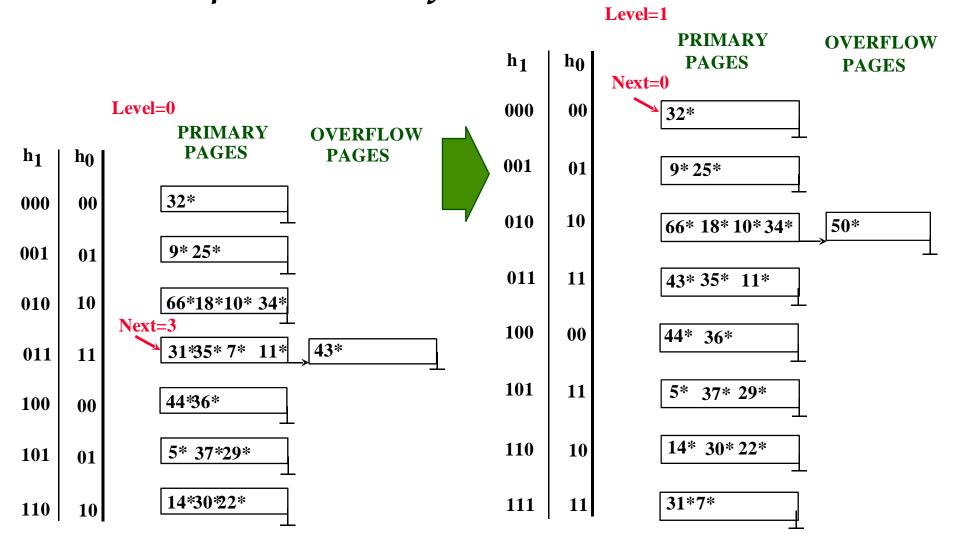
- $\bigstar$  Insert: Find bucket by applying  $\mathbf{h}_{Level}$  /  $\mathbf{h}_{Level+1}$ :
  - If bucket to insert into is full:
    - Add overflow page and insert data entry.
    - (*Maybe*) Split *Next* bucket and increment *Next*.
- Can choose any criterion to `trigger' split.
- Since buckets are split round-robin, long overflow chains don't develop!
- Doubling of directory in Extendible Hashing is similar; switching of hash functions is *implicit* in how the # of bits examined is increased.

# Example of Linear Hashing

❖ On split, h<sub>Level+1</sub> is used to re-distribute entries.



#### Example: End of a Round



#### LH Described as a Variant of EH

- The two schemes are actually quite similar:
  - Begin with an EH index where directory has *N* elements.
  - Use overflow pages, split buckets round-robin.
  - First split is at bucket 0. (Imagine directory being doubled at this point.) But elements <1,N+1>, <2,N+2>, ... are the same. So, need only create directory element *N*, which differs from 0, now.
    - When bucket 1 splits, create directory element *N*+1, etc.
- So, directory can double gradually. Also, primary bucket pages are created in order. If they are allocated in sequence too (so that finding i-th is easy), we actually don't need a directory! That is LH.

#### Summary

- Hash-based indexes: best for equality searches, cannot support range searches.
- Static Hashing can lead to long overflow chains.
- Extendible Hashing avoids overflow pages by splitting a full bucket when a new data entry is to be added to it. (Duplicates may require overflow pages.)
  - Directory to keep track of buckets, doubles periodically.
  - Can get large with skewed data; additional I/O if this does not fit in main memory.

#### Summary (Cont.)

- Linear Hashing avoids directory by splitting buckets round-robin, and using overflow pages.
  - Overflow pages not likely to be long.
  - Duplicates handled easily.
  - Space utilization could be lower than Extendible Hashing, since splits not concentrated on 'dense' data areas.
    - Can tune criterion for triggering splits to trade-off slightly longer chains for better space utilization.
- \* For hash-based indexes, a *skewed* data distribution is one in which the *hash values* of data entries are not uniformly distributed!